



Magnetic Field Effect on Lid-Driven Porous Cavity Heated to the Right Wall

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ABSTRACT

In the present investigation, we report the behavior of magnetohydrodynamics mixed convective flow (MHD-MCF) of Cu-water nanofluid (Prandtl number, $Pr = 6.2$) inside a lid-driven porous square cavity is carried out. The hot temperature is applied on the right side of the cavity (wall). The governing equations are defined using continuity, momentum, and energy equations. Further, the continuity and momentum equations are transformed into a streamfunction-vorticity approach and solved using the finite difference method. The solutions are obtained through an implication of implicit scheme and successive under relaxation. The results of MHD-MCF within a cavity are represented by using the streamfunction (ψ), isotherms (θ) and heatfunction (IT) for various values of Darcy number $10^{-2} \leq Da \leq 10^2$, Reynolds number ($1 \leq Re \leq 10$) and Hartmann number ($0 \leq Ha \leq 50$) at a fixed solid volume fraction ($\phi = 0.1$). An improvement in convective flow circulation is noticed on higher values of the Darcy number. Also, free convective effects are found to be prominent at lower Re and forced convection effects make domination on higher Re

Keywords: Mixed field, Magnetic convection, Porous, Heatlines

1. Introduction

The necessity of heat transfer and fluid flow in porous media is increasing and advancing due to its huge variety of applications in the field of science, engineering, and technology. Some important applications for this type of problem are heat exchangers, separation

processes in chemical industries, contaminant transport, geophysical problem, aquifer transport, etc. A comprehensive overview of the transport of fluids in porous media can be found in [1, 2]. Also, Applications of convection in porous media are found in [3-5]. In the past few years, the blending of nano-sized particles to the nor-

mal to the normal conventional fluid is emerging due to its eligibility of increasing the overall thermophysical properties of the fluids [6, 7]. For instance, Sumit Gupta et al. [8] considered Ag/TiO₂-water based nanofluids to pass over the vertical stretching sheet and analyzed the MHD free convective flows (MHD-FCF). Moreover, Sumit Gupta et al. [9] explored the heat/mass transfer of Cu-water and Al₂O₃-water nanofluid due to radiative MHD convective flow over an exponentially stretching surface. Recently, Jino and Vanav [10] examined the heat transfer and fluid flow (HTFF) within a Cu-Al₂O₃-water nanofluid packed porous cavity due to MHD-FCF. From the above studies, it is noticed that the heat transfer rate is increased by the nanofluids. In addition, Cu nanoparticle is found to actively improve the heat transfer performance over the other nanoparticles.

An impact of magnetic field effect in free convection on Al₂O₃-water nanofluid-filled square cavity is discussed by Ghasemi et al. [11]. It is noticed that the augmentation in Ha makes a reduction in the convective HTFF. Selimefendigil and Öztop [12] explored the MHD-FCF and its entropy generation inside a square enclosure with different shaped obstacles present inside. Selimefendigil et al. [13] later discussed in detail about the MHD-MCF and generation of the entropy in a cavity-filled nanofluid. Basak et al. [14-16] analyzed the effect of mixed convective HTFF in a lid-driven square-shaped cavity with various types of boundary conditions. From their studies, it is observed that the heat transfer increases by augmenting the Darcy number and Grashof number. An increase in Reynolds number leads to forced convection to be dominant. Also, the flow intensity improved with the increase in Darcy number. Emami et al. [17] investigated the free convection effects on HTFF in an inclined porous cavity filled with Cu-water nanofluid. The study concludes that every parameter involved in the study

such as inclination angle, Da , Ra and ϕ holds the responsibility in HTFF.

