

APPENDIX B
SOLVING EQUATION (2.11)

$$\begin{aligned}
\frac{\partial I_t}{\partial e_t} &= A / K_t \left\{ \frac{MKUP_t \frac{dp_t x_t}{de_t} - p_t x_t \frac{dMKUP_t}{de_t}}{MKUP_t^2} + \frac{MKUP_t^* \frac{de_t p_t^* x_t^*}{de_t} - e_t p_t^* x_t^* \frac{dMKUP_t^*}{de_t}}{MKUP_t^{*2}} \right\} \\
&\quad - e_t L_t^* \frac{dw_t^*}{de_t} - w_t^* L_t^* \frac{de_t}{de_t} \\
\frac{\partial I_t}{\partial e_t} &= A / K_t \left\{ \frac{MKUP_t x_t \frac{dp_t}{de_t} \frac{e_t}{p_t} \frac{p_t}{e_t} - p_t x_t \frac{dMKUP_t}{de_t} \frac{e_t}{MKUP_t} \frac{MKUP_t}{e_t}}{MKUP_t^2} \right. \\
&\quad \left. + \frac{MKUP_t^* \left[e_t x_t^* \frac{dp_t^*}{de_t} \frac{e_t}{p_t^*} \frac{p_t^*}{e_t} + p_t^* x_t^* \right] - e_t p_t^* x_t^* \frac{dMKUP_t^*}{de_t} \frac{e_t}{MKUP_t^*} \frac{MKUP_t^*}{e_t}}{MKUP_t^{*2}} \right\} \\
&\quad - e_t L_t^* \frac{dw_t^*}{de_t} \frac{e_t}{w_t^*} \frac{w_t^*}{e_t} - w_t^* L_t^* \frac{de_t}{de_t} \\
\frac{\partial I_t}{\partial e_t} &= A / K_t \left\{ \frac{p_t x_t (\varepsilon_{p,e} - \varepsilon_{MKUP,e})}{e_t MKUP_t} + \frac{e_t p_t^* x_t^* (\varepsilon_{p^*,e} + 1 - \varepsilon_{MKUP^*,e})}{e_t MKUP_t^*} - \frac{e_t w_t^* L_t^* (1 + \varepsilon_{w^*,e})}{e_t} \right\} \\
\frac{\partial I_t}{\partial e_t} &= A \cdot TR_t / K_t \left\{ \frac{p_t x_t (\varepsilon_{p,e} - \varepsilon_{MKUP,e})}{TR_t MKUP_t} + \frac{e_t p_t^* x_t^* (\varepsilon_{p^*,e} + 1 - \varepsilon_{MKUP^*,e})}{TR_t MKUP_t^*} - \frac{e_t w_t^* L_t^* (1 + \varepsilon_{w^*,e}) TC_t}{TR_t TC_t} \right\} \frac{1}{e_t} \\
\frac{\partial I_t}{\partial e_t} &= A \cdot TR_t / K_t \left\{ \frac{(1 - X_t) (\varepsilon_{p,e} - \varepsilon_{MKUP,e})}{MKUP_t} + \frac{X_t (\varepsilon_{p^*,e} + 1 - \varepsilon_{MKUP^*,e})}{MKUP_t^*} - \frac{\alpha_t (1 + \varepsilon_{w^*,e}) TC_t}{TR_t} \right\} \frac{1}{e_t} \\
\frac{\partial I_t}{\partial e_t} &= A \cdot TR_t / K_t \left\{ \frac{(1 - X_t) (\varepsilon_{p,e} - \varepsilon_{MKUP,e})}{MKUP_t} + \frac{X_t (\varepsilon_{p^*,e} + 1 - \varepsilon_{MKUP^*,e})}{MKUP_t^*} - \frac{\alpha_t (1 + \varepsilon_{w^*,e})}{MKUP_t} \right\} \frac{1}{e_t} \\
\frac{\partial I_t}{\partial e_t} &= \frac{A'}{AMKUP} \left\{ (1 - X_t) (\varepsilon_{p,e} - \varepsilon_{MKUP,e}) + X_t (\varepsilon_{p^*,e} + 1 - \varepsilon_{MKUP^*,e}) - \alpha_t (1 + \varepsilon_{w^*,e}) \right\} \frac{1}{e_t}
\end{aligned}$$

Note that:

$$\text{profit gross of investment costs: } \Pi_t = p_t x_t + e_t p_t^* x_t^* - w_t L_t - e_t w_t^* L_t^*$$

F.O.C. of profit-max problem:

$$\frac{\partial \Pi_t}{\partial K_t} = (1 + \eta_t^{-1}) p(x_t, e_t) \frac{\partial f}{\partial K} = 0$$

$$\text{since } \frac{\partial f}{\partial K_t} = \frac{\frac{\Pi_t}{K_t} - \left(\frac{p_t x_t + e_t p_t^* x_t^*}{K_t} \right) + [p(x_t, e_t)(1 + \eta_t^{-1})] \left[\frac{x_t + x_t^*}{K_t} \right]}{[p(x_t, e_t)(1 + \eta_t^{-1})]}$$

$$\begin{aligned} \frac{\partial \Pi_t}{\partial K_t} &= \frac{\Pi_t}{K_t} - \left(\frac{p_t x_t + e_t p_t^* x_t^*}{K_t} \right) + [p(x_t, e_t)(1 + \eta_t^{-1})] \left[\frac{x_t + x_t^*}{K_t} \right] = 0 \\ &\quad - w_t L_t - e_t w_t^* L_t^* + [p(x_t, e_t)(1 + \eta_t^{-1})] (x_t + x_t^*) = 0 \\ &\quad [p(x_t, e_t)(1 + \eta_t^{-1})] (x_t + x_t^*) = w_t L_t + e_t w_t^* L_t^* \quad (B.1) \end{aligned}$$

$$\frac{TR_t}{TC_t} = \frac{p_t x_t + e_t p_t^* x_t^*}{w_t L_t + e_t w_t^* L_t^*} \quad (B.2)$$

$$\frac{TR_t}{TC_t} = \frac{p_t (x_t + x_t^*)}{w_t L_t + e_t w_t^* L_t^*} \quad (B.3) \quad \text{according to Law of one price}$$

$$\frac{TR_t}{TC_t} = \frac{p_t (x_t + x_t^*)}{[p(1 + \eta_t^{-1})] (x_t + x_t^*)} \quad (B.4)$$

$$\frac{TR_t}{TC_t} = \frac{1}{1 + \eta_t^{-1}} = MKUP_t \quad (B.5)$$