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#### LIST OF SYMBOLS

#### **SYMBOL**

C

Ε evaporation Ν number of grid points time integration of the numerical scheme М gas constant R  $\vec{R}$ radiation vector S latent heating temperature Т  $\vec{V}$ velocity drag force of the earth  $F_d$  $R_d$ dry air gas constant  $S_q$ phase-change source acceleration due to gravity g diffusion coefficients k pressure р specific humidity qW weight heat capacity at constant pressure  $C_p$ 

conductive heating

- $d_t$  distance between the trajectories at the time
- $\hat{x}_i$  forecast value
- $x_i$  observed value
- $\rho$  density
- $\delta$  deviation from the trajectory
- $\lambda$  Lyapunov exponent
- $\phi$  geopotential height
- $\Omega$  rotation of the earth
- $\alpha_i$  rescaling parameter

## LIST OF TECHNICAL TERMS AND ABBREVIATIONS

CTRL	Control Run
EdGCM	Educational Global Climate Model
FSLE	Finite Size Lyapunov Exponent
FTLE	Finite Time Lyapunov Exponent
GCM	Global Climate Model
GISS GCM Model II	Goddard Institute for Space Studies General Circulation Model II
GHG	Greenhouse Gas
IPCC	Intergovernmental Panel on Climate Change
LE	Lyapunov Exponents
LLE	Local Lyapunov Exponent
MLE	Maximum Lyapunov Exponent
MoLE	Modified Lyapunov Exponent
NASA/GISS	NASA's Goddard Institute for Space Studies
NWP	Numerical Weather Prediction
PER	Perturbed Run
RMSE	Root Mean Square Error
SLE	Supremum Lyapunov Exponent
med	Median