

Chapter III

Modifying Ma's Matrix Method to Accommodate the Presence of Bid-Ask Spread

3.1 Data Collection

This article focuses on the arbitrage opportunity with six currency(USD, JPY, GBP, SGD,HKD,EUR) in six markets(New York, Frankford, Singapore, Tokyo, London, Hong Kong). For the three month study period from Sep 1, 2008 to Nov 28, 2008, the daily exchange rate data from Datastream. Note that the data for each exchange rate is not synchronized. For example, the daily HKD/USD rate and the USD/GBP rate are not collected at the same time of day. However, we shall use this data set to illustrate the procedure of determining an arbitrage path.

3.2 Analytical Framework

Quantitative analysis is used to analyze the association between the arbitrage path, maximum bid-ask spread, profit and currency which be underpriced or overpriced. This analysis is based on Ma's matrix method, but some adjustments is made in order to accommodate the presence of the bid-ask spread.

This research performs three different matrix to analyze how the arbitrage path can be found with or without the bid-ask spread. Three month data is used. Both analysis are performed to show the arbitrage path, profit and find the currency which be underpriced or overpriced, which can provide the optimal path and maximum profit for the arbitrage. We now illustrate the method for the case with bid-ask spread, the raw data is as follows.

Table 1 Raw data with bid price and ask price

Currency pair	Price	Transaction date (65 days)						
		2008-9-1	2008-9-2	2008-9-3	2008-9-4		2008-11-27	2008-11-28
USD / EUR	bid	1.4585	1.4514	1.4491	1.4241		1.2894	1.269
	ask	1.459	1.4519	1.4496	1.4246		1.2899	1.2695
USD / GBP	bid	1.7993	1.7829	1.775	1.76		1.5393	1.5381
	ask	1.7998	1.7834	1.7755	1.7605		1.5398	1.5386
HKD / USD	bid	7.8054	7.8071	7.8075	7.8072		7.7516	7.7502
	ask	7.8064	7.8081	7.8085	7.8082		7.7526	7.7512
JPY / USD	bid	108.13	108.58	108.21	106.41		95.31	95.53
	ask	108.18	108.64	108.25	106.46		95.36	95.58
SGD / USD	bid	1.4237	1.4325	1.4351	1.4396		1.5095	1.5133
	ask	1.4247	1.4335	1.4361	1.4406		1.5105	1.5143
HKD / EUR	bid	11.3859	11.3356	11.2887	11.2284		9.9793	9.8323
	aks	11.3894	11.3387	11.2918	11.2313		9.9823	9.836
JPY / EUR	bid	157.7255	158.0066	156.7573	155.4083		123.0111	120.8183
	aks	157.8017	158.0974	156.8332	155.4839		123.0912	120.8945
SGD / EUR	bid	2.0775	2.0758	2.0765	2.063		1.9423	1.9133
	ask	2.0789	2.0772	2.0778	2.0644		1.9435	1.9148
GBP / EUR	bid	0.8109	0.8128	0.8137	0.8114		0.8353	0.8267
	ask	0.8113	0.8132	0.814	0.8118		0.8357	0.8272
JPY / GBP	bid	192.35	190.7	189.97	188.39		142.24	143.12
	ask	200.35	198.7	197.97	196.39		150.24	151.12
JPY / SGD	bid	75.66	75.23	75.14	74.84		62.2	62.63
	ask	77.32	76.89	76.8	76.5		63.86	64.29
JPY / HKD	bid	13.49	13.47	13.51	13.44		11.87	11.89
	ask	14.35	14.33	14.37	14.3		12.73	12.75
HKD / SGD	bid	5.477	5.477	5.421	5.4575		5.128	5.141
	ask	5.4845	5.4845	5.4285	5.4655		5.134	5.147
HKD / GBP	bid	14.095	14.095	13.825	13.895		11.93	11.955
	ask	14.11	14.11	13.84	13.91		11.945	11.97
SGD/GBP	bid	2.5657	2.5549	2.5501	2.5419		2.3255	2.3261
	ask	2.5657	2.5549	2.5501	2.5419		2.3255	2.3261

From the raw data, We pick Sep 1, 2008 as the example to construct matrix A, B, and C. First, we build the matrix A with bid price and ask price,. For example, 1.459 is the ask price of USD/EUR, 0.685636 equal to 1/1.4585, where the 1.4584 is the bid price of USD/EUR.