Wilkes [18] explained the finite difference computations (FDC) to solve the FCF within a rectangular cavity. Moreover, Rudriah et al. [19] extended the FCF to MHD-FCF within a cavity by using FDC. Recently, Jino and Vanav [20] used FDC to solve the MHD-FCF in a Cu-water nanofluid-packed porous enclosure. Other than the FDC techniques, Jagdev Singh et al. [21, 22] used hybrid methods such as homotopy perturbation Elzaki/homotopy analysis transform to solve the non-linear equations to interpret the fluid flow. Also, Sumit Gupta et al. [23] considered Homotopy analysis to determine the analytical solution to interpret the nanofluid flow over the variable thickness surfaces due to radiative MHD flows.

Grosan et al. [24] discussed the HTFF within a porous enclosure on MHD-FCF and heat generation effect. Revnic et al. [25] discussed the unsteady natural convective flow in a porous cavity. The study apprises that the diffusive heat transfer becomes prominent when increasing the Ha and Ra . Rashad et al. [26] analyzed the internal heat generation and MHD-FCF within a rectangular enclosure that is filled with Cu-water nanofluid. The result highlights that the heat transfer increases with ϕ . Also, when advancing Ha , the maximum value of the temperature enhances and streamfunction intensity decreases. Jino et al. [27-31] discussed the MHD-FCF in a porous square cavity filled with Cu-water nanofluid. The porous media is framed using the Carman-Kozeny/Darcy-Brinkman equations. The studies are discussed with various thermal boundaries. Also, heatfunction visualization was incorporated for better prediction of heat flow. From the studies, it is noted that the heatfunction study is indispensable for understanding the heat flow. In addition, it is noted that the Cu-water nanofluid involves in enhancement in the heat transfer process. Sivasankaran et al. [32] numerically studied

the MCF in a lid-driven porous cavity containing Cu-water nanofluid by considering a partial slip. Chamkha et al. [33] discussed the effect of source-sink on MHD-MCF within a lid-driven porous cavity. Chamkha et al. [33] investigated the MHD-MCF within a porous lid-driven cavity. It is noted that the addition of Cu nanoparticles enhances entropy generation. Sheikholeslami [34] discussed nanofluids' MHD-MCF in a lid-driven porous cavity. The results denote that the effect of convective heat transfer increases for an increase in Da and Re . Also, it is noted that the heat transfer declines with Ha . Çolak et al. [35] explored the HTFF due to convection and partially heated block within a cavity. The results show that the heat transfer is drastically increasing on higher Da as well as with the orientation in the heater block.

The present study illustrates the MHD-MCF on the lid-driven porous enclosure of square-shaped. The Cu-water nanofluid's HTFF is discussed by using the flow contour visualization tools such as streamlines, heatlines, and isotherms. The role of Ha , Da and Re in flow characteristics by heating the right side of the cavity are demonstrated.

2. Problem Description

The two-dimensional square cavity of side distance $H \times H$, filled up with the Cu-water nanofluid is considered. The properties of the loaded nanofluid (base fluid and nanoparticle) are given in Table 1.

The velocities u and v are considered along the horizontal direction x and vertical direction y . The right side of the cavity is maintained at higher temperature (T_h), (T_c)

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0 \tag{2.1}$$

$$\rho_n \left[u \frac{\partial u}{\partial x} + v \frac{\partial v}{\partial y} \right] = \mu_n \left(\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 v}{\partial y^2} - u \frac{\mu_n}{K} \right) - \frac{\partial p}{\partial x} \tag{2.2}$$

left wall is maintained at a lower temperature (T_c) and the other two walls are adiabatic respectively. The top wall of the cavity is moving with the uniform velocity ($u = U_0$) and other walls are maintained stationary as shown in the Fig. 1.

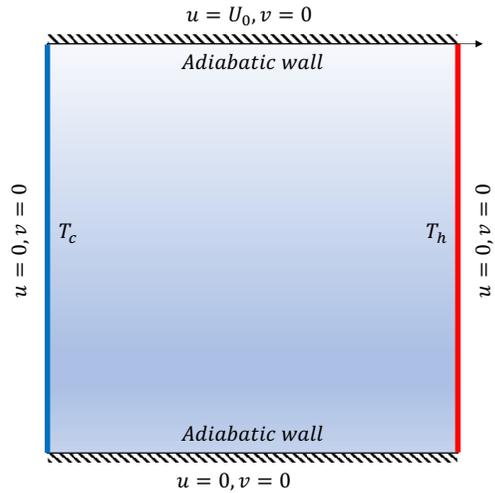


Fig. 1. Problem model.

