

An Experimental Study of Segmented Two-Phase Flow and Heat Transfer  
Characteristics in a Microchannel

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### Abstract

Cooling systems are needed for the electronic devices in order to operate efficiently. Because the size of the equipment is decreased to the micro scale, research on the heat transfer characteristics in a microchannel heat sink is needed. In this work, the nonboiling of segmented air-water flow was proposed to be an alternative method for heat transfer enhancement in a microchannel heat sink compared to using single-phase water cooling. The experiment was conducted with two-phase air-water flow in a single rectangular microchannel with a hydraulic diameter of 267  $\mu\text{m}$ . The test section was made of copper. For a clear understanding, a two-phase flow pattern, a pressure drop, and heat transfer characteristics in the low Reynolds number of air-water flow were identified. The results show that segmented, throat-annular, throat-annular/liquid, and annular flow were observed in the test section. A flow pattern map was created and compared with the previous maps. The pressure drop can be predicted by the homogeneous flow model and the Friedel correlation separated flow model. In the heat transfer characteristics, the results demonstrated that the Nusselt number of segmented flow increases up to 1.2 times over the single-phase flow.

**Keywords:** Microchannel/Segmented flow/Flow pattern/Nusselt number/Pressure drop

หัวข้อวิทยานิพนธ์	การศึกษาเชิงทดลองของลักษณะการไหลสองเฟสแบบเชกเมนต์และการถ่ายเทความร้อนในอุปกรณ์ระบายความร้อนที่มีช่องทางการไหลขนาดเล็กมาก
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### บทคัดย่อ

การถ่ายเทความร้อนให้แก่อุปกรณ์อิเล็กทรอนิกส์เป็นสิ่งจำเป็นเพื่อให้อุปกรณ์สามารถทำงานได้เต็มประสิทธิภาพ แต่ปัจจุบันอุปกรณ์อิเล็กทรอนิกส์มีขนาดลดลงอย่างต่อเนื่อง งานวิจัยจึงควรให้ความสำคัญต่อการศึกษาและทำความเข้าใจเกี่ยวกับการถ่ายเทความร้อนให้แก่อุปกรณ์ขนาดเล็กเพื่อให้ได้มาซึ่งวิธีที่เหมาะสม งานวิจัยนี้ได้ทำการทดลองเกี่ยวกับการไหลสองเฟสในช่องทางการไหลขนาดเล็กมากโดยหน้าตัดของช่องทางการไหลเป็นสี่เหลี่ยมที่ทำจากทองแดง มีเส้นผ่าศูนย์กลางไฮดรอลิกส์ขนาด 267 ไมโครเมตร รูปแบบการไหล ความดันลด และการถ่ายเทความร้อนจะเกิดในช่วงที่มีค่าเรย์โนลด์ส์ต่ำที่ใช้น้ำและอากาศเป็นสารทำงานให้แก่ระบบ จากผลการทดลองพบว่า รูปแบบการไหลที่เกิดขึ้นคือ segmented, throat-annular, throat-annular/liquid และ annular มีแผนที่รูปแบบการไหลที่มีลักษณะเฉพาะตัว และสามารถทำนายความดันลดได้ทั้งการใช้โมเดลความดันลดแบบ รูปแบบการไหลแบบเนื้อเดียว และรูปแบบการไหลแบบแยกส่วน และสำหรับลักษณะการถ่ายเทความร้อนจากการทดลองพบว่า การไหลสองเฟสแบบเชกเมนต์สามารถเพิ่มความสามารถในการถ่ายเทความร้อนให้กับช่องทางการไหลได้เพิ่มขึ้นสูงถึง 1.2 เท่าเมื่อเปรียบเทียบกับการไหลเฟสเดียวของน้ำ

คำสำคัญ : ช่องทางการไหลขนาดเล็กมาก/การไหลแบบเชกเมนต์/รูปแบบการไหล/ค่านัสเซิลต์  
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## LIST OF SYMBOLS

$A_{ch}$	surface area of the test section, m <sup>2</sup>
$AR$	aspect ratio of channel
$C$	coefficient $C$ value
$C_c$	coefficient of contraction
$C_p$	specific heat (J/kgK)
$D_h$	hydraulic diameter of channel, m
$Fr_H$	the dimensionless factor
$f$	friction factor
$G$	mass flux, kg/m <sup>2</sup> s
$g$	gravitational acceleration, m/s <sup>2</sup>
$H$	channel height, m
$h$	heat transfer coefficient (W/m <sup>2</sup> K)
$k$	thermal conductivity (W/mK)
$L$	channel length, m
$Nu$	Nusselt number
$P$	pressure, Pa
$Q_{bulk}$	heat transfer, W
$q''$	heat flux, W/m <sup>2</sup>
$Re$	Reynolds number
$T$	Temperature, °C, K
$U$	superficial velocity, m/s

$V$	volume flow rate, m <sup>3</sup> /s
$W$	channel width, m
$We$	Weber number
$X_{vv}$	Martinelli parameter for laminar-laminar flow
$x$	quality

### **Greek symbols**

$\beta$	gas volumetric ratio
$\rho$	density, kg/m <sup>3</sup>
$\alpha$	void fraction
$\mu$	dynamic viscosity, kg/m s
$\rho$	density, kg/m <sup>3</sup>
$\gamma$	ratio of the cross-sectional flow area in the flow passage connected to the channel test section to that in the channel test section
$\phi$	two-phase frictional multiplier
$\Delta P$	pressure drop, kPa/m

### **Subscripts**

$ch$	channel
$c/e$	contraction/expansion
exp	experimental value
$f$	fluid
$G$	gas
$GS$	gas superficial velocity
$H$	homogeneous flow
$L$	liquid
$LS$	liquid superficial velocity

*pred* predicted value

*s* surface

*TP* two-phase

## **APPENDICES**

## APPENDIX A. THE EXAMPLES OF UNCERTAINTY CALCULATIONS

### 1. The uncertainty of the superficial velocity of gas ( $\delta U_{GS}$ )

$$\delta U_{GS} = \sqrt{\left(\frac{\partial U_{GS}}{\partial \dot{m}_G} \delta \dot{m}_G\right)^2 + \left(\frac{\partial U_{GS}}{\partial A} \delta A\right)^2}$$

$$U_{GS} = \frac{\dot{m}_G}{\rho_G A} = \frac{(9.667 \times 10^{-8}) \frac{kg}{s}}{(1.1302) \frac{kg}{m^3} \times (8 \times 10^{-8}) m^2} = 1.0692 m/s$$

$$\dot{m}_G = \rho_G V_G = (1.1302) \frac{kg}{m^3} (8.333 \times 10^{-8}) \frac{m^3}{s} = 9.418 \times 10^{-8} \frac{kg}{s}$$

$$A = WL$$

$$\frac{\partial A}{\partial L} = W$$

$$\frac{\partial A}{\partial W} = L$$

$$\delta A = \sqrt{\left(\frac{\partial A}{\partial W} \delta W\right)^2 + \left(\frac{\partial A}{\partial L} \delta L\right)^2}$$

$$\delta A = \sqrt{\left((0.0002 mm)(10^{-5} mm)\right)^2 + \left((0.0004 mm)(2 \times 10^{-5} mm)\right)^2}$$

$$\delta A = \pm 8.246 \times 10^{-9} m^2$$

$$\frac{\delta A}{A} \times 100 = \frac{\pm 8.246 \times 10^{-9}}{8 \times 10^{-8}} \times 100 = 10.3\%$$

$$\delta \dot{m}_G = (9.667 \times 10^{-8}) \frac{kg}{s} (0.08) = 7.733 \times 10^{-9} \frac{kg}{s}$$

$$\frac{\partial U_{GS}}{\partial \dot{m}_G} = \frac{1}{\rho_G A} = \frac{1}{1.1302 \frac{kg}{m^3} (0.0002 \times 0.0004 m^2)} = 11059989 \frac{m}{kg}$$

$$\frac{\partial U_{GS}}{\partial A} = \frac{\dot{m}_G}{\rho_G A^2} = \frac{9.667 \times 10^{-8} \frac{kg}{s}}{1.1302 \frac{kg}{m^3} (0.0002 \times 0.0004)^2 m^4} = 13364614 s^{-1} m^{-1}$$

so

$$\delta U_{GS} = \sqrt{\left(11059989 \frac{m}{kg} (7.733 \times 10^{-9}) \frac{kg}{s}\right)^2 + \left(13364614 s^{-1} m^{-1} (8.246 \times 10^{-9}) m^2\right)^2}$$

$$\delta U_{GS} = \pm 0.1368 m/s$$

$$\frac{\delta U_{GS}}{U_{GS}} \times 100 = \frac{\pm 0.1368}{1.06913} \times 100 = 12.8\%$$

## 2. The uncertainty of the superficial velocity of liquid ( $\delta U_{LS}$ )

$$\delta U_{LS} = \sqrt{\left( \frac{\partial U_{LS}}{\partial \dot{m}_L} \delta \dot{m}_L \right)^2 + \left( \frac{\partial U_{LS}}{\partial A} \delta A \right)^2}$$

$$U_{LS} = \frac{\dot{m}_L}{\rho_L A} = \frac{(2.082 \times 10^{-6}) \frac{kg}{s}}{(992.08) \frac{kg}{m^3} \times (8 \times 10^{-8}) m^2} = 0.0262 m/s$$

$$\dot{m}_L = \rho_L V_L = (992.08) \frac{kg}{m^3} (2.082 \times 10^{-9}) \frac{m^3}{s} = 2.066 \times 10^{-6} \frac{kg}{s}$$

$$\delta \dot{m}_L = 2.082 \times 10^{-6} \frac{kg}{s} (0.001) = 2.082 \times 10^{-9} \frac{kg}{s}$$

$$\delta A = \pm 8.246 \times 10^{-9} m^2$$

$$\frac{\partial U_{LS}}{\partial \dot{m}_L} = \frac{1}{\rho_L A} = \frac{1}{992.08 \frac{kg}{m^3} (0.0002 \times 0.0004 m^2)} = 12599 \frac{m}{kg}$$

$$\frac{\partial U_{LS}}{\partial A} = \frac{\dot{m}_L}{\rho_L A^2} = \frac{2.082 \times 10^{-6} \frac{kg}{s}}{992.08 \frac{kg}{m^3} (0.0002 \times 0.0004)^2 m^4} = 327909.54 s^{-1} m^{-1}$$

so

$$\delta U_{LS} = \sqrt{\left( 12599 \frac{m}{kg} (2.082 \times 10^{-9}) \frac{kg}{s} \right)^2 + \left( (327909.54) s^{-1} m^{-1} (8.246 \times 10^{-9}) m^2 \right)^2}$$

$$\delta U_{LS} = \pm 2.704 \times 10^{-3} m/s$$

$$\frac{\delta U_{LS}}{U_{LS}} \times 100 = \frac{\pm 2.704 \times 10^{-3}}{2.745 \times 10^{-2}} \times 100 = 9.85\%$$

### 3. The uncertainty of frictional pressure drop $\left( \delta \left( \frac{dP}{dz} \right)_{friction} \right)$

$$\begin{aligned} \left( \frac{dP}{dz} \right)_{friction} &= \left( \frac{dP}{dz} \right)_{Total} - \left( \frac{dP}{dz} \right)_{acceleration} - \left( \frac{dP}{dz} \right)_{c/e} \\ \left( \frac{dP}{dz} \right)_{Total} &= 368750 \frac{Pa}{m} \\ \left( \frac{dP}{dz} \right)_{Acceleration} &= G^2 \left[ \left( \frac{x^2}{\rho_G \alpha} + \frac{(1-x)^2}{(1-\alpha)\rho_L} \right)_{outlet} - \left( \frac{x^2}{\rho_G \alpha} + \frac{(1-x)^2}{(1-\alpha)\rho_L} \right)_{inlet} \right] \\ \left( \frac{dP}{dz} \right)_{Acceleration} &= \frac{(27.23)^2}{0.05} \left[ \left( \frac{0.0444^2}{(1.0957)(0.976)} + \frac{(1-0.0444)^2}{(1-0.976)998.09} \right) - \left( \frac{0.0444^2}{1.167(0.976)} + \frac{(1-0.0444)^2}{(1-0.976)988.09} \right) \right] \\ &= 5.8439 \frac{Pa}{m} \end{aligned}$$

$$\left( \frac{dP}{dz} \right)_{friction} = 362561 \frac{Pa}{m}$$

$$\delta \left( \frac{dP}{dz} \right)_{friction} = \sqrt{\left( \delta \left( \frac{dP}{dz} \right)_{Total} \right)^2 + \left( \delta \left( \frac{dP}{dz} \right)_{acceleration} \right)^2}$$

$$\delta \left( \frac{dP}{dz} \right)_{Total} = \pm 737.5 \frac{Pa}{m}$$

$$\delta \left( \frac{dP}{dz} \right)_{acceleration} = \sqrt{\left( \frac{\partial \left( \frac{dP}{dz} \right)_{acceleration}}{\partial x} \delta x \right)^2 + \left( \frac{\partial \left( \frac{dP}{dz} \right)_{acceleration}}{\partial \alpha} \delta \alpha \right)^2}$$

$$x = \frac{G_g}{G}$$

$$\frac{\partial x}{\partial G} = \frac{G_g}{G^2} = \frac{1.21}{27.23^2} = 1.632 \times 10^{-3}$$

$$\frac{\partial x}{\partial G_g} = \frac{1}{G^1} = \frac{1}{27.23} = 3.672 \times 10^{-2}$$

$$\delta x = \sqrt{\left( \frac{\partial x}{\partial G} \delta G \right)^2 + \left( \frac{\partial x}{\partial G_g} \delta G_g \right)^2}$$