Table 2 Matrix A, using data from 1/9/2008

2008-9-1	USD	EUR	GBP	JPY	HKD	SGD
USD	1	0.685636	0.555772	108.18	7.8064	1.4247
EUR	1.459	1	0.8113	157.8017	11.3894	2.0789
GBP	1.7998	1.233198	1	200.35	14.11	2.5657
JPY	0.009248	0.00634	0.005199	1	0.074129	0.013217
HKD	0.128116	0.087828	0.070947	14.35	1	0.182582
SGD	0.702395	0.481348	0.389757	77.32	5.4845	1

Next, we calculate the $\lambda_{\max}$ and eigen values and eigenvectors associated with $\lambda_{\max}$ of matrix A with MATLAB, So we get $\lambda_{\max}=6.0221$ and $G=[g_1, g_2, \dots, g_n] = [0.3802, 0.5548, 0.6881, 0.0035, 0.049, 0.2678]$, because the exchange rate of any two currency is determined by their gold contend, therefore, there is no arbitrage opportunity and λ of matrix B is equal to n, where matrix B is the arbitrage free benchmark. We can prove (see Ma 2004) that the sufficient condition of no arbitrage is $\lambda_{\max}=n$ and the eigen value G is the gold contend. Here, we get the conclusion that there is arbitrage opportunity if $\lambda_{\max}$ not equal to n. From

$$B = \begin{bmatrix} \frac{g_1}{g_1} & \frac{g_1}{g_2} & \dots & \frac{g_1}{g_n} \\ \frac{g_2}{g_1} & \frac{g_2}{g_2} & \dots & \frac{g_2}{g_n} \\ \vdots & \vdots & \ddots & \vdots \\ \frac{g_n}{g_1} & \frac{g_n}{g_2} & \dots & \frac{g_n}{g_n} \end{bmatrix},$$

we get matrix B.

Table 3 Matrix B, using data from 1/9/2008

2008-9-1	USD	EUR	GBP	JPY	HKD	SGD
USD	1	0.685292	0.552536	108.6286	7.759184	1.419716
EUR	1.459232	1	0.806278	158.5143	11.32245	2.071695
GBP	1.809837	1.240267	1	196.6	14.04286	2.569455
JPY	0.009206	0.006309	0.005086	1	0.071429	0.013069
HKD	0.12888	0.08832	0.071211	14	1	0.182972
SGD	0.704366	0.482696	0.389188	76.51429	5.465306	1

Last, with the formula $C=A \div B$, (where $\div$ means element-by-element division), we get matrix C. for example, $0.99984=1.459/1.459232$.

Table 4 Matrix C, using data from 1/9/2008

2008-9-1	USD	EUR	GBP	JPY	HKD	SGD
USD	1	1.0005	1.005856	0.995871	1.006085	1.00351
EUR	0.99984	1	1.006228	0.995505	1.005913	1.003478
GBP	0.99445	0.9943	1	1.019074	1.004781	0.998539
JPY	1.00461	1.005	1.022095	1	1.037806	1.011291
HKD	0.99408	0.99443	0.996301	1.025	1	0.997865
SGD	0.9972	0.99721	1.001463	1.01053	1.003512	1