Table 1. Physical properties.

	Water	Cu particle
ρ (kg / m^3)	997.1	8933
μ ($Pa s$)	8.9×10^{-4}	–
c_p ($J / kg K$)	4179	385
k ($W / m K$)	0.613	401
σ (S / m)	0.05	5.96×10^7
β (K^{-1})	2.1×10^{-4}	16.7×10^{-4}

The Boussinesq approximation is applicable for fluid properties and the other properties are maintained constant. By the assumptions made, the governing equations for flow in a cavity are given by,

$$\rho_n \left[u \frac{\partial u}{\partial x} + v \frac{\partial v}{\partial y} \right] = \mu_n \left(\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 v}{\partial y^2} - v \frac{\mu_n}{K} \right) - \frac{\partial p}{\partial y} + (\rho\beta)_n g(T_h - T_c) - \sigma_n B_0^2 v \quad (2.3)$$

$$(\rho c_p)_n \left[u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} \right] = k_n \left(\frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} \right) \quad (2.4)$$

where the thermophysical properties are the function of solid volume fraction is given by,

$$\mu_n = \mu_f / (1 - \phi)^{2.5} \quad (2.5)$$

$$\mu_n = \mu_f / (1 - \phi) \rho_f + \phi \rho_p \quad (2.6)$$

$$(\rho c_p)_n = (1 - \phi)(\rho c_p)_f + \phi(\rho c_p)_p \quad (2.7)$$

$$(\rho\beta)_n = (1 - \phi)(\rho\beta)_f + \phi(\rho\beta)_p \quad (2.8)$$

$$k_n = k_f \left[\frac{k_p + 2k_f - 2\phi(k_f - k_p)}{k_p + 2k_f - 2\phi(k_f - k_p)} \right] \quad (2.9)$$

Also, the velocities (u, v) , pressure (p) and temperature (T) are the function of two-dimensional space x and y , respectively.

The above dimensional governing Eqs. (2.1-2.4) can be non-dimensionalized using the parameters,

$$\frac{\partial U}{\partial X} + \frac{\partial V}{\partial Y} = 0 \quad (2.10)$$

$$U \frac{\partial U}{\partial X} + V \frac{\partial V}{\partial Y} = \frac{\mu_n \rho_f}{\rho_n \mu_f} \cdot \frac{1}{Re} \left(\frac{\partial^2 U}{\partial X^2} + \frac{\partial^2 U}{\partial Y^2} - \frac{U}{Da} \right) - \frac{\rho_f}{\rho_n} \cdot \frac{\partial P}{\partial X} \quad (2.11)$$

$$U \frac{\partial V}{\partial X} + V \frac{\partial V}{\partial Y} = \frac{\mu_n \rho_f}{\rho_n \mu_f} \cdot \frac{1}{Re} \left(\frac{\partial^2 V}{\partial X^2} + \frac{\partial^2 V}{\partial Y^2} - \frac{V}{Da} \right) - \frac{\rho_f}{\rho_n} \cdot \frac{\partial P}{\partial Y} + \frac{(\rho\beta)_n}{\rho_n \beta_f} \cdot \frac{Gr}{Re^2} \theta - \frac{\rho_f \sigma_n}{\rho_n \sigma_f} \cdot \frac{Ha^2}{Re} V \quad (2.12)$$

$$U \frac{\partial \theta}{\partial X} + V \frac{\partial \theta}{\partial Y} = \frac{\alpha_n}{\alpha_f} \left(\frac{\partial^2 \theta}{\partial X^2} + \frac{\partial^2 \theta}{\partial Y^2} \right) \quad (2.13)$$