The uncertainty of two-phase mass flux ( $\delta G$ )

$$G_g = \frac{\dot{m}_G}{A}$$

$$\delta G_g = \sqrt{\left(\frac{\partial G_g}{\partial \dot{m}_G} \delta \dot{m}_G\right)^2 + \left(\frac{\partial G_g}{\partial A} \delta A\right)^2}$$

$$\frac{\partial G_g}{\partial \dot{m}_G} = \frac{1}{A} = \frac{1}{(8 \times 10^{-8})} = 1.25 \times 10^7 \text{ m}^{-1}$$

$$\frac{\partial G_g}{\partial A} = \frac{\dot{m}_g}{A^2} = \frac{9.67 \times 10^{-8}}{(8 \times 10^{-8})^2} = 1.51 \times 10^7 \frac{\text{kg}}{\text{sm}^4}$$

$$\delta G_g = \sqrt{\left(\left(1.25 \times 10^7 \text{ m}^{-1}\right)\left(7.733 \times 10^{-9} \frac{\text{kg}}{\text{s}}\right)\right)^2 + \left(\left(1.51 \times 10^7 \frac{\text{kg}}{\text{sm}^4}\right)\left(8.246 \times 10^{-9} \text{m}^2\right)\right)^2} = 0.1576 \frac{\text{kg}}{\text{m}^2 \text{s}}$$

$$G = \frac{\dot{m}_L + \dot{m}_G}{A}$$

$$\delta G = \sqrt{\left(\frac{\partial G}{\partial \dot{m}_L} \delta \dot{m}_L\right)^2 + \left(\frac{\partial G}{\partial \dot{m}_G} \delta \dot{m}_G\right)^2 + \left(\frac{\partial G}{\partial A} \delta A\right)^2}$$

$$\frac{\partial G}{\partial \dot{m}_L} = \left(\frac{\dot{m}_L + \dot{m}_G}{A}\right) \frac{1}{\dot{m}_L} = \left(\frac{\left(\left(2.08 \times 10^{-6}\right) + \left(9.667 \times 10^{-8}\right)\right)}{8 \times 10^{-8}}\right) \frac{1}{\left(2.08 \times 10^{-6}\right)} = 13080949.5 \text{ m}^2$$

$$\frac{\partial G}{\partial \dot{m}_G} = \left(\frac{\dot{m}_L + \dot{m}_G}{A}\right) \frac{1}{\dot{m}_G} = \left(\frac{\left(\left(2.08 \times 10^{-6}\right) + \left(9.667 \times 10^{-8}\right)\right)}{8 \times 10^{-8}}\right) \frac{1}{\left(9.667 \times 10^{-8}\right)} = 281456242.9 \text{ m}^2$$

$$\frac{\partial G}{\partial A} = \left(\frac{\dot{m}_L + \dot{m}_G}{A^2}\right) = \left(\frac{\left(\left(2.08 \times 10^{-6}\right) + \left(9.667 \times 10^{-8}\right)\right)}{\left(8 \times 10^{-8}\right)^2}\right) = 340104687.5 \frac{\text{kg}}{\text{m}^4 \text{s}}$$

$$\delta G = \sqrt{\left(\left(13080949.5 \text{ m}^2\right)\left(2.082 \times 10^{-9} \frac{\text{kg}}{\text{s}}\right)\right)^2 + \left(\left(281456242.9 \text{ m}^2\right)\left(7.733 \times 10^{-9} \frac{\text{kg}}{\text{s}}\right)\right)^2 + \left(\left(340104687.5 \frac{\text{kg}}{\text{m}^4 \text{s}}\right)\left(8.246 \times 10^{-9} \text{m}^2\right)\right)^2}$$

$$\delta G = \pm 3.5499 \frac{\text{kg}}{\text{ms}}$$

$$\frac{\delta G}{G} \times 100 = \frac{\pm 3.5499}{27.3} \times 100 = 13\%$$

The uncertainty of gas quality ( $\delta x$ )

$$\delta x = \sqrt{\left(\frac{\partial x}{\partial G} \delta G\right)^2 + \left(\frac{\partial x}{\partial G_g} \delta G_g\right)^2}$$

$$\delta x = \sqrt{\left((1.632 \times 10^{-3})(3.5499)\right)^2 + \left((3.672 \times 10^{-2})(0.1576)\right)^2} = \pm 8.189 \times 10^{-3}$$

The uncertainty of void fraction ( $\delta\alpha$ )

$$\alpha = \frac{1}{1 + \frac{(1-x)}{x} \left(\frac{\rho_G}{\rho_L}\right)^{\frac{2}{3}}} = 0.9760$$

$$\frac{\partial \alpha}{\partial x} = \left( \frac{1}{1 + \frac{(1-x)}{x} \left(\frac{\rho_G}{\rho_L}\right)^{\frac{2}{3}}} \right) \frac{1}{x} = \left( \frac{1}{1 + \frac{(1-0.0444)}{0.0444} \left(\frac{1.167}{995}\right)^{\frac{2}{3}}} \right) \frac{1}{0.0444} = 18.17$$

$$\delta \alpha = \sqrt{\left(\frac{\partial \alpha}{\partial x} \delta x\right)^2} = \sqrt{\left((18.17)(\pm 8.189 \times 10^{-3})\right)^2} = \pm 0.1488$$

$$\frac{\delta \alpha}{\alpha} \times 100 = \frac{\pm 0.14879}{0.976} \times 100 = 15.24\%$$

The uncertainty of accelerational pressure drop

$$\delta \left( \frac{dP}{dz} \right)_{acceleration} = \sqrt{\left( \frac{\partial \left( \frac{dP}{dz} \right)_{acceleration}}{\partial x} \delta x \right)^2 + \left( \frac{\partial \left( \frac{dP}{dz} \right)_{acceleration}}{\partial \alpha} \delta \alpha \right)^2}$$

$$\frac{\partial \left( \frac{dP}{dz} \right)_{acceleration}}{\partial x} = \frac{G^2}{L} \left( \frac{-2+2x}{\rho_L(1-\alpha)} + \frac{2x}{\rho_G \alpha} \right) = \frac{27.24^2}{0.05} \left( \frac{-2+2(0.0444)}{995(1-0.976)} + \frac{2(0.0444)}{1.167(0.976)} \right) = -30.71$$

$$\frac{\partial \left( \frac{dP}{dz} \right)_{acceleration}}{\partial \alpha} = \frac{G^2}{L} \left( \frac{(1-x)^2}{\rho_L(1-\alpha)} - \frac{x^2}{\rho_G \alpha^2} \right) = \frac{27.24^2}{0.05} \left( \frac{(1-0.0444)^2}{995(1-0.976)} - \frac{0.0444^2}{1.167(0.976)} \right) = 541.8$$

$$\delta \left( \frac{dP}{dz} \right)_{acceleration} = \sqrt{\left((-30.71)(\pm 8.189 \times 10^{-3})\right)^2 + \left((541.8)(\pm 0.1488)\right)^2} = \pm 80.62$$

#### 4. The uncertainty of the friction factor ( $\delta f$ )

The uncertainty of two-phase Reynolds number

$$\text{Re}_{TP} = \frac{GD_h}{\mu_{TP}}$$

$$\frac{\partial \text{Re}_{TP}}{\partial G} = \frac{D_h}{\mu_{TP}} = \frac{0.0002667}{0.00059801} = 0.446$$

$$\frac{\partial \text{Re}_{TP}}{\partial D_h} = \frac{G}{\mu_{TP}} = \frac{27.23}{0.00059801} = 45534.3$$

$$\delta \text{Re}_{TP} = \sqrt{\left(\frac{\partial \text{Re}_{TP}}{\partial G} \delta G\right)^2 + \left(\frac{\partial \text{Re}_{TP}}{\partial D_h} \delta D_h\right)^2}$$

The uncertainty of two-phase mass flux

$$\delta G = \pm 3.5499 \frac{\text{kg}}{\text{ms}}$$

$$\frac{\delta G}{G} \times 100 = \frac{\pm 3.5499}{27.3} \times 100 = 13\%$$

so the uncertainty of two-phase Reynolds number is

$$\delta \text{Re}_{TP} = \sqrt{\left((0.446)(3.5499)\right)^2 + \left((45534.3)(8.246 \times 10^{-9})\right)^2} = 1.583$$

$$\frac{\delta \text{Re}_{TP}}{\text{Re}_{TP}} \times 100 = \frac{\pm 1.583}{11.3845} \times 100 = 13.9\%$$

The uncertainty of the friction factor

$$\delta f = \sqrt{\left(\frac{\partial f}{\partial \left(\frac{dP}{dz}\right)_{friction}} \delta \left(\frac{dP}{dz}\right)_{friction}\right)^2 + \left(\frac{\partial f}{\partial \text{Re}_{TP}} \delta \text{Re}_{TP}\right)^2}$$

$$f = \left(\frac{dP}{dz}\right)_{frictional} \frac{\rho_L D_h^3}{2 \text{Re}_{TP}^2 \mu_L^2} = 0.6842$$

$$\frac{\partial f}{\partial \left(\frac{dP}{dz}\right)_{friction}} = \frac{\rho_L D_h^3}{2 \text{Re}_{TP}^2 \mu_L^2} = \frac{(983.18)(0.0002667)^3}{2(11.3845)^2 (0.00064434)^2} = 1.733 \times 10^{-4}$$

$$\frac{\partial f}{\partial \text{Re}_{TP}} = -\left(\frac{dP}{dz}\right)_{friction} \frac{\rho_L D_h^3}{\text{Re}_{TP}^3 \mu_L^2} = -\left(\frac{18128}{0.05}\right) \frac{(983.18)(0.0002667)^3}{(11.3845)^3 (0.00064434)^2} = 11.038$$

$$\delta f = \sqrt{\left( (1.733 \times 10^{-4}) \delta \left( \frac{dP}{dz} \right)_{friction} \right)^2 + ((11.038)(1.583))^2}$$

## 5. The uncertainty of the Nusselt number ( $\delta Nu$ )

The uncertainty of the heat transfer at the test section

$$\delta Q_{bulk} = \sqrt{\left( \frac{\partial Q_{bulk}}{\partial \dot{m}} \cdot \delta \dot{m} \right)^2 + \left( \frac{\partial Q_{bulk}}{\partial T_{fluid,in}} \cdot \delta T_{fluid,in} \right)^2 + \left( \frac{\partial Q_{bulk}}{\partial T_{fluid,out}} \cdot \delta T_{fluid,out} \right)^2}$$

$$Q_{bulk} = \dot{m} C_p (T_{fluid,out} - T_{fluid,in})$$

$$Q_{bulk} = (2.179 \times 10^{-6}) \frac{kg}{s} (3931.6) \frac{J}{kg \cdot ^\circ C} (49.0861 - 29.4495) ^\circ C = 0.1682W$$

$$\frac{\partial Q_{bulk}}{\partial \dot{m}} = C_p (T_{fluid,out} - T_{fluid,in}) = (3931.6) \frac{J}{kg \cdot ^\circ C} (49.0861 - 29.4495) ^\circ C = 77.2 \frac{kJ}{kg}$$

$$\dot{m} = \dot{m}_G + \dot{m}_L$$

$$\frac{\partial \dot{m}}{\partial \dot{m}_G} = (\dot{m}_G + \dot{m}_L) \dot{m}_G = \left( (9.667 \times 10^{-8}) \frac{kg}{s} + (2.0822 \times 10^{-6}) \frac{kg}{s} \right) (9.667 \times 10^{-8}) \frac{kg}{s}$$

$$\frac{\partial \dot{m}}{\partial \dot{m}_G} = 22.11 \times 10^{-13} \frac{kg}{s}$$

$$\delta \dot{m}_G = 9.667 \times 10^{-6} \frac{kg}{s} (0.08) = 7.734 \times 10^{-7} \frac{kg}{s}$$

$$\frac{\partial \dot{m}}{\partial \dot{m}_L} = (\dot{m}_G + \dot{m}_L) \dot{m}_L = \left( (9.667 \times 10^{-8}) \frac{kg}{s} + (2.0822 \times 10^{-6}) \frac{kg}{s} \right) (2.0822 \times 10^{-6}) \frac{kg}{s}$$

$$\frac{\partial \dot{m}}{\partial \dot{m}_L} = 4.537 \times 10^{-12} \frac{kg}{s}$$

$$\delta \dot{m}_L = 2.082 \times 10^{-6} \frac{kg}{s} (0.001) = 2.082 \times 10^{-9} \frac{kg}{s}$$

$$\delta \dot{m} = \sqrt{\left( \frac{\partial \dot{m}}{\partial \dot{m}_G} \cdot \delta \dot{m}_G \right)^2 + \left( \frac{\partial \dot{m}}{\partial \dot{m}_L} \cdot \delta \dot{m}_L \right)^2}$$

$$\delta \dot{m} = \sqrt{\left( 22.11 \times 10^{-13} \frac{kg}{s} \cdot 7.734 \times 10^{-7} \frac{kg}{s} \right)^2 + \left( 4.537 \times 10^{-12} \frac{kg}{s} \cdot 2.082 \times 10^{-9} \frac{kg}{s} \right)^2}$$

$$\delta \dot{m} = \pm 1.71 \times 10^{-18} \frac{kg}{s}$$

$$\frac{\partial Q_{bulk}}{\partial T_{fluid,in}} = \dot{m} C_p = (2.1788 \times 10^{-6} \text{ kg})(3931.6 \frac{\text{J}}{\text{kg}^\circ\text{C}}) = 8.5661 \times 10^{-6} \frac{\text{kJ}}{\text{s}^\circ\text{C}}$$

$$\frac{\partial Q_{bulk}}{\partial T_{fluid,out}} = -\dot{m} C_p = -(2.1788 \times 10^{-6} \text{ kg})(3931.6 \frac{\text{J}}{\text{kg}^\circ\text{C}}) = -8.5661 \times 10^{-6} \frac{\text{kJ}}{\text{s}^\circ\text{C}}$$

so

$$\delta Q_{bulk} = \sqrt{\left(77.2 \frac{\text{kJ}}{\text{kg}} 1.71 \times 10^{-18} \frac{\text{kg}}{\text{s}}\right)^2 + \left(8.5661 \times 10^{-6} \frac{\text{kJ}}{\text{s}^\circ\text{C}} 0.5^\circ\text{C}\right)^2 + \left(-8.5661 \times 10^{-6} \frac{\text{kJ}}{\text{s}^\circ\text{C}} 0.5^\circ\text{C}\right)^2}$$

$$\delta Q_{bulk} = \pm 6.057 \times 10^{-6} \frac{\text{kJ}}{\text{s}} = \pm 6.057 \times 10^{-6} \text{ kW}$$

$$\frac{\delta Q_{bulk}}{Q} \times 100 = \frac{\pm 6.057 \times 10^{-6}}{0.0001682} \times 100 = 3.6\%$$