From matrix C, we can find which currency overpriced or underpriced. Now, we try to find an arbitrage path. we convert EUR into GBP, where GBP is underpriced, then convert GBP into HKD, where HKD is underpriced. At last we convert HKD into EUR to close the route and realize the profit. $1/0.9943*1/0.996301*1/1.005913-1=0.35328\%$. Even though this profit is calculated from the hypothetical matrix C, we can show that it is equal to the real profit computed using real-world exchange rate from matrix A. To see this, suppose that we followed the path EUR -> GBP -> HKD -> EUR, using the rates quoted in matrix A. The profit from this transaction (taking in the effect of bid-ask spread) is $(1 / 1.233198 / 0.070947 / 11.3894) - 1 = 0.35328\%$, which is equal to the profit computed from the numbers in matrix C.

3.3 Result

Result presented in two tables. Table 5 shows the arbitrage with bid-ask spread and Table 6 shows the arbitrage without bid-ask spread.

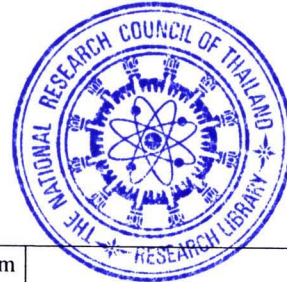
Table 5 Arbitrage with bid-ask spread

	$\lambda_{\max}$	Path	Profit(%)	Underpriced	Overpriced
2008-9-1	6.0221	EUR-GBP-HKD-EUR	0.353	GBP/ EUR HKD/ GBP	EUR/HKD
2008-9-2	6.0222	USD-GBP-HKD-USD	1.221	GBP/USD HKD/GBP	USD/HKD
2008-9-3	6.0221	HKD-GBP-EUR-HKD	0.381	GBP/HKD HKD/ EUR	EUR/GBP
2008-9-4	6.0224	USD-EUR-JPY-USD	2.469	EUR/USD JPY/ EUR USD/JPY	
2008-9-5	6.0227	USD-JPY-EUR-USD	1.141	JPY/USD USD/ EUR	EUR/JPY
2008-9-8	6.0223	USD-GBP-HKD-USD	1.055	GBP/USD HKD/GBP	USD/HKD
2008-9-9	6.0225	USD-EUR-JPY-USD	0.706	EUR/USD JPY/ EUR	USD/JPY
2008-9-10	6.0226	USD-GBP-HKD-USD	0.798	GBP/USD HKD/GBP	USD/HKD
2008-9-11	6.0227	USD-JPY-EUR-USD	1.246	JPY/USD USD/ EUR	EUR/JPY