The pertinent dimensionless flow equations are solved using the thermal boundaries as $\theta = 1$ at the left wall, $\theta = 0$ at the right wall, and $\partial\theta/\partial Y = 0$ at the horizontal wall. Top lid movement, $U_0 = 1, V = 0$ and remaining wall velocities as $U = 0, V = 0$.

$$\begin{aligned} U &= \frac{u}{U_0}, & V &= \frac{v}{U_0}, \\ X &= \frac{x}{H}, & Y &= \frac{y}{H}, \\ P &= \frac{p}{\rho_f U_0^2}, & \theta &= \frac{T - T_c}{T_h - T_c}, \\ Pr &= \frac{\nu_f}{\alpha_f}, & Re &= \frac{U_0 H}{\nu_f}, \\ Da &= \frac{k}{H^2}, & Ha &= B_0 H \sqrt{\frac{\sigma_f}{\rho_f \nu_f}}, \\ Gr &= \frac{g \beta_f H^3 (T_h - T_c)}{\nu_f^2}. \end{aligned}$$

The dimensionless flow equations thus derived after the substitution of the above non-dimensional parameter to the primary two-dimensional Eqs. (2.1-2.4) as,

Streamline- ψ and heatlines- II are adopted for better picturization of the fluid and heat flow respectively.

$$\frac{\partial^2 \psi}{\partial X^2} + \frac{\partial^2 \psi}{\partial Y^2} = \frac{\partial U}{\partial Y} - \frac{\partial V}{\partial X} \quad (2.14)$$

$$\frac{\partial^2 \Pi}{\partial X^2} + \frac{\partial^2 \Pi}{\partial Y^2} = \frac{\partial(U\theta)}{\partial Y} - \frac{\partial(V\theta)}{\partial X} \quad (2.15)$$

Local Nusselt number is used to represent the transfer of heat from the right wall and it is given by,

$$Nu = \frac{k_n}{k_f} \cdot \frac{\partial \theta}{\partial X} \Big|_{wall} \quad (16)$$

3. Numerical Solution

Governing Eqs. (2.1-2.4) are non-dimensionalized (2.10-2.13) and, the continuity and momentum equations are formulated into the vorticity-streamfunction based equations. Further, the equations are solved by using the implicit-FDC. The computation is carried out still the residuals for the streamfunction get below 10^{-5} .

The work is initiated after validating the code with a previously published work. Fig. 2 shows a good comparison between the results by Basak et al. [10] and the present study.

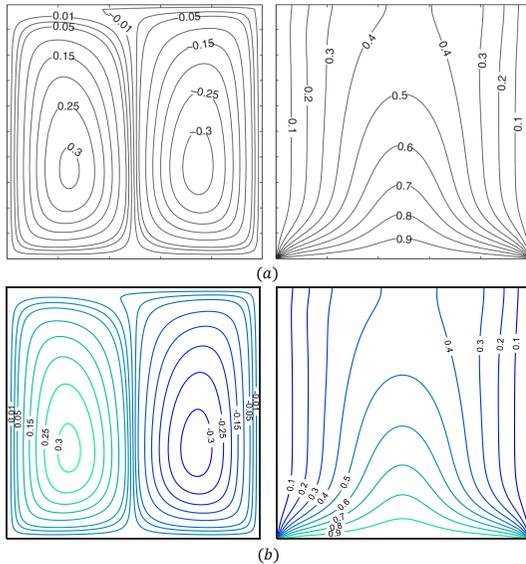


Fig. 2. Validation of ψ and θ with the earlier studies.

4. Result and Discussions

The HTFF of lid-driven porous cavity due to the MHD-MCF on heated right wall is studied by varying the dimensionless

parameters such as Darcy number ($10^{-2} \leq Da \leq 10^2$), Hartmann number ($0 \leq Ha \leq 50$) and Reynolds number ($1 \leq Re \leq 10$). The whole computation is done for fixed parameters solid volume fraction ($\phi = 0.1$), Prandtl number ($Pr = 6.2$), and Grashof number ($Gr = 10^4$). The results are framed by using ψ , θ and Π respectively. In addition, the heat transfer from the right wall is demonstrated using Nu .