The uncertainty of the heat flux ( $\delta q''$ )

$$\delta q'' = \sqrt{\left(\frac{\partial q''}{\partial Q_{bulk}} \cdot \delta Q_{bulk}\right)^2 + \left(\frac{\partial q''}{\partial L} \cdot \delta L\right)^2 + \left(\frac{\partial q''}{\partial H} \cdot \delta H\right)^2 + \left(\frac{\partial q''}{\partial W} \cdot \delta W\right)^2}$$

$$q'' = \frac{Q_{bulk}}{A_b} = \frac{Q_{bulk}}{(2H+W)L} = \frac{0.1682\text{W}}{((2 \times 0.0002\text{m}) + 0.0004\text{m})(0.05\text{m})} = 4.205 \frac{\text{kW}}{\text{m}^2}$$

$$\frac{\partial q''}{\partial Q_{bulk}} = \frac{1}{(2H+W)L} = \frac{1}{((2 \times 0.0002\text{m}) + 0.0004\text{m})(0.05\text{m})} = 25000 \text{m}^{-2}$$

$$\frac{\partial q''}{\partial L} = \frac{Q_{bulk}}{(2H+W)L^2} = \frac{0.1682\text{W}}{((2 \times 0.0002\text{m}) + 0.0004\text{m})(0.05\text{m})^2} = 84.1 \frac{\text{kW}}{\text{m}^2}$$

$$\frac{\partial q''}{\partial H} = \frac{Q_{bulk}}{(2H+W)LH} = \frac{0.1682\text{W}}{((2 \times 0.0002\text{m}) + 0.0004\text{m})(0.05\text{m})(0.0002\text{m})} = 21.025 \frac{\text{kW}}{\text{m}^3}$$

$$\frac{\partial q''}{\partial W} = \frac{Q_{bulk}}{(2H+W)LW} = \frac{0.1682\text{W}}{((2 \times 0.0002\text{m}) + 0.0004\text{m})(0.05\text{m})(0.0004\text{m})} = 10.5125 \frac{\text{kW}}{\text{m}^3}$$

$$\delta Q_{bulk} = \pm 6.057 \times 10^{-6} \text{ kW}$$

$$\delta L = (0.05\text{m})(0.05) = 2.5 \times 10^{-3} \text{ m}$$

$$\delta H = (0.0002\text{m})(0.05) = 1 \times 10^{-5} \text{ m}$$

$$\delta W = (0.0004\text{m})(0.05) = 2 \times 10^{-5} \text{ m}$$

$$\delta q'' = \sqrt{\left((25000 \text{m}^{-2})(\pm 6.057 \times 10^{-6} \text{ kW})\right)^2 + \left((84.1 \text{m}^{-2})(1 \times 10^{-5} \text{ m})\right)^2 + \left((21.025 \text{m}^{-3})(1 \times 10^{-5} \text{ m})\right)^2 + \left((10.5125 \text{m}^{-3})(2 \times 10^{-5} \text{ m})\right)^2}$$

$$\delta q'' = \pm 0.3891 \frac{\text{kW}}{\text{m}^2}$$

$$\frac{\delta q''}{q''} \times 100 = \frac{\pm 0.3891}{4.205} \times 100 = 9.25\%$$

The uncertainty of the wall temperature ( $\delta T_{wall,avg}$ )

$$T_{wall,avg} = \frac{1}{N} \sum_{i=1}^N T_i$$

$$\delta T_{wall,avg} = \sqrt{N \left( \frac{1}{N} \delta T \right)^2}$$

$$\delta T_{wall,avg} = \sqrt{5 \left( \frac{1}{5} \cdot (0.5) \right)^2}$$

$$\delta T_{wall,avg} = \pm 0.2236^\circ C$$

The uncertainty of the fluid temperature ( $\delta T_{fluid}$ )

$$T_{fluid} = \frac{T_{fluid,in} + T_{fluid,out}}{2}$$

$$\delta T_{fluid} = \sqrt{2 \left( \frac{1}{2} \cdot (0.5^\circ C) \right)^2}$$

$$\delta T_{fluid} = \pm 0.3536^\circ C$$

The uncertainty of the heat transfer coefficient ( $\delta h$ )

$$\delta h = \sqrt{\left( \frac{\partial h}{\partial T_{wall}} \cdot \delta T_{wall} \right)^2 + \left( \frac{\partial h}{\partial T_{fluid}} \cdot \delta T_{fluid} \right)^2 + \left( \frac{\partial h}{\partial q''} \cdot \delta q'' \right)^2}$$

$$h = \frac{q''}{T_{wall} - T_{fluid}} = \frac{4.205 \frac{kW}{m^2}}{(75.08 - 39.27)^\circ C} = 0.1174 \frac{kW}{m^2 \cdot ^\circ C}$$

$$\frac{\partial h}{\partial T_{wall}} = \frac{q''}{(T_{wall} - T_{fluid}) T_{wall}} = \frac{4.205 \frac{kW}{m^2}}{(75.08 - 39.27)^\circ C (75.08)^\circ C} = 1.564 \times 10^{-3}$$

$$\frac{\partial h}{\partial T_{fluid}} = \frac{q''}{(T_{wall} - T_{fluid}) T_{fluid}} = \frac{4.205 \frac{kW}{m^2}}{(75.08 - 39.27)^\circ C (39.27)^\circ C} = 2.99 \times 10^{-3}$$

$$\frac{\partial h}{\partial q} = \frac{1}{T_{wall} - T_{fluid}} = \frac{1}{(75.08 - 39.27)^\circ C} = 2.793 \times 10^{-2}$$

$$\delta h = \sqrt{\left( (1.564 \times 10^{-3})(0.2236^\circ) \right)^2 + \left( (2.99 \times 10^{-3})(0.3536) \right)^2 + \left( (2.793 \times 10^{-2})(0.3891) \right)^2}$$

$$\delta h = \pm 1.092 \times 10^{-2} \frac{kW}{m^2 \cdot ^\circ C}$$

$$\frac{\delta h}{h} = \frac{\pm 1.092 \times 10^{-2} \frac{kW}{m^2 \cdot ^\circ C}}{0.1174 \frac{kW}{m^2 \cdot ^\circ C}} = 9.3\%$$

The uncertainty of the Nusselt number ( $\delta Nu$ )

$$\delta Nu = \sqrt{\left( \frac{\partial Nu}{\partial h} \cdot \delta h \right)^2 + \left( \frac{\partial Nu}{\partial D_h} \cdot \delta D_h \right)^2}$$

$$Nu = \frac{h D_h}{k} = \frac{\left( 0.1174 \frac{kW}{m^2 K} \right) (0.0002667 m)}{0.00063157 \frac{kW}{m \cdot K}} = 0.04958$$

$$\frac{\partial Nu}{\partial h} = \frac{D_h}{k} = \frac{0.0002667 m}{0.00063157 \frac{kW}{m \cdot K}} = 0.4223$$

$$\frac{\partial Nu}{\partial D_h} = \frac{h}{k} = \frac{0.1174 \frac{kW}{m^2 K}}{0.00063157 \frac{kW}{m \cdot K}} = 185.89$$

$$\delta Nu = \sqrt{\left( (0.4223)(1.092 \times 10^{-2}) \right)^2 + \left( (185.89)(8.246 \times 10^{-9}) \right)^2}$$

$$\delta Nu = \pm 4.612 \times 10^{-3}$$

$$\frac{\delta Nu}{Nu} = \frac{\pm 4.612 \times 10^{-3}}{0.04958} = 9.3\%$$

**Table A.** Uncertainties of measured quantities and calculated parameters conclusion

<b>Variable</b>	<b>Maximum relative uncertainty</b>	<b>Source</b>
Pressure	$\pm 0.2\%$	Manufacturers specs (Bourdon HEANI)
Temperature	$\pm 0.4\%$	Manufacturers specs (Omega)
Water mass flow rate	$\pm 0.1\%$	Resolution limit
Gas volumetric flow rate	$\pm 8\%$	Resolution limit
Channel dimension	$\pm 5\%$	Resolution limit
Superficial velocity of gas	$\pm 12.8\%$	Uncertainty Propagation (Figiola and Beasley, 2006 on eq. 14)
Superficial velocity of liquid	$\pm 9.85\%$	Uncertainty Propagation (Figiola and Beasley, 2006 on eq. 14)
Frictional pressure drop	$\pm 3.99\%$	Uncertainty Propagation (Figiola and Beasley, 2006 on eq. 14)
Nusselt number	$\pm 9.3\%$	Uncertainty Propagation (Figiola and Beasley, 2006 on eq. 14)

According to error analysis theory, the uncertainties in Table A. are estimated as follows (Figiola and Beasley, 2006).

## **APPENDIX B. GRAPHICAL PROGRAMMING FOR DATA ACQUISITION SYSTEM**

The National Instrument data acquisition system is used to collect the experimental data which using NI LabVIEW software for the experimental computing and data visualization.