2008-9-12	6.0227	USD-SGD-GBP-USD	1.867	SGD/USD GBP/SGD USD/GBP	
2008-9-15	6.0227	USD-HKD-GBP-USD	1.569	HKD/USD GBP/HKD	USD/GBP
2008-9-16	6.0231	EUR-GBP-HKD-EUR	1.128	GBP/ EUR HKD/GBP	EUR/HKD
2008-9-17	6.0228	USD-HKD-GBP-USD	0.845	HKD/USD	GBP/HKD, USD/GBP
2008-9-18	6.023	USD-EUR-SGD-USD	0.309	EUR/USD SGD/ EUR	USD/SGD
2008-9-19	6.0227	EUR-HKD-GBP-EUR	1.484	HKD/EUR EUR/GBP GBP/HKD	
2008-9-22	6.0224	USD-HKD-EUR-USD	1.031	HKD/USD USD/EUR	EUR/HKD
2008-9-23	6.0224	USD-EUR-HKD-USD	0.382	EUR/USD HKD/EUR	USD/HKD
2008-9-24	6.0225	USD-GBP-HKD-USD	0.390	GBP/USD HKD/GBP	USD/HKD
2008-9-25	6.0228	USD-GBP-HKD-USD	1.087	GBP/USD HKD/GBP	USD/HKD
2008-9-26	6.0225	USD-GBP-SGD-USD	0.351	GBP/USD SGD/GBP	USD/SGD
2008-9-29	6.0225	USD-GBP-JPY-USD	1.952	GBP/USD USD/JPY	JPY/GBP
2008-9-30	6.0233	EUR-JPY-SGD-EUR	1.412	JPY/EUR EUR/SGD	SGD/JPY
2008-10-1	6.0228	EUR-GBP-HKD-EUR	1.947	GBP/EUR HKD/GBP	EUR/HKD
2008-10-2	6.0228	EUR-GBP-SGD-EUR	0.403	GBP/EUR SGD/GBP	EUR/SGD
2008-10-3	6.0231	EUR-SGD-GBP-EUR	0.630	SGD/EUR GBP/SGD EUR/GBP	
2008-10-6	6.0231	EUR-SGD-JPY-EUR	2.824	SGD/EUR JPY/SGD EUR/JPY	
2008-10-7	6.024	USD-EUR-JPY-USD	1.026	EUR/USD JPY/EUR	USD/JPY
2008-10-8	6.024	USD-GBP-HKD-USD	1.905	GBP/USD HKD/GBP	USD/HKD
2008-10-9	6.0245	USD-EUR-JPY-USD	1.362	EUR/USD JPY/EUR	USD/JPY
2008-10-10	6.0249	USD-EUR-GBP-USD	0.786	EUR/USD GBP/EUR USD/GBP	
2008-10-13	6.0254	USD-JPY-SGD-USD	2.752	JPY/USD USD/SGD	SGD/JPY
2008-10-14	6.0237	EUR-SGD-GBP-EUR	0.738	SGD/EUR GBP/SGD	EUR/GBP
2008-10-15	6.0241	USD-EUR-JPY-USD	2.292	EUR/USD JPY/EUR	USD/JPY
2008-10-16	6.0246	USD-JPY-EUR-USD	1.768	JPY/USD USD/EUR	EUR/JPY
2008-10-17	6.024	EUR-GBP-HKD-EUR	0.465	GBP/EUR HKD/GBP	EUR/HKD