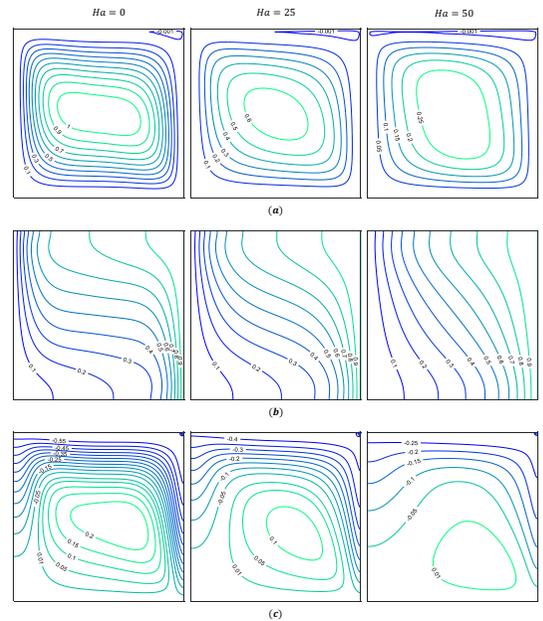


Fig 3. Streamfunction (a), Isotherms (b), Heatfunction (c) for various Ha at $Da = 10^{-2}$ and $Re = 1$.

Fig. 3 represents (a). streamlines, (b). isotherms and (c). heatlines for various values of Hartmann number ($Ha = 0, 25, 50$) at $Da = 10^{-2}$ and $Re = 1$. When the Ha equals 0, there is primary circulation which covers the major region of the cavity. Also, a small secondary circulation arises adjacent to the right wall.

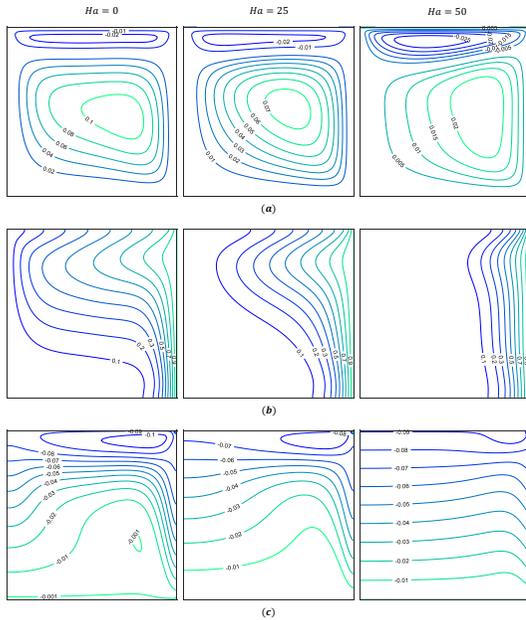


Fig 4. Streamfunction (a), Isotherms (b), Heatfunction (c) for various Ha at $Da=10^2$ and $Re=10$.

This secondary circulation at the top is due to the lid-driven effects. With respect to the ψ , the temperature is distributed from the heated wall. Moreover, the heat flow can be visualized clearly in the contour Π . The heat travels from the right wall to the left. The denser heatlines adjacent to the heated right wall and the circulation indicates the convective heat transfer. By the way, when Ha increases to 25 and 50 it causes widening of ψ contour from the horizontal direction to the vertical direction by reducing the intensity. In addition, the growth of secondary circulation is noted with the augmentation in the Ha , which is observed at the top of the cavity.