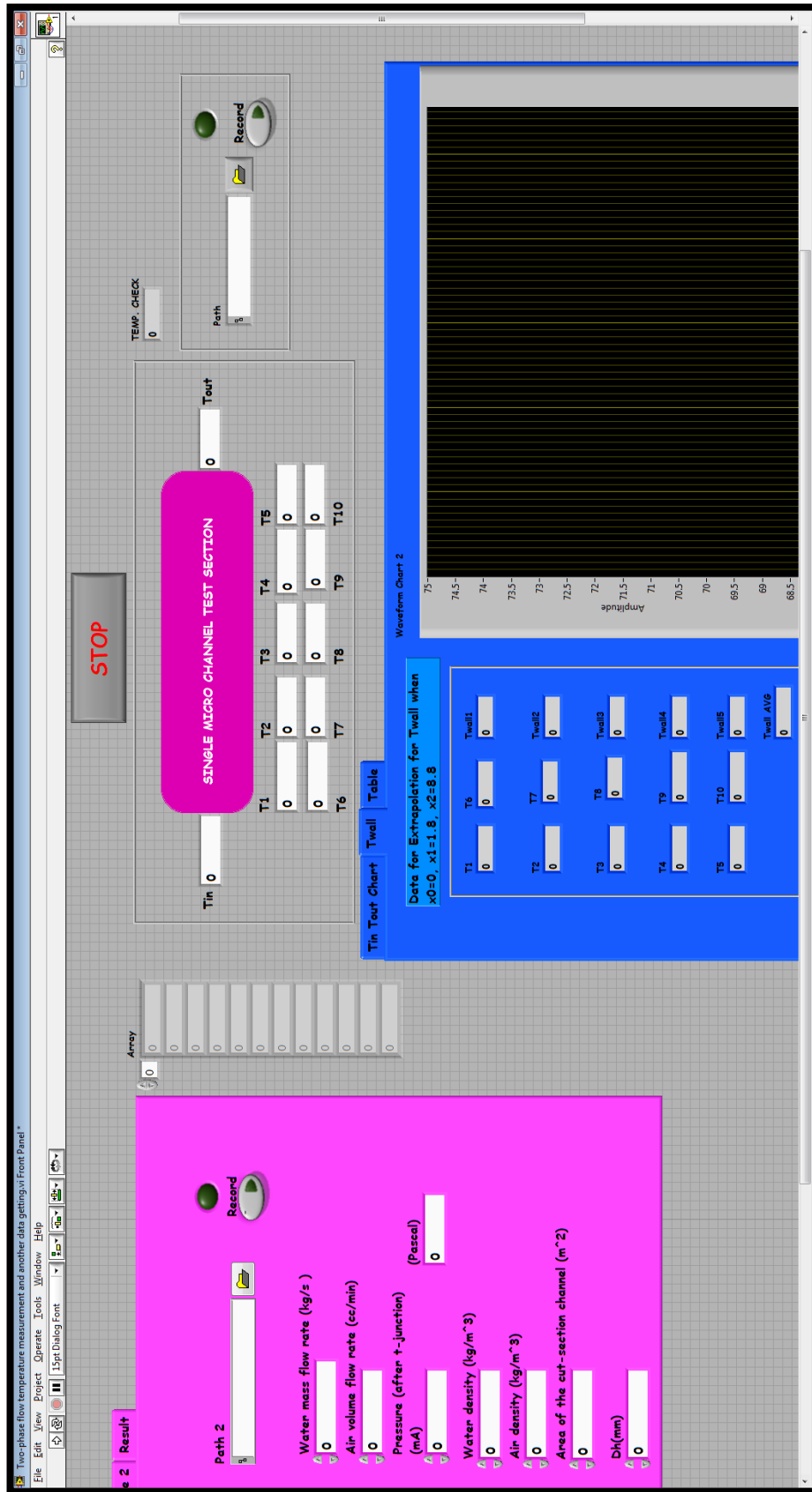


Figure B.1 LabVIEW front panel for monitoring and displaying the system

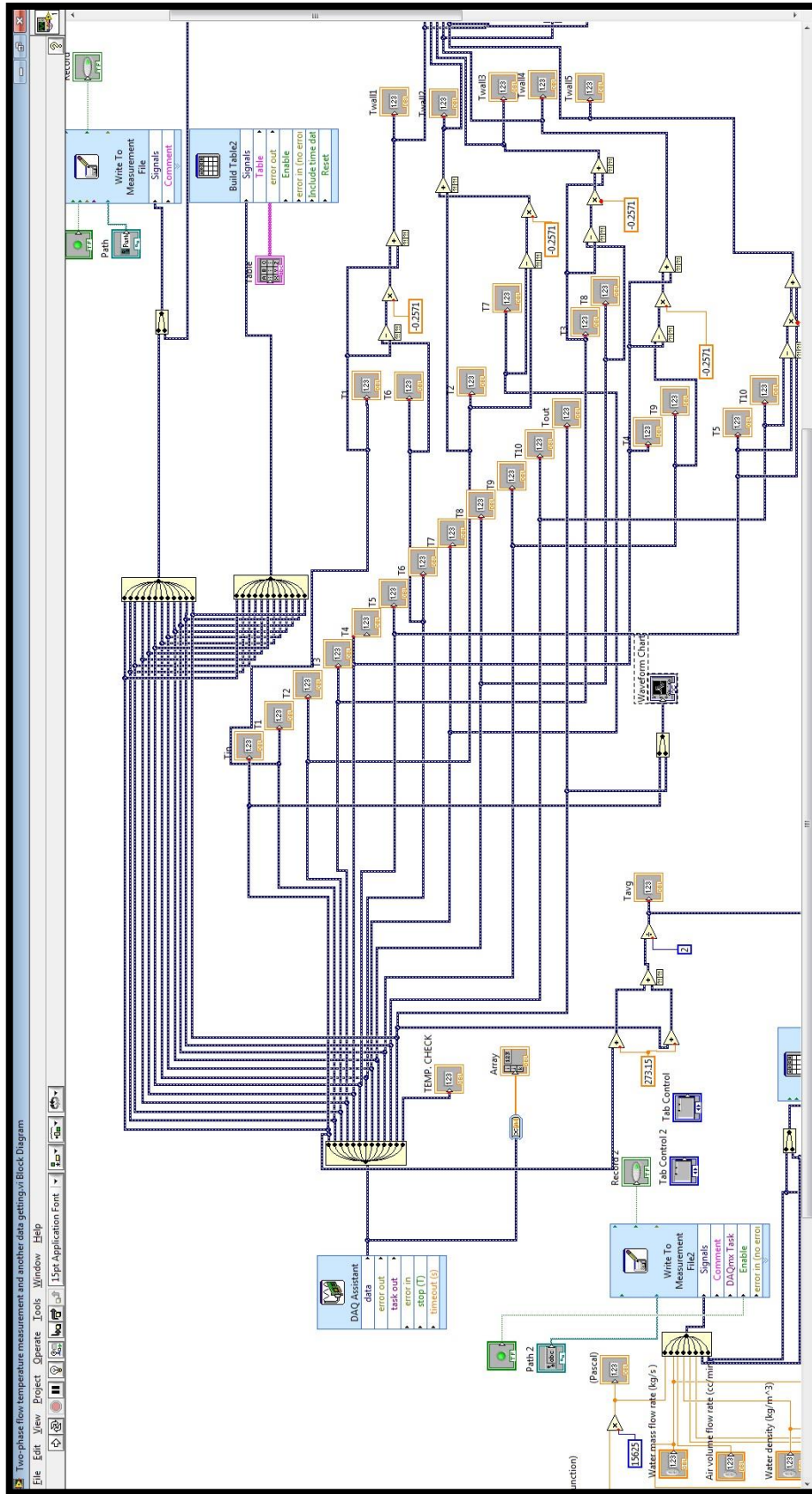


Figure B.2 The structure of a graphical block diagram

**APPENDIX C. DRAWING CONSTRUCTIONS OF THE  
TEST SECTION ASSEMBLY**

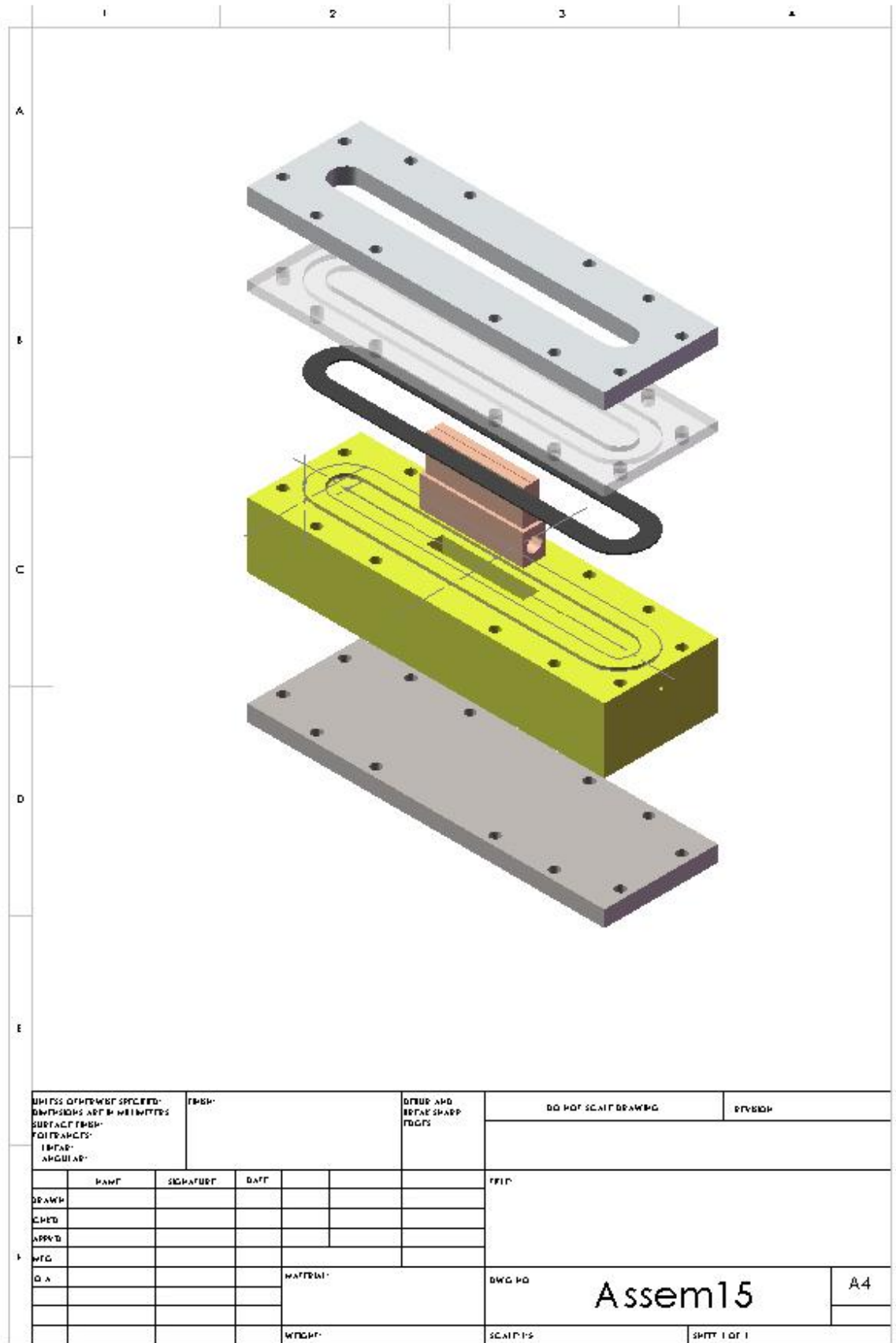


Figure C.1 The 2-D drawing of parts assembly

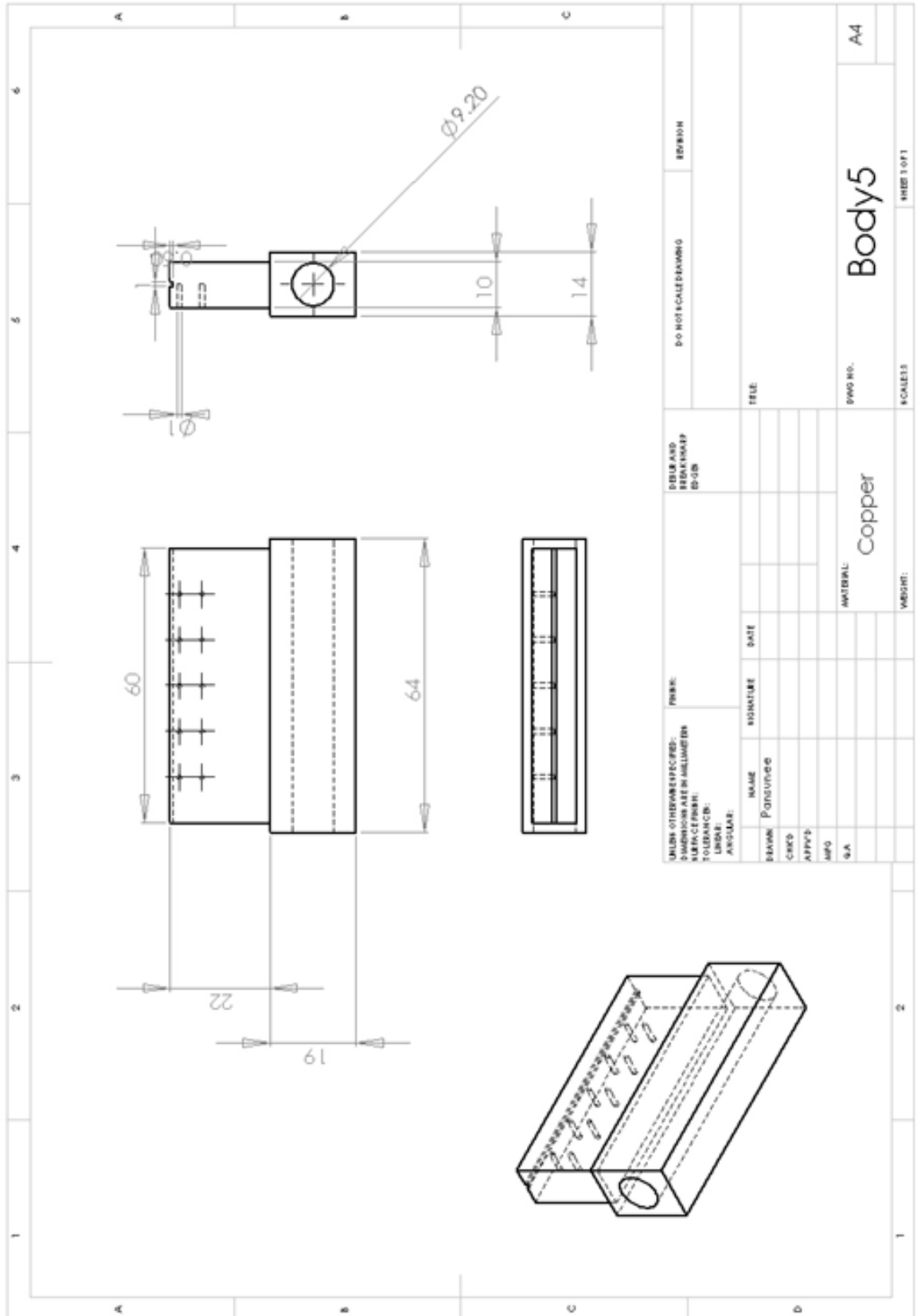
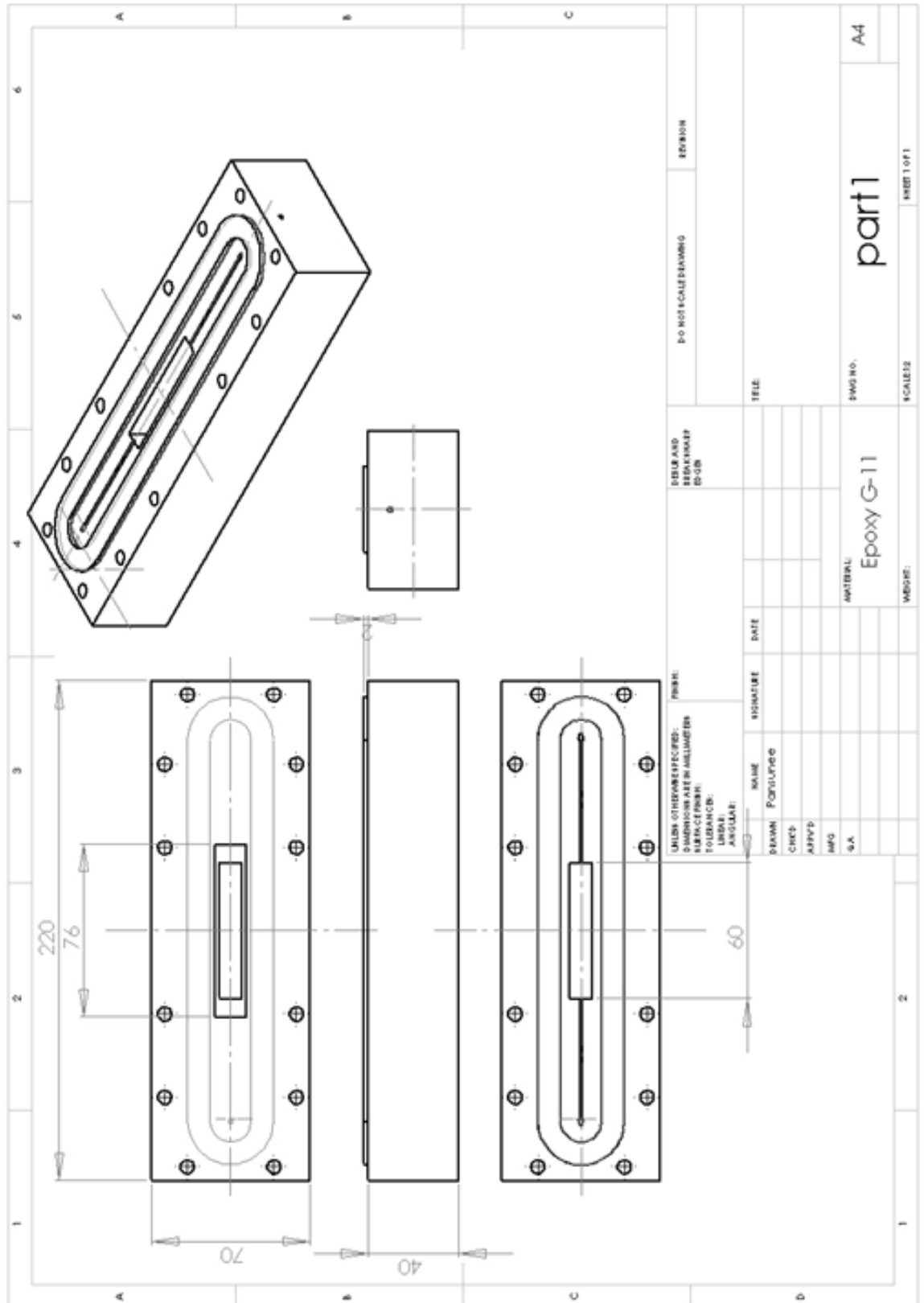