	$\lambda_{\max}$	Path	Profit(%)	Underpriced	Overpriced
2008-10-20	6.024	EUR-GBP-HKD-EUR	1.968	GBP/EUR HKD/GBP	EUR/HKD
2008-10-21	6.0242	USD-GBP-HKD-USD	2.515	GBP/USD HKD/GBP	USD/HKD
2008-10-22	6.0249	USD-GBP-JPY-USD	2.403	GBP/USD JPY/GBP USD/JPY	
2008-10-23	6.0257	USD-JPY-EUR-USD	0.999	JPY/USD USD/EUR	EUR/JPY
2008-10-24	6.0263	EUR-GBP-JPY-EUR	3.770	GBP/EUR EUR/JPY	JPY/GBP
2008-10-27	6.027	EUR-GBP-HKD-EUR	0.994	GBP/EUR HKD/GBP	EUR/HKD
2008-10-28	6.028	USD-JPY-GBP-USD	5.953	JPY/USD USD/GBP	GBP/JPY
2008-10-29	6.0258	USD-HKD-GBP-USD	1.224	HKD/USD GBP/HKD	USD/GBP
2008-10-30	6.0253	EUR-GBP-HKD-EUR	1.862	GBP/EUR HKD/GBP	EUR/HKD
2008-10-31	6.0255	USD-GBP-SGD-USD	1.181	GBP/USD SGD/GBP	USD/SGD
2008-11-3	6.0256	USD-GBP-HKD-USD	3.802	GBP/USD HKD/GBP USD/HKD	
2008-11-4	6.0255	EUR-HKD-GBP-EUR	2.398	HKD/EUR GBP/HKD EUR/GBP	
2008-11-5	6.0251	USD-EUR-JPY-USD	2.377	EUR/USD JPY/EUR USD/JPY	
2008-11-6	6.0256	USD-GBP-HKD-USD	1.616	GBP/USD HKD/GBP	USD/HKD
2008-11-7	6.0261	USD-EUR-HKD-USD	0.518	EUR/USD HKD/EUR	USD/HKD
2008-11-10	6.0254	USD-EUR-JPY-USD	1.075	EUR/USD JPY/EUR USD/JPY	
2008-11-11	6.026	USD-GBP-HKD-USD	1.442	GBP/USD HKD/GBP	USD/HKD
2008-11-12	6.0265	USD-GBP-JPY-USD	4.065	GBP/USD USD/JPY	JPY/GBP
2008-11-13	6.027	USD-JPY-EUR-USD	3.562	JPY/USD USD/EUR	EUR/JPY
2008-11-14	6.0266	USD-EUR-SGD-USD	0.778	EUR/USD SGD/EUR	USD/SGD
2008-11-17	6.0269	EUR-HKD-GBP-EUR	1.623	HKD/EUR GBP/HKD EUR/GBP	
2008-11-18	6.0268	EUR-SGD-GBP-EUR	0.497	SGD/EUR GBP/SGD	EUR/GBP
2008-11-19	6.0268	USD-EUR-JPY-USD	2.340	EUR/USD JPY/EUR	USD/JPY
2008-11-20	6.0269	USD-EUR-JPY-USD	1.394	EUR/USD JPY/EUR USD/JPY	
2008-11-21	6.0276	USD-JPY-EUR-USD	1.399	JPY/USD USD/EUR	EUR/JPY
2008-11-24	6.0279	USD-JPY-SGD-USD	3.204	JPY/USD USD/SGD	SGD/JPY
2008-11-25	6.0266	USD-HKD-GBP-USD	2.327	HKD/USD GBP/HKD USD/GBP	
2008-11-26	6.0268	EUR-SGD-GBP-EUR	0.522	SGD/EUR GBP/SGD	EUR/GBP
2008-11-27	6.0267	USD-GBP-EUR-USD	0.201	GBP/USD USD/EUR	EUR/GBP
2008-11-28	6.0267	EUR-GBP-HKD-EUR	0.479	GBP/EUR HKD/GBP	EUR/HKD