The increase in Ha causes an increase in the applied magnetic field which is from the direction left to right. It is well-known fact that the magnetic field subdues the flow of fluid inside the cavity by the resistive force. At $Ha=0$, the flow is free from any kind of magnetic force hence, the circulation of fluid is intense as seen from Streamlines of Fig. 3(a) (left). As Ha increases, the

circulation of fluid is less intense due to the suppressive act of an applied magnetic field. Hence, the contours represent the same in Fig. 3(a) (middle and right) as compared to Fig. 3(a) (middle). However, as the convective effects are getting weak (heatlines also represent the same), the fluid is replaced by a counter flow from the right corner as seen from Fig. 3(a)(right), which is also supported by the moving lid. This eventually is due to the conservation of mass law, which is the equation of continuity.

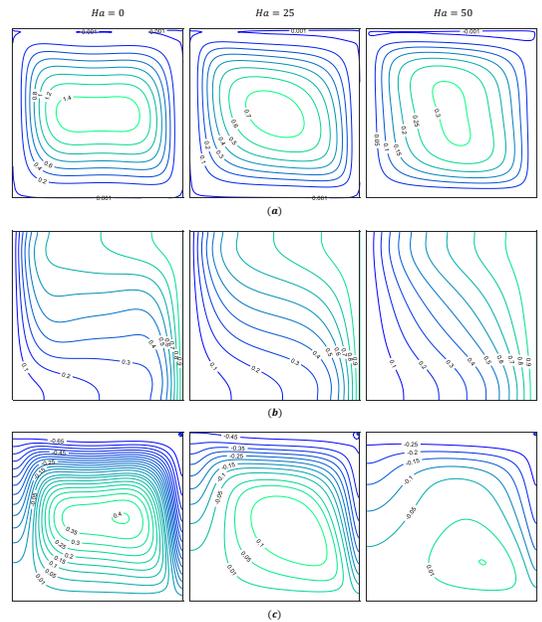


Fig 5. Streamfunction (a), Isotherms (b), Heatfunction (c) for Ha at $Da=10^2$ and $Re=1$.

Similarly, Fig 4 represents the flow patterns for $Re=10$. Here, the bottom primary circulation intensity is reduced as compared to Fig 3. Also, the secondary circulation has grown more than ten times. This is due to the action of forced convection. By increasing Re , the force from the lid drives the flow and thus rises the secondary circulation. Since the primary circulation is weaker than at the lower Re , temperature distribution over the entire cavity is affected. Moreover, only where the region between

both the circulations are met, where the temperature distribution is more. From the contour θ , it is clearly visible that the bottom heatline circulation is weaker as compared to the top secondary circulation. This illustrates the forced convective heat transfer than the natural convection. However, while $Ha = 50$ there is no circulation detected, and this signs the conductive dominated heat flow.

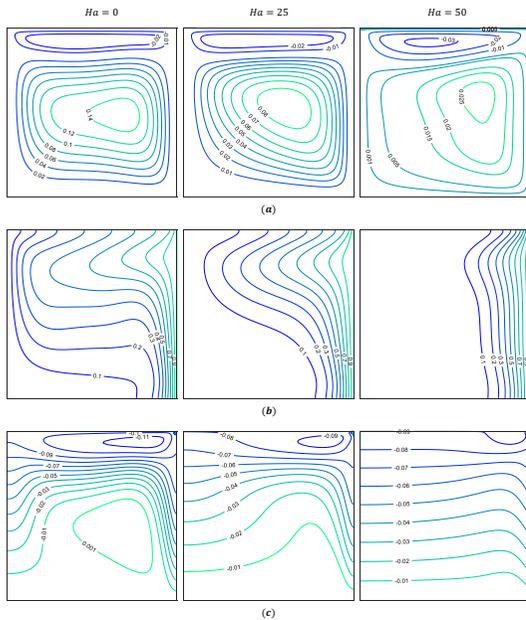


Fig 6. Streamfunction (a), Isotherms (b), Heatfunction (c) for various Ha at $Da=10^2$ and $Re=10$.