Figure C.2 The 2-D drawing of a copper body



**Figure C.3** The 2-D drawing of an insulator cover

# CHAPTER 1 INTRODUCTION

## 1.1 Rational

The two-phase flow of gas and liquid is not only usually found in nature but is also widely used in energy and chemical applications. There are many related applications, such as oil transport and processing, steam generators, cooling systems, and reactors. Presently, the two-phase flow in microchannels has found applications as Micro-Electro-Mechanical Systems (MEMS), cooling electronics devices, medical systems, and bioengineering systems for the different purposes. Hence, the knowledge of fluid mechanics and heat transfer in micro scale devices is necessary. It leads to the study of the two-phase flow in microchannels with an emphasis on pressure drop, void fraction, flow pattern, and heat transfer coefficient. These are important elements for the design and development of devices to provide the best performance.

## 1.2 Literature review

Over the past decades, the single-phase flow of liquids or gases has been a topic of interest, and many questions about single-phase flow in small channels have been answered reasonably. On the other hand, the two-phase gas-liquid flow in microchannels has received comparatively little attention in literature (Fouilland and Fletcher, 2010).

For two-phase flow in the conventional size, gravitation highly influences the shear stress and surface tension. In microchannels, the influence of gravitation to shear stress and the surface tension relationship is reduced. This is a significant change of the various states discovered by Kreutzer et al. (2005) who proposed to divide the size of the channel. The flow pattern in the two phases with the critical Bond number can be used and has been analyzed by Bretherton (1961).

$$Bo = \frac{(\rho_L - \rho_G)gD_h^2}{\sigma} < 3.368 \quad (1.1)$$

where  $\rho_L$  and  $\rho_G$  are the gas and liquid densities, respectively,  $\sigma$  is the surface tension,  $g$  is the gravitational constant.

Thus, if we use air-water as the working fluid, it can be said that the hydraulic diameter of two-phase flow, which can be referred to as “microchannel,” is  $D_h < 5$  mm.

### Adiabatic Two-Phase Flow Patterns

During the past decade, there are a number of researches that study of two-phase flow pattern in microchannels. They conducted experiments by varying the shape, size, and working fluids of the microchannels for the purpose of observing the flow patterns and generating the flow regime maps.

Triplett et al. (1999) studied horizontal channels as circular microchannels with 1.1 and 1.45 mm diameter and semi-triangular microchannels with hydraulic diameters of 1.09 and 1.49 mm presented bubbly, churn, slug, slug-annular, and annular flow patterns. They found that the experimental data could be compared with the similar data of Suo and Griffith (1964) and Damianides and Westwater (1988).

For the vertical channels, Satitchaicharoen and Wongwises (2004) conducted the experiment to observe the two-phase flow of air-water, air-20 wt. % glycerol solution, and air-40 wt. % glycerol solution. They used five various sized rectangular test sections of mini-gap transparent acrylic glass channels and reported that the flow patterns of cap-bubbly, slug, churn, and annular types were observed in every size of channel, whereas the bubbly flow pattern was only found in the 40 mm × 3 mm rectangular section of air-water flow. The effects of channel sizes and working fluids were also discussed, which is consistent with the study of Zhao and Bi (2001). They reported that the bubbly flow was not found in the small channel.

There are various names of the same flow pattern that have been defined by many researchers, which results in the difficulty in distinguishing the same or different flow patterns. For example, slug (Triplett et al. 1999), Taylor (Yue et al. 2009), and bubble train flow patterns (Thulasidas et al. 1997) have been designed to indicate the same flow pattern.

### **Two-Phase Pressure Drop**

Many researchers, such as Cubaud and Ho (2004), Chung and Kawaji (2004), and Saisorn and Wongwises (2008) have applied the separated flow model with the

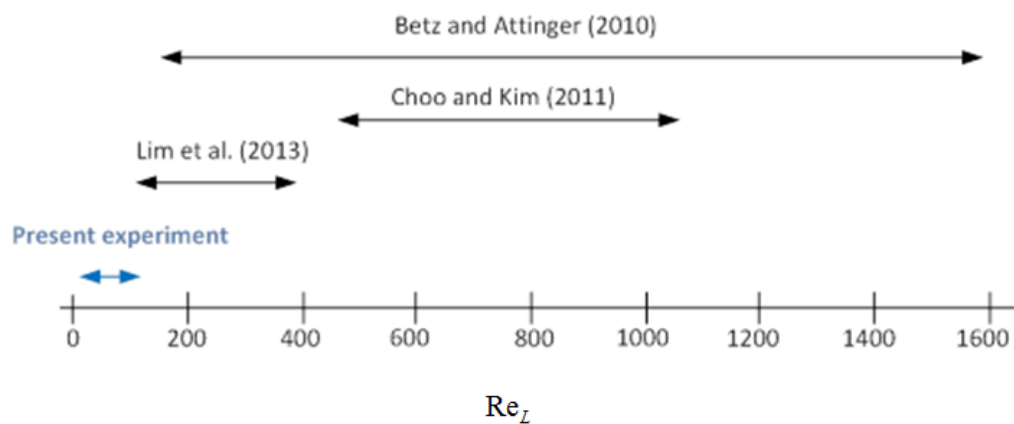
modified two-phase frictional multiplier to predict a two-phase frictional pressure drop. On the other hand, Sur and Liu (2012) showed that using flow pattern-based model can predict the frictional pressure drop better than the separated or homogeneous flow model.

### **Heat Transfer Characteristics**

Nowadays, electronic devices and the microprocessor are available in smaller sizes. The optimized cooling system design needs for heat transfer enhancement. Most researchers focus on the study of using flow boiling to enhance heat transfer in the system instead of on the single-phase flow that occur in low Nusselt number in the laminar flow condition. However, using flow boiling may be ineffective backflow, due to flashing, and instability phenomena. Moreover, it is not suitable to use air and water as the working fluids in flow boiling because of the high boiling temperature of the water. Thus, the segmented air-water flow in microchannels is proposed by Betz and Atinger (2010), Lim et al. (2013), and Majumder et al. (2013). They concluded that segmented air-water flow can enhance the Nusselt number in the channels up to 1.76 times over the single-phase flow of water. The factors that make the heat transfer enhancement are the mixer velocity from the air injection and the internal circulation of liquid slug induced by the gas bubbles, which enhances the mixing of the hot liquid film near the channel wall with cooler liquid from the center.

There are few researches on two-phase flow in microchannels, and researches on of the segmented flow characteristics in microchannels have gaps and conflicting conclusions as shown in Figure 1.1. Therefore, it is necessary to add to fill the research gap completely and accurately.

In this work, we performed the experimental study on two-phase flow patterns, the pressure drop, and segmented flow heat transfer characteristics of a rectangular microchannel having unique shape and size with different flow conditions in order to fulfill and improve the fundamental understanding of two-phase flow in the microchannel.



**Figure 1.1** Range of Reynolds which the Nusselt number have been studied in the microchannels

### 1.3 Objectives

1. To conduct conduct systematic experiments to study on two-phase flow pattern, pressure drop and segmented flow heat transfer characteristics of a rectangular microchannel which has the unique shape, size and flowing conditions in order to fulfill and improve the fundamental understanding of two-phase flow in microchannels.
2. To compare the experimental results with the relevant models and correlations.

#### **1.4 Scopes**

1. A copper rectangular microchannel is used as the test section and placed horizontally.
2. Working fluids are air and water under ambient conditions.
3. Two-phase flow patterns, pressure drop and heat transfer characteristics will be determined.

## **CHAPTER 2 BACKGROUND KNOWLEDGE**

### **2.1 Method of analysis**

The method is used to analyze a two-phase flow, and is an extension of those already well known for single-phase flows. Three main types of assumption have been made. These are also applied to the flow in microchannel.

#### **2.1.1 Homogeneous flow model**

In this approach, the simplest approach to the problem, the two-phase flow is assumed to be a single-phase flow having pseudo-properties arrived by suitably weighting the properties of the individual phase.

#### **2.1.2 Separated flow model**

In this approach, the two phases of the flow are considered to be artificially segregated. Two sets of basic equations can now be written, one for each phase. Alternatively, the equations can be combined. In either case formation must be forthcoming about the area of the channel occupied by each phase (or alternatively, about the velocities of each phase) and about the friction interactions with the channel wall. In the former case additional information concerning the frictional interaction between phases is also required. This information is inserted into the basic equations, either from separating empirical relationships in which the void fraction and the wall shear stress relate to the primary variables, or on the basis of simplified models or flow.

### **2.1.3 Flow pattern model**

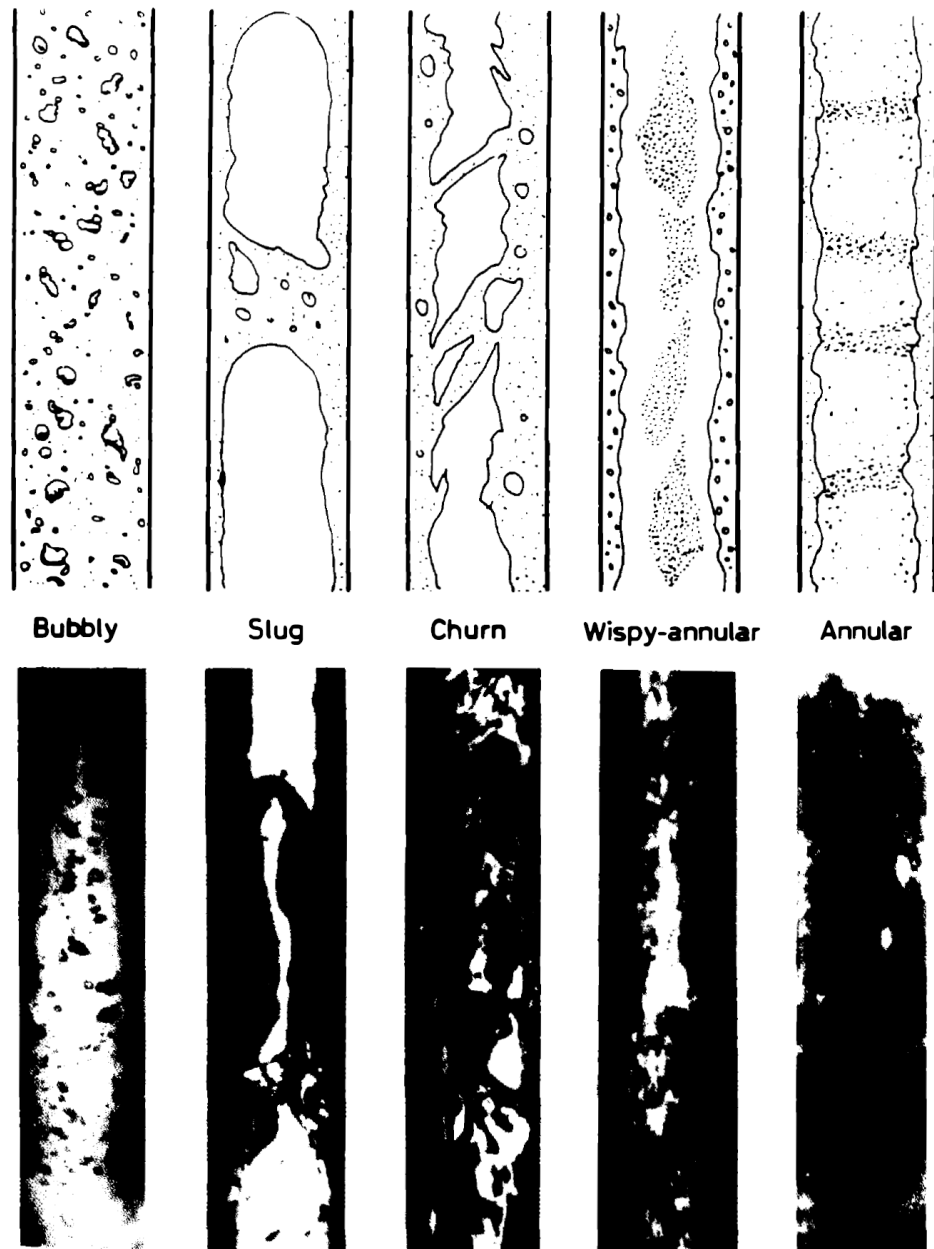
In this more sophisticated approach the two-phase are considered to be arranged in one of three or four definite prescribed geometries. These geometries are based on the various configuration or flow patterns found when a gas and a liquid flow together in a channel. The basic equations are solved within the framework of each of these idealized representations. In order to apply these models, it is necessary to know when each should be used and to be able to predict the transition from one pattern to another. Nevertheless, this approach is still in its infancy.