Table 6 Arbitrage without bid-ask spread

	$\lambda_{\max}$	Path	Profit(%)	maximum bid-ask spread	Underpriced	Overpriced
2008-9-1	6*	EUR-GBP-JPY-EUR	0.948	0.248	GBP/ EUR JPY/GBP EUR/JPY	
2008-9-2	6*	HKD-USD-GBP-HKD	1.294	0.318	USD/HKD GBP/USD HKD/GBP	
2008-9-3	6*	GBP-JPY-USD-GBP	0.952	0.249	USD/JPY GBP/USD	JPY/GBP
2008-9-4	6.0001	GBP-JPY-USD-GBP	2.687	0.544	JPY/GBP USD/JPY GBP/USD	
2008-9-5	6*	JPY-EUR-USD-JPY	1.207	0.301	EUR/JPY USD/EUR	JPY/USD
2008-9-8	6*	GBP-JPY-USD-GBP	1.849	0.417	JPY/GBP USD/JPY GBP/USD	
2008-9-9	6*	JPY-USD-SGD-JPY	1.000	0.259	USD/JPY SGD/USD JPY/SGD	
2008-9-10	6*	GBP-HKD-USD-GBP	0.874	0.233	HKD/GBP USD/HKD GBP/USD	
2008-9-11	6*	JPY-EUR-SGD-JPY	1.368	0.333	SGD/EUR JPY/SGD	EUR/JPY
2008-9-12	6.0001	GBP-USD-JPY-GBP	2.677	0.543	USD/GBP JPY/USD GBP/JPY	
2008-9-15	6.0001	JPY-USD-HKD-JPY	2.631	0.537	USD/JPY HKD/USD	JPY/HKD
2008-9-16	6*	JPY-HKD-USD-JPY	1.266	0.313	HKD/JPY USD/HKD JPY/USD	
2008-9-17	6.0001	JPY-USD-HKD-JPY	1.988	0.440	USD/JPY HKD/USD	JPY/HKD
2008-9-18	6*	JPY-HKD-USD-JPY	0.681	0.189	HKD/JPY USD/HKD	JPY/USD
2008-9-19	6.0001	GBP-USD-JPY-GBP	2.469	0.513	USD/GBP JPY/USD GBP/JPY	
2008-9-22	6*	JPY-USD-HKD-JPY	1.326	0.325	USD/JPY HKD/USD	JPY/HKD
2008-9-23	6*	GBP-HKD-JPY-GBP	1.049	0.270	HKD/GBP GBP/JPY	JPY/HKD
2008-9-24	6*	JPY-HKD-USD-JPY	0.680	0.189	HKD/JPY USD/HKD	JPY/USD
2008-9-25	6*	GBP-HKD-USD-GBP	1.274	0.3150	HKD/GBP USD/HKD GBP/USD	
2008-9-26	6*	HKD-GBP-EUR-HKD	1.522	0.3612	GBP/HKD HKD/EUR	EUR/GBP
2008-9-29	6.0001	GBP-JPY-USD-GBP	4.124	0.724	JPY/GBP USD/JPY GBP/USD	
2008-9-30	6.0001	EUR-JPY-SGD-EUR	2.634	0.537	JPY/EUR SGD/JPY EUR/SGD	
2008-10-1	6.0001	EUR-GBP-HKD-EUR	2.069	0.453	GBP/EUR HKD/GBP EUR/HKD	
2008-10-2	6*	EUR-SGD-JPY-EUR	1.580	0.371	SGD/EUR JPY/SGD EUR/JPY	
2008-10-3	6*	EUR-JPY-GBP-EUR	1.261	0.312	JPY/EUR GBP/JPY EUR/GBP	
2008-10-6	6.0003	EUR-GBP-JPY-EUR	5.059	0.823	GBP/EUR JPY/GBP EUR/JPY	
2008-10-7	6*	EUR-JPY-GBP-EUR	1.801	0.409	JPY/EUR GBP/JPY EUR/GBP	
2008-10-8	6.0001	GBP-JPY-USD-GBP	3.703	0.675	JPY/GBP USD/JPY GBP/USD	
2008-10-9	6*	JPY-USD-EUR-JPY	1.433	0.344	USD/JPY EUR/USD JPY/EUR	
2008-10-10	6*	JPY-HKD-USD-JPY	1.325	0.324	HKD/JPY USD/HKD	JPY/USD
2008-10-13	6.0002	GBP-USD-JPY-GBP	5.185	0.835	USD/GBP JPY/USD GBP/JPY	
2008-10-14	6*	HKD-GBP-EUR-HKD	1.655	0.384	EUR/GBP HKD/EUR	GBP/HKD
2008-10-15	6.0001	JPY-USD-GBP-JPY	3.411	0.640	USD/JPY GBP/USD JPY/GBP	
2008-10-16	6*	JPY-SGD-USD-JPY	1.921	0.429	USD/SGD JPY/USD	SGD/JPY