Fig. 5 represents the flow field for various Ha at $Da=10^2$ and $Re=1$. At $Da=10^2$, the contours of ψ , θ and θ are looks similar as in the case of $Da=10^{-2}$. However, the intensity of streamfunction increases due to the increase in permeability. This leads to augmentation in the buoyancy effect than the viscous force. The intense flow causes the temperature to distribute all over the cavity and increases the convective heat transfer rate. In the absence of a magnetic field effect, the heatline circulation intensity is much higher and denser lines are observed adjacent to the right wall. In addition, no secondary

circulations are noted. This leads us to conclude the domination of the free convective heat transfer regime. This FCF gets destroyed by the action of augmenting Ha . This can be noticed in the heatline plots (reduced denser lines and circulations) on $Ha = 25$ and 50 . Meanwhile, in Fig. 6, it is noticed that the increase in Re to 10 also increases overall flow intensity as compared to the lower Darcy number ($Da=10^{-2}$).

Because of the increased permeability and forced convective behavior, overall secondary circulation intensity is raised.

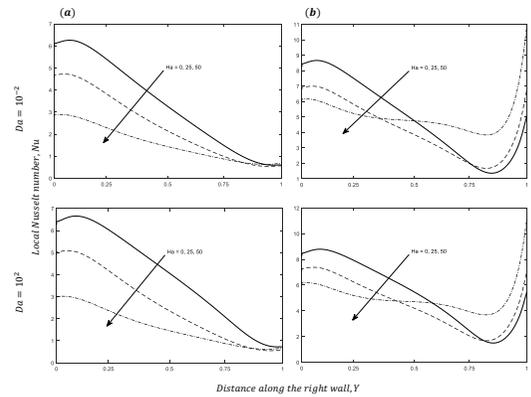


Fig. 7. Visualization of local Nusselt number.

Heat transfer originates along the right wall is denoted by local Nusselt number, which is presented in Fig 7. At lesser Re , a lower portion of the right wall provides the highest heat transfer rate and gradually decreases towards the top of the wall. A very small variation in Nu due to the lid movement effect is noted in the case of $Re=1$. This Nu reduces by increasing the Hartmann number because of the resistive force generated in the flow and this leads a viscous force to slow down the convective heat transfer rate. But for the higher Re , the local Nusselt number decreases from the lower region of the right wall till $3/4^{th}$ of the cavity and increases further. Heat transfer due to lid movement (FCF) increases by quantifying the Reynolds number. At $Re=10$, the

transfer of heat decreases at bottom of the wall and increases at the top while quantifying the Ha . At the same time, the non-existence of a heatline circulation at the upper side cavity on higher Ha indicates the improvement in the conduction-based heat transfer.

5. Conclusion

The MCF in a porous lid-driven square cavity is studied by considering higher temperatures on the right wall. The study is addressed with the effects of a magnetic field. Some of the main observations are,

- Fluid velocity augments with permeability by advancing the Darcy number from 10^{-2} to 10^2 .
- An improvement in Ha leads to reducing the heatline and streamline circulations.
- Forced convective HTFF increases with increasing the Re .
- Circulations at the primary circulation (lower) are due to free convection and the top secondary circulation is due to forced convection.
- This study shows that heatline plots are indispensable for heat flow analysis and give a fine insight into the HTFF.
- At $Re = 10$, an increase in Ha causes no circulation in the heatlines. This illustrates the conduction mode of heat transfer.

Apart from this study, the authors would like to suggest future research directions. Some suggestions are,

- The different types of nanofluid can be explored. Further, the hybrid nanofluids flow has to be explored deeply.
- Exergy analysis has to be performed on various nanofluid/hybrid nanofluids flow.
- Since lesser research is carried out in the turbulent flows, importance has to be given to transitional and turbulent flows.
- Nanoparticle distribution, double-diffusive, Soret, Dufort, chemical

reactions can be incorporated into the study.

- Future research can be improved with non-linear convection, non-linear radiation based studies.
- Bifurcation studies are also recommended.

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