## **2.2 Flow patterns**

The particular flow pattern depends on the conditions of pressure, flow, heat flux and channel geometry. Each has a descriptive name and the design of a heat exchanger, it is desirable to know what the flow pattern or successive flow patterns are so that hydrodynamic or heat transfer theory appropriate to that pattern can be chosen.

### **2.2.1 Flow patterns in vertical co-current flow**

The flow patterns encountered in vertical upwards co-current flow are shown schematically in Figure 2.1 together with actual photographs of each flow pattern.



**Figure 2.1** Flow patterns in vertical pipe (Collier and Thome, 1996)

### 2.2.1.1 Bubbly flow

In bubbly flow the gas or vapor phase is distributed as discrete bubbles in a continuous liquid phase. At one extreme the bubble may be large with a spherical cap and a flat tail. In this latter state, although the size of bubbles does not approach the diameter of the pipe, there may be some confusion with slug flow.

### **2.2.1.2 Slug flow**

In slug flow, the gas or vapor bubbles are approximately the diameter of the pipe. The nose of the bubble has a characteristic spherical cap and a gas in the bubble is separated from the pipe wall by a slowly descending film of liquid. The liquid flow is contained in liquid slugs which separate successive gas bubbles. These slugs may or may not contain smaller entrained gas bubbles carried in the wake of the large bubble. The length of the main gas bubble can vary considerably.

### **2.2.1.3 Churn flow**

Churn flow is formed by the breakdown of the large vapor bubbles in slug flow. The gas or vapor flows in a more or less chaotic manner through the liquid which is mainly displaced to the channel wall. The flow has an oscillatory or time varying character; hence, the descriptive name 'churn' flow. This region is also sometimes referred to as semi-annular or slug-annular flow.

### **2.2.1.4 Wispy-annular flow**

Wispy-annular flow has the form of a relatively thick liquid film on the walls of the pipe together with a considerable amount of liquid entrained in a central gas or vapor core. The liquid in the film is aerated by small gas bubbles and the entrained liquid phase appears as large droplets which have agglomerated into long irregular filaments or wisps.

### **2.2.1.5 Annular Flow**

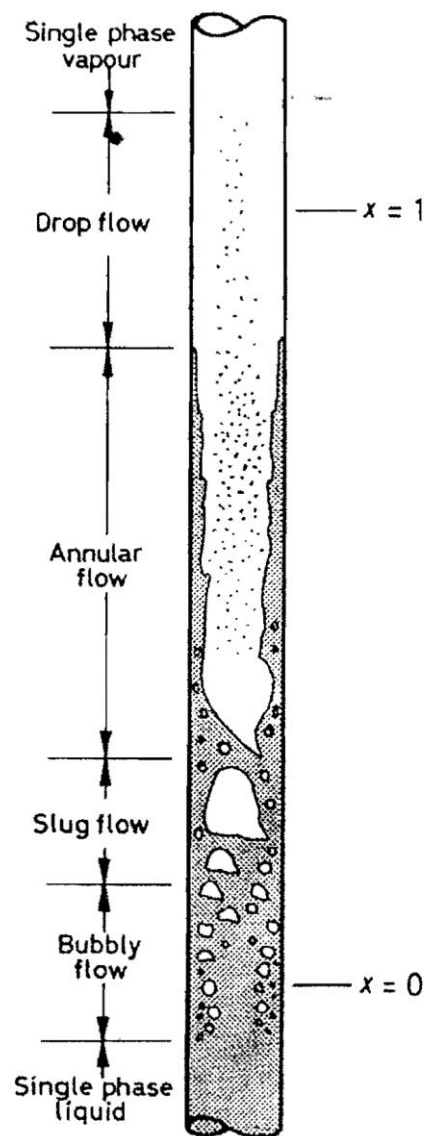
In annular flow, a liquid film forms at the pipe wall with a continuous central gas or vapor core.

### **2.2.2 Flow pattern in vertical heated channels**

The formation of a two-phase mixture by vapor generation in a vertical heated tubular channel represents an important special case. The presence of a heat flux through the channel wall alters the flow pattern from that which would have occurred in a long unheated channel at the same local flow conditions. These changes occur due to two main reasons: firstly, the departure from thermodynamic equilibrium coupled with the presence of radial temperature profiles in the channel, and secondly, the departure from local hydrodynamic equilibrium throughout the channel. Figure 2.2 shows a schematic representation of a vertical tubular channel heated by uniform low heat flux and fed at its base with liquid just below the saturation temperature.

In the initial single-phase region, the liquid is being heated to the saturation temperature. A thermal boundary layer forms at the wall and a radial temperature profile is set up. At some position upstream, the wall temperature will exceed the saturation temperature and the conditions for the formation of vapor (nucleation) at the walls are satisfied. The vapor is formed at preferred positions or sites on the surface of the tube. Vapor bubbles gravity from these sites finally detach from tube wall to form a bubbly flow. With the production of more vapor, the bubble population increases with length and coalescence takes place to form slug flow, which in turn gives way to annular flow further along the channel. Close to the boiling point, the formation of

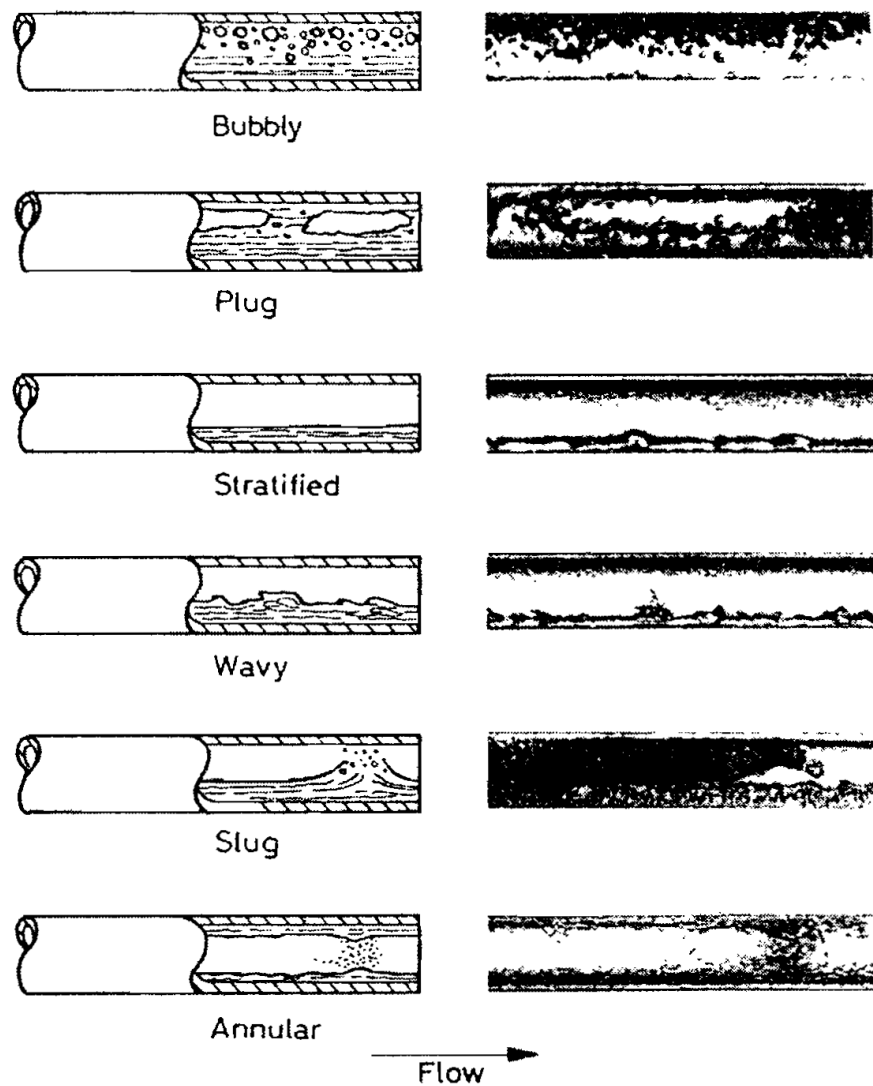
vapor at sites on the wall may cease and further vapor formation will be a result of evaporation at the liquid film-vapor core interface. Increasing velocities in the vapor core will cause entrainment of liquid in the form of droplets. The depletion of the liquid from the film by this entrainment and by evaporation finally causes the film to dry out completely. Droplets continue to exist and slowly evaporate until only single-phase vapor is present.



**Figure 2.2** Flow patterns of flow boiling in vertical pipe (Collier and Thome, 1996)

### 2.2.3 Flow patterns in horizontal co-current flow

The flow patterns observed in co-current two-phase flow in horizontal and inclined tubular channels are complicated by asymmetry of the phases resulting from the influence of gravity. The generally accepted flow patterns as given by Alves (1954) are shown diagrammatically in Figure 2.3.



**Figure 2.3** Flow patterns in horizontal pipe (Collier and Thome, 1996)

### **2.2.3.1 Bubbly flow**

This flow pattern is similar to that in vertical flow except that the vapor bubbles tend to travel in the upper half of the pipe.

### **2.2.3.2 Plug flow**

This is similar to slug flow in the vertical direction. Again the gas bubbles tend to travel in the upper half of the pipe.

### **2.2.3.3 Stratified flow**

This pattern only occurs at very low liquid and vapor velocities. The two-phase flow separates with a relatively smooth interface.

### **2.2.3.4 Wavy flow**

As the vapor velocity is increased the interface becomes disturbed by waves traveling in the direction of flow.

### **2.2.3.5 Slug flow**

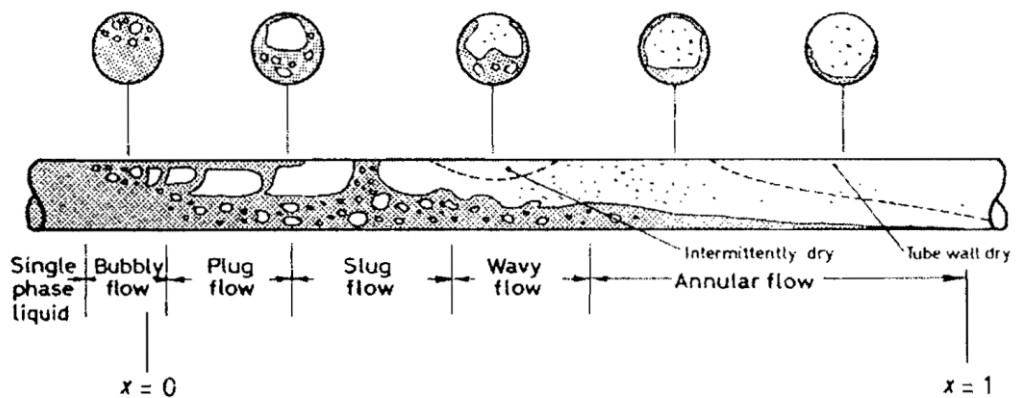
A further increase in vapor velocity causes the wave at the interface to be picked up to form a frothy slug which is propagated along the channel at a high velocity. The upper surface of the tube behind the wave is wetted by a residual film which drains into the bulk of the liquid.

### 2.2.3.6 Annular flow

A still higher vapor velocity will result in the formation of a gas core with a liquid film around the periphery of the pipe. The film may or may not be continuous around the entire circumference but it will be thicker at the base of the pipe.

### 2.2.4 Flow patterns in horizontal heated channels

Similar flow structures previously discussed can also be found in the horizontal pipe. Flow patterns formed during the generation of vapor in horizontal tubular channels are influenced by departures from thermodynamic and hydrodynamic equilibrium in the same way as for vertical flow. Figure 2.4 shows a schematic representation of a horizontal tubular channel heated by a uniform low heat flux and fed with liquid just below the saturation temperature.



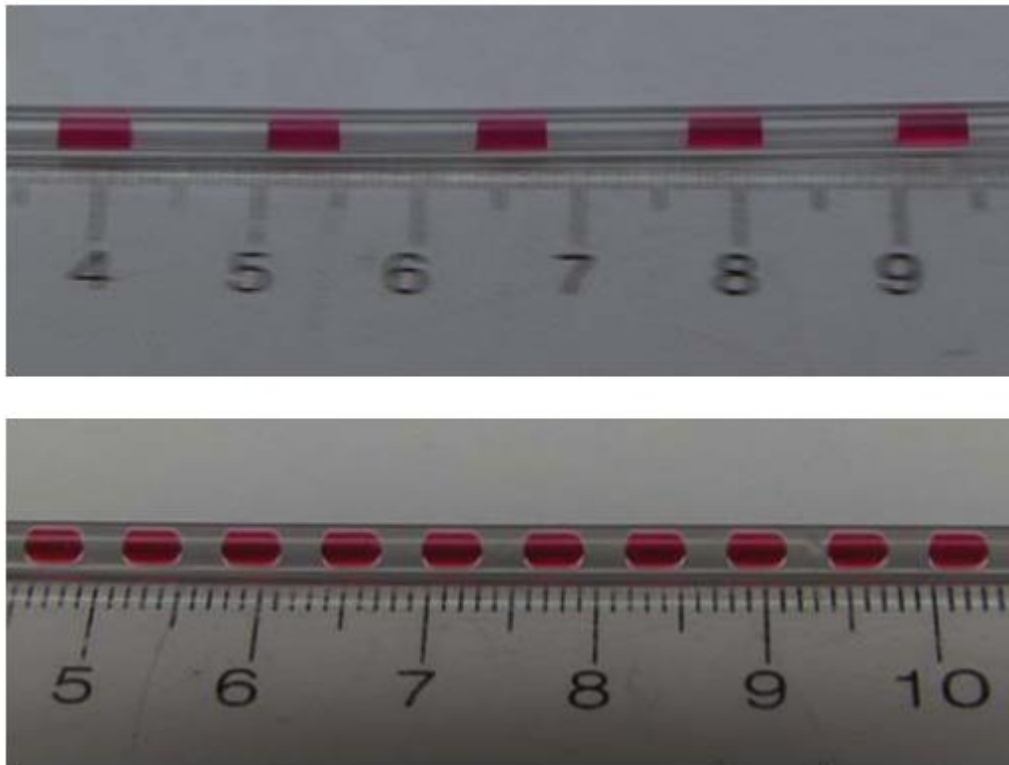
**Figure 2.4** Flow patterns of flow boiling on horizontal pipe (Collier and Thome, 1996)

The design of many heat exchangers using horizontal tubular elements requires that these elements be interconnected using  $180^\circ$  return bends to form a serpentine

arrangement. In this case the influence of the return bend on the flow pattern is considerable. This topic is interesting for further research.

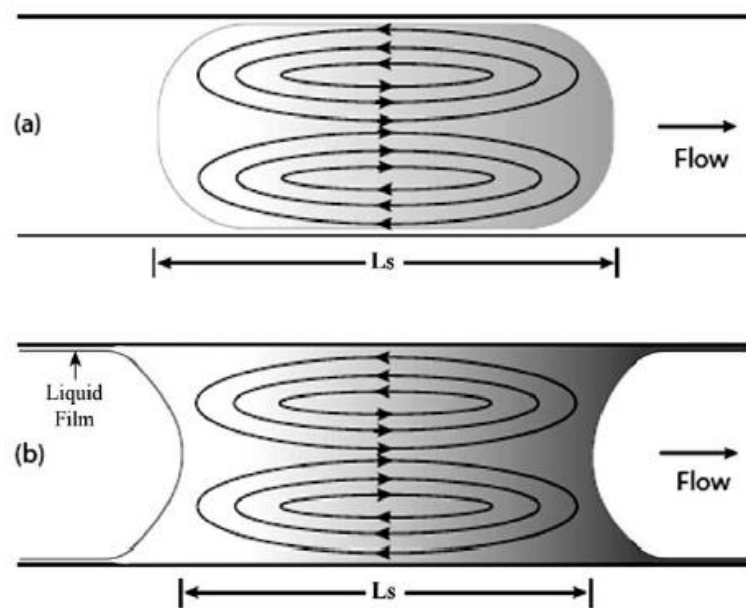
### 2.3 Hydrodynamic of segmented flow

Many researchers have preferred as the segmented gas-liquid flow stream as Taylor plug flow. Examples of gas-liquid and liquid-liquid segmented flow are shown in Figure 2.5



**Figure 2.5** Water/air (top) and oil/water (bottom) segmented flow. The water has been tinted red for enhanced visualization of the interface (Janes et al., 2010)

An important characteristic of Taylor flow is presence of a pair of recirculation zones within the liquid plugs as shown in Figure 2.6. These zones result from the presence of the liquid/gas or liquid/liquid interface. The dynamics of the fluid motion is such that the circulation rolls in a manner akin of tank tracks in the direction of the flow. The circulation affects the flow in a manner which promotes radial transport of heat or mass in addition to a boundary layer renewal, since the fresh fluid is constantly being transported to the leading edge of the plug. In Muzychka et al. (2009), the authors show that heat transfer data for isothermal tubes scaled according to plug length so that the classic Graetz-Leveque model could be used as predictive measure of the thermal performance, provided certain conditions are met.



**Figure 2.6** Liquid plug circulation in segmented flow; a) hydrophobic and b) hydrophilic (Talimi et al., 2012)

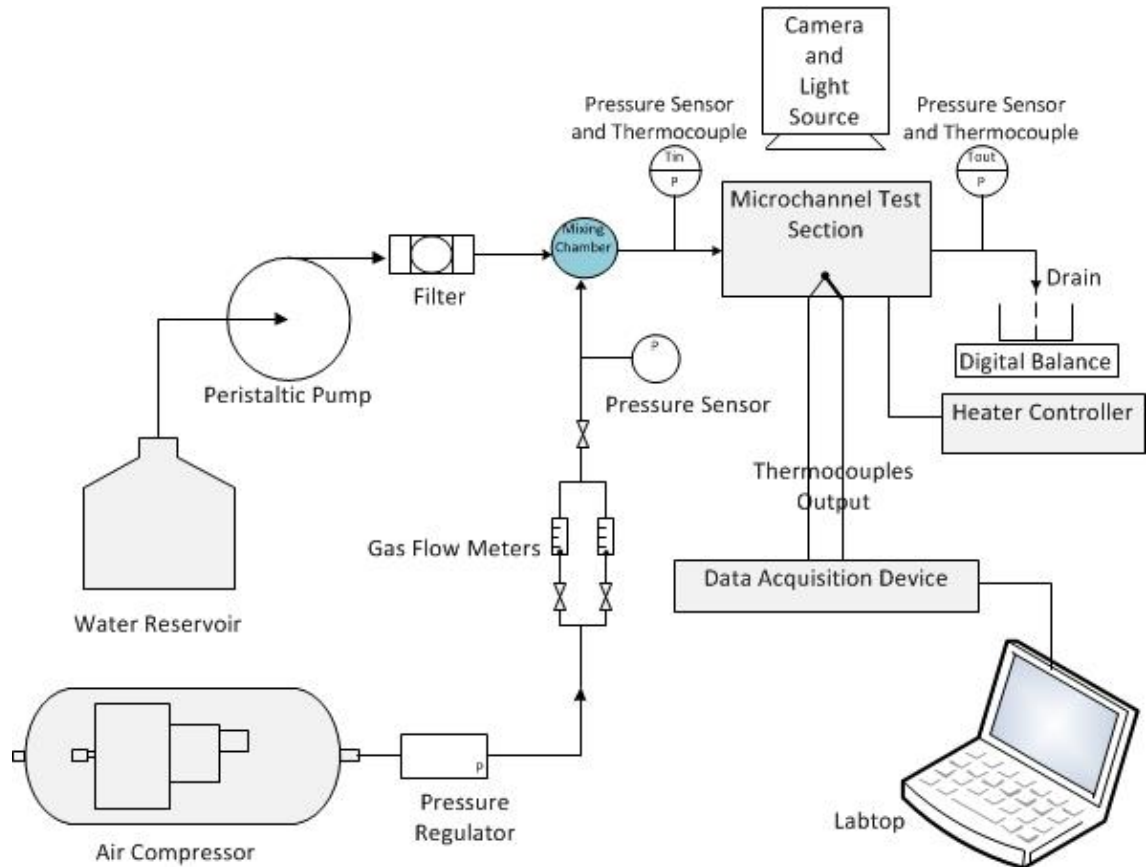
## CHAPTER 3 EXPERIMENTAL APPARATUS

The schematic diagram of the test apparatus is shown in Fig. 3.1. Water and air were mixed by the Valco Tee connector as Fig. 3.3 (SS, 0.25 mm bore, 1/16", 10-32) where the water was pumped from a peristaltic pump (Masterflex L/S, easy-load model 7518-00) and the mass flow rate of water was found by measuring at the outlet with a digital balance ( $320 \pm 0.001$  g). The air was injected to generate bubbles by air compressor through a pressure regulator and the air flow rates are measured by two sets of rotameter within the range of 5-50 sccm and 0.05-0.5 SCFH, respectively (Dwyer, 5-50 sccm  $\pm 8\%$  uncertainty, 0.05-0.5 SCFH  $\pm 4\%$  uncertainty). The pressure was varied depending on the mass flow rate. The pressure drop along the channel was measured (BOURDON HAENNI, type E913, 250 kPa,  $\pm 0.5$  kPa uncertainty). Thermocouples (Type T 0.5 mm diameter, Omega, 100 ms response time,  $\pm 0.5^\circ\text{C}$  or 0.4% uncertainty) are used to measure water temperatures at the inlet and outlet of the test section. The data of temperature and pressure were collected by a data acquisition system (National Instrument NI CompactDAQ).

A rectangular microchannel (Fig. 3.2) device consists of a single rectangular microchannel. It was made from a copper slab with the dimensions 500 mm of length, 400  $\mu\text{m}$  of width, 200  $\mu\text{m}$  of height. This 267  $\mu\text{m}$  hydraulic diameter of microchannel used to create and observe the flow. The cover of the test section is transparent polycarbonate. The copper heat substrate was heated in the constant value by the cartridge heater from DC power supply source which verify the surface temperature by using the five rows of two thermocouples and calculate surface temperature by the linear extrapolation. The test section was good insulated by G10 epoxy and bolt together with the a copper part of rectangular microchannel and the aluminium cover plate to firm the assembly.

The flow was illuminated by the cold light (LED) source and stereo zoom microscope (Nikon SMZ745T) mounted together with a camera system (Nikon D7100, shutter speeds of 1/30 – 1/8,000 sec.) were used for record each flow pattern that occurred in a microchannel.

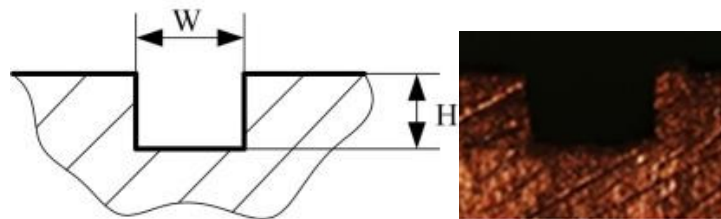
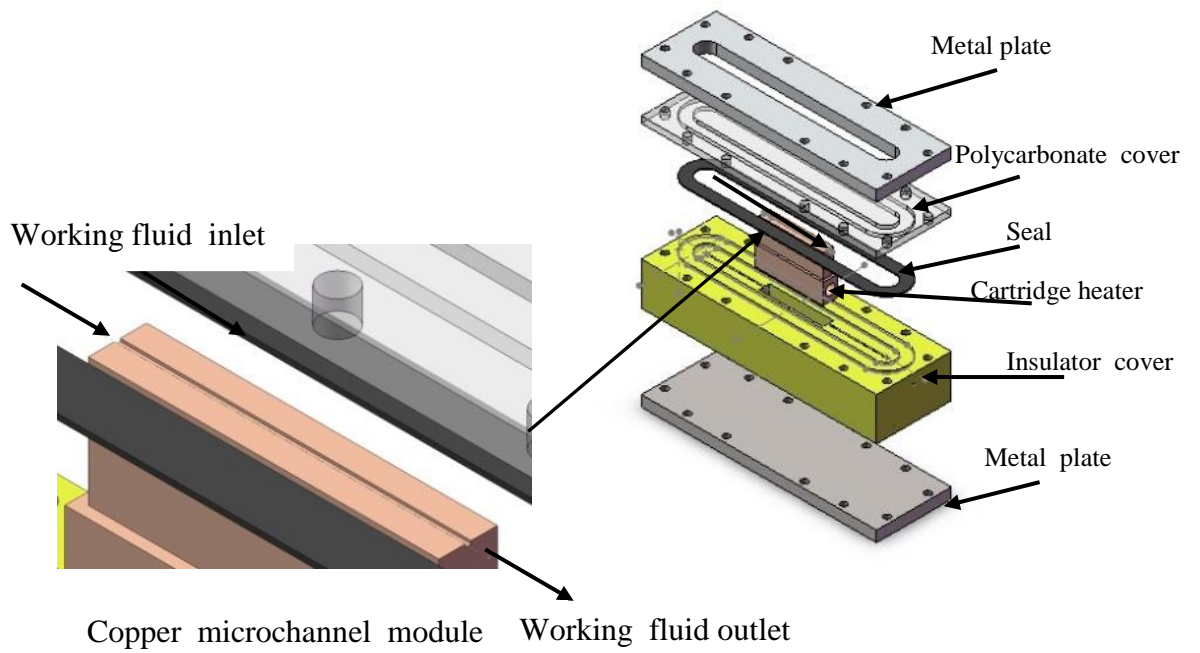
The experiments were conducted at the room temperature (30° C) at various air and liquid flow rates to define the flow regime maps. The system was allowed to approach steady conditions before the air and water flow rates, flow pattern and pressure drop were recorded.



**Figure 3.1** Schematic diagram of the experimental apparatus

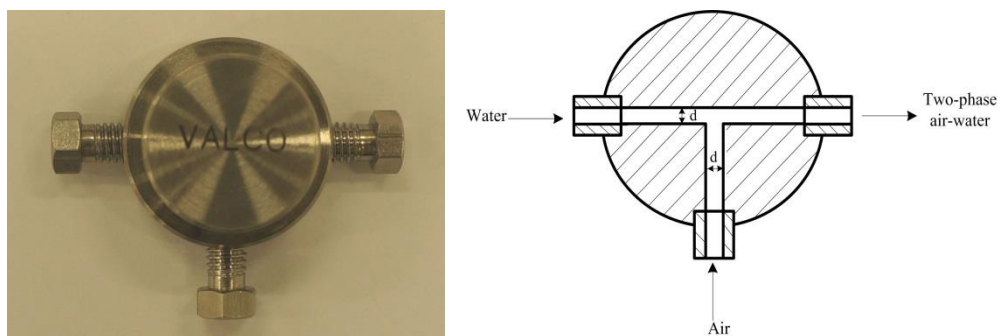
### 3.1 Test Section

A rectangular microchannel (Fig. 3.2) device consists of a single rectangular microchannel. It was made from a copper slab with the dimensions 500 mm of length, 400  $\mu\text{m}$  of width, 200  $\mu\text{m}$  of height. This 267  $\mu\text{m}$  hydraulic diameter of microchannel used to create and observe the flow. The cover of the test section is transparent polycarbonate. The copper heat substrate was heated in the constant value by the cartridge heater from DC power supply source which verify the surface temperature by using the five rows of two thermocouples and calculate the surface temperature by the linear extrapolation. The test section was good insulated by G10 epoxy and bolt together with the a copper part of rectangular microchannel and the aluminium cover plate to firm the assembly.



Section detail of microchannel after mixing section,  $W = 400 \mu\text{m}$ ,  $H = 200 \mu\text{m}$

**Figure 3.2** test section



**Figure 3.3** (a) Sketch and (b) actual photograph of the Valco Tee two-phase mixing chamber with  $d = 250 \mu\text{m}$  inner diameter.

**Table 3.1** Uncertainties of measured quantities and calculated parameters

<b>Variable</b>	<b>Maximum relative uncertainty</b>
Pressure	±0.2%
Temperature	±0.4%
Heat flux	±3.6%
Water mass flow rate	±0.1%
Gas volumetric flow rate	±8%
Channel dimension	±5%
Superficial velocity of gas	±12.8%
Superficial velocity of liquid	±9.85%
Frictional pressure drop	±3.99%
Nusselt number	±9.3%

$$W_E = \sqrt{\left(\frac{dE}{dy_1} w_1\right)^2 + \left(\frac{dE}{dy_2} w_2\right)^2 + \dots + \left(\frac{dE}{dy_n} w_n\right)^2} \quad (3.1)$$

where  $W$  is the error associated with any calculated parameter  $E$

$w$  is the error associated with any calculated parameter  $y$

Kline and McClintock (1953)

## CHAPTER 4 DATA REDUCTION

The following calculation is employed to determine the superficial velocities of the flow patterns, heat transfer coefficient, Nusselt number and two-phase friction factor, from the data recorded during each test run at steady state conditions.

### 4.1 Flow regime map

The use of multiple rotameters for the air and digital balance for water over the ranges of gas superficial velocities = 1.04-8.30 m/s of air and liquid superficial velocities = 0.0013-0.3429 m/s of water is defined as

$$U_{GS} = \frac{V_G}{A_{ch}} \quad (4.1)$$

$$U_{LS} = \frac{V_L}{A_{ch}} \quad (4.2)$$

where  $A_{ch}$  is the microchannel cross-sectional area,  $V_G$  and  $V_L$  are the volume flow rates of air and water are respectively.

### 4.2 Pressure drop

The pressure drop of fluid flow through a horizontal channel can be calculated from

$$\left( \frac{dP}{dz} \right)_{frictional} = f \frac{L}{D_h} \frac{U^2}{2g} \quad (4.3)$$

where  $f$  is friction factor,  $L$  is length of the channel test section,  $U$  is average velocity in the channel test section

The Reynolds number of gas,  $Re_G$  and liquid,  $Re_L$  are defined by

$$Re_G = \frac{\rho_G U_{GS} D_h}{\mu_G}, \quad Re_L = \frac{\rho_L U_{LS} D_h}{\mu_L} \quad (4.4)$$

where  $\mu_G$  is the dynamic viscosity of gas and  $\mu_L$  is the dynamic viscosity of liquid.

Shah and London (1978) proposed a correlation of  $f$  Re for single-phase isothermal, incompressible and fully developed laminar flow in rectangular channel is

$$f \text{ Re} = 96(1 - 1.3553AR + 1.9467AR^2 - 1.7012AR^3 + 0.9564AR^4 - 0.2537AR^5) \quad (4.5)$$

$$AR = \frac{H}{W} \quad (4.6)$$

In this study, the experimentally derived friction factor is a function of Reynolds number for a rectangular channel with the aspect ratio  $AR = 0.5$  is

$$f = \frac{62.2}{\text{Re}} \quad (4.7)$$

two-phase mixture can be treated as a single-phase fluid. A two-phase pressure drop consists of frictional, accelerational and gravitational terms (Carey (1992)). The gravitational terms are neglected in the horizontal flow study so, the formula is

$$\left(\frac{dP}{dz}\right)_{TP} = \left(\frac{dP}{dz}\right)_{friction} + \left(\frac{dP}{dz}\right)_{acceleration} + \left(\frac{dP}{dz}\right)_{c/e} \quad (4.8)$$

where

$\left(\frac{dP}{dz}\right)_{friction}$  is the frictional pressure drop,  $\left(\frac{dP}{dz}\right)_{acceleration}$  is accelerational pressure drop and

$\left(\frac{dP}{dz}\right)_{c/e}$  represents pressure drop due to sudden contraction and expansion. All the components

can be evaluated by the following expressions.

$$\left(\frac{dP}{dz}\right)_{friction} = f_{TP} \frac{1}{D_h} \frac{G^2}{2\rho_{TP}} \quad (4.9)$$

where  $f_{TP}$  is a two-phase friction factor,  $G$  is the mass flux and  $\rho_{TP}$  is the two-phase density

$$\rho_{TP} = \left(\frac{x}{\rho_G} + \frac{1-x}{\rho_L}\right)^{-1} \quad (4.10)$$

$$f_{TP} = \frac{62.2}{\text{Re}_{TP}} \quad (4.11)$$

$$\text{Re}_{TP} = \frac{GD_h}{\mu_{TP}} \quad (4.12)$$

$$\left(\frac{dP}{dz}\right)_{\text{acceleration}} = G^2 \left[ \left( \frac{x^2}{\rho_G \alpha} + \frac{(1-x)^2}{(1-\alpha)\rho_L} \right)_{\text{outlet}} - \left( \frac{x^2}{\rho_G \alpha} + \frac{(1-x)^2}{(1-\alpha)\rho_L} \right)_{\text{inlet}} \right] \quad (4.13)$$

$$\left(\frac{dP}{dz}\right)_{\text{contraction}} = \frac{G^2}{2\rho_L} \left[ \left( \frac{1}{C_c} - 1 \right)^2 + \left( 1 - \frac{1}{\gamma^2} \right) \right] \left[ 1 + \left( \frac{\rho_L}{\rho_G} - 1 \right) x \right] \quad (4.14)$$

$$\left(\frac{dP}{dz}\right)_{\text{expansion}} = G^2 \gamma (\gamma - 1) \left[ \frac{1-x^2}{\rho_L (1-\alpha)} + \frac{x^2}{\alpha \rho_G} \right] \quad (4.15)$$

$x$  represents the mass quality,  $\alpha$  is the void fraction,  $G$  is the mass velocity,  $C_c$  is the coefficient of contraction which can be given by Chisholm (1983).

$$C_c = \frac{1}{0.639 \left[ 1 + \left( \frac{1}{\gamma} \right) \right]^{\frac{1}{2}} + 1} \quad (4.16)$$

where  $\gamma$  represents the ratio of the cross-sectional flow area in the flow passage connected to the channel test section to that in the channel test section.

The void fraction is used for calculation of acceleration pressure drop. Armand correlation (Armand and Treschev (1946)) was chosen which is in reasonable agreement with Serizawa et al. (2002) and Zhao and Bi (2001)

$$\alpha = 0.833\beta \quad (4.17)$$

when  $\beta$  and  $\alpha$  are gas volumetric ratio and void fraction respectively.

### Homogeneous flow model (HFM)

The homogeneous flow model assumes that the gas and liquid phases are so well mixed that the two-phase mixture can be treated as a single-phase fluid.

Viscosity for homogeneous flow model;

$$\text{McAdams et al. (1942):} \quad \mu_{TP} = \left( \frac{x}{\mu_G} + \frac{1-x}{\mu_L} \right)^{-1} \quad (4.18)$$

Owen (1961): 
$$\mu_{TP} = \mu_L \quad (4.19)$$

Dukler et al. (1964): 
$$\mu_{TP} = \beta\mu_G + (1-\beta)\mu_L \quad (4.20)$$

Beattie and Whalley (1982): 
$$\mu_{TP} = \beta\mu_G + (1-\beta)(1+2.5\beta)\mu_L \quad (4.21)$$

Lin et al. (1991): 
$$\mu_{TP} = \frac{\mu_G\mu_L}{\mu_G + x^{1.4}(\mu_L - \mu_G)} \quad (4.22)$$

Awad and Muzychka (2008): 
$$\mu_{TP} = \mu_G \frac{2\mu_G + \mu_L - 2(\mu_G - \mu_L)(1-x)}{2\mu_G + \mu_L + (\mu_G - \mu_L)(1-x)} \quad (4.23)$$

Choi and Kim (2011) proposed the accuracy of model predictions which was assessed using the mean absolute error (MAE), expresses as a percentage.

$$MAE = \frac{1}{M} \sum \left[ \frac{|\Delta P_{TP,pred} - \Delta P_{TP,exp}|}{\Delta P_{TP,exp}} \times 100 \right] \quad (4.24)$$

where  $\Delta P_{TP,pred}$  is the pressure drop obtained from predicted model,  $\Delta P_{TP,exp}$  is the pressure drop obtained from an experiment and  $M$  is the number of data,

### Separated flow model

For separated flow assumption which was found to be good agreement with the experimental data, SFMs are based on the two phase multiplier ( $\phi$ ), which is defined as

$$\phi_L^2 = \left( \frac{dP}{dz} \right)_{TP} / \left( \frac{dP}{dz} \right)_L \quad (4.25)$$

Lockhart and Martinelli (1949) suggested that  $\phi_L^2$  is a function of the Martinelli parameter

$$\phi_L^2 = 1 + \frac{C}{X_{vv}} + \frac{1}{X_{vv}^2} \quad (4.26)$$

Where  $X_{vv}$  is a parameter of a laminar liquid-laminar gas flow

$$X_{vv} = \left[ \left( \frac{dp}{dz} \right)_L / \left( \frac{dp}{dz} \right)_G \right]^{0.5} = \left( \frac{1-x}{x} \right)^{0.5} \left( \frac{\rho_G}{\rho_L} \right)^{0.5} \left( \frac{\mu_L}{\mu_G} \right)^{0.5} \quad (4.27)$$

Friedel (1979) developed a correlation with 25,000 data points. The smallest pipe diameter used is 4 mm. The correlation includes the gravity effect through the Froude number ( $Fr$ ), and the effects of surface tension and total mass flux using the Weber number ( $We$ ). The correlation is the following form

$$\phi_L^2 = E + \frac{3.24FH}{Fr_H^{0.45} We_L^{0.035}} \quad (4.28)$$

The dimensionless factors  $Fr_H$ ,  $F$  and  $H$  are as follows:

$$E = (1-x^2) + x^2 \frac{\rho_L f_G}{\rho_G f_L} \quad (4.29)$$

$$F = x^{0.78} (1-x)^{0.224} \quad (4.30)$$

$$H = \left( \frac{\rho_L}{\rho_G} \right)^{0.91} \left( \frac{\mu_G}{\mu_L} \right)^{0.19} \left( 1 - \frac{\mu_G}{\mu_L} \right)^{0.7} \quad (4.31)$$

The liquid Weber  $We_L$  is defined as:

$$We_L = \frac{GD_h}{\sigma \rho_H} \quad (4.32)$$

Using the following alternative definition of the homogeneous flow density  $\rho_H$  based on vapor quality:

$$\rho_H = \left( \frac{x}{\rho_G} + \frac{1-x}{\rho_L} \right)^{-1} \quad (4.33)$$

### 4.3 Heat Transfer Characteristics

The average Nusselt number for single phase and segmented flow was defined as:

$$Nu = \frac{hD_h}{k_L} \quad (4.34)$$

where  $h$  is heat transfer coefficient and  $k_L$  is the thermal conductivity of water. The value of heat flux and heat transfer coefficient are calculated as:

$$h = \frac{q''}{T_{wall} - T_{fluid}} \quad (4.35)$$

$$q'' = \frac{Q_{Bulk}}{(2H + W)L} \quad (4.36)$$

where  $T_{wall}$  is the average wall temperature using linear extrapolation from five rows of two T-type thermocouples.  $T_{fluid}$  is the average value fluid temperature defined as

$$T_{fluid} = 0.5(T_{fluid,in} + T_{fluid,out}) \quad (4.37)$$

The total heat transfer to the fluid was determined from using a simple energy balance from inlet to exist:

$$Q_{bulk} = m C_p (T_{f,out} - T_{f,in}) \quad (4.38)$$

The thermal equilibration of air and water in segmented flow allows the determination of the heat capacity as mass averaged properties.

$$C_p = \phi C_{p,water} + (1 - \phi) C_{p,air} \quad (4.39)$$

where the mass fraction of water is

$$\phi = \left( \frac{\rho_{water} Q_{water}}{\rho_{water} Q_{water} + \rho_{air} Q_{air}} \right) \quad (4.40)$$

$\rho_{water}$  and  $\rho_{air}$  are the water and air densities respectively.

## CHAPTER 5 RESULTS AND DISCUSSION

In this chapter, the results of adiabatic two-phase flow patterns, flow regime maps, frictional pressure drop and heat transfer characteristics are presented and discussed.

### 5.1 Adiabatic Two-phase flow patterns and flow pattern transitions

#### 5.1.1 Flow patterns

Four different two-phase flow patterns were identified, namely, the segmented flow, throat-annular, throat-annular/liquid and annular flow as shown in Figure 5.1

##### a) Segmented Flow

This flow pattern features liquid slugs alternating with air bubbles. With the width of the bubbles close to the width of the channel, the length of the bubble would be longer than the hydraulic diameter of the channel. No water droplets were recognized in the air bubbles, nor are any air bubbles presents in the water slugs, as well. After all, segmented flow is also called plug, Taylor, slug, bubble-train, and intermittent flow.

##### b) Annular flow