	$\lambda_{\max}$	Path	Profit(%)	maximum bid-ask spread	Underpriced	Overpriced
2008-10-17	6*	EUR-GBP-JPY-EUR	0.752	0.205	GBP/EUR EUR/JPY	JPY/GBP
2008-10-20	6*	EUR-GBP-HKD-EUR	2.084	0.455	GBP/EUR HKD/GBP EUR/HKD	
2008-10-21	6.0002	GBP-JPY-USD-GBP	4.496	0.764	JPY/GBP USD/JPY GBP/USD	
2008-10-22	6.0002	GBP-JPY-USD-GBP	4.962	0.813	JPY/GBP USD/JPY GBP/USD	
2008-10-23	6*	JPY-EUR-USD-JPY	1.072	0.274	USD/EUR JPY/USD	EUR/JBP
2008-10-24	6.0004	EUR-GBP-JPY-EUR	6.561	0.962	GBP/EUR JPY/GBP EUR/JBP	
2008-10-27	6.0001	EUR-GBP-JPY-EUR	3.520	0.653	GBP/EUR JPY/GBP EUR/JBP	
2008-10-28	6.0006	GBP-USD-JPY-GBP	8.936	1.149	USD/GBP JPY/USD GBP/JPY	
2008-10-29	6*	GBP-SGD-JPY-GBP	1.879	0.422	SGD/GBP JPY/SGD GBP/JPY	
2008-10-30	6.0001	EUR-GBP-JPY-EUR	2.546	0.524	GBP/EUR JPY/GBP EUR/JPY	
2008-10-31	6*	GBP-JPY-USD-GBP	1.351	0.329	USD/JPY GBP/USD	JPY/GBP
2008-11-3	6.0002	HKD-USD-GBP-HKD	3.927	0.701	USD/HKD GBP/USD HKD/GBP	
2008-11-4	6.0001	EUR-HKD-GBP-EUR	2.502	0.518	HKD/EUR GBP/HKD EUR/GBP	
2008-11-5	6.0001	EUR-JPY-USD-EUR	2.456	0.511	JPY/EUR USD/JPY EUR/USD	
2008-11-6	6.0001	GBP-JPY-USD-GBP	2.662	0.541	JPY/GBP USD/JPY GBP/USD	
2008-11-7	6.0001	EUR-JPY-GBP-EUR	2.478	0.515	JPY/EUR EUR/GBP	GBP/JPY
2008-11-10	6.0001	GBP-JPY-USD-GBP	2.632	0.537	JPY/GBP USD/JPY GBP/USD	
2008-11-11	6*	GBP-HKD-USD-GBP	1.508	0.358	HKD/GBP USD/HKD GBP/USD	
2008-11-12	6.0004	GBP-JPY-USD-GBP	6.956	0.996	JPY/GBP USD/JPY GBP/USD	
2008-11-13	6.0001	JPY-EUR-USD-JPY	3.639	0.667	EUR/JPY USD/EUR JPY/USD	
2008-11-14	6*	EUR-SGD-JPY-EUR	0.944	0.248	SGD/EUR JPY/SGD EUR/JPY	
2008-11-17	6.0001	EUR-JPY-GBP-EUR	2.071	0.453	GBP/JPY EUR/GBP	JPY/EUR
2008-11-18	6*	EUR-JPY-GBP-EUR	1.255	0.311	JBP/EUR GBP/JPY EUR/GBP	
2008-11-19	6*	EUR-JPY-USD-EUR	2.419	0.506	JBP/EUR USD/JPY EUR/USD	
2008-11-20	6.0001	GBP-JPY-USD-GBP	3.560	0.658	JBP/GBP USD/JPY GBP/USD	
2008-11-21	6.0001	GBP-USD-JPY-GBP	2.894	0.573	USD/GBP GBP/USD GBP/JPY	
2008-11-24	6.0003	JPY-GBP-USD-JPY	6.117	0.923	GBP/JPY USD/GBP JBP/USD	
2008-11-25	6.0001	GBP-USD-HKD-GBP	2.397	0.503	USD/GBP HKD/USD GBP/HKD	
2008-11-26	6*	EUR-SGD-GBP-EUR	0.598	0.169	SGD/EUR GBP/SGD EUR/GBP	
2008-11-27	6*	EUR-JPY-GBP-EUR	0.710	0.195	JBP/EUR EUR/GBP	GBP/JPY
2008-11-28	6*	EUR-GBP-JPY-EUR	0.665	0.185	GBP/EUR JBP/GBP EUR/JPY	

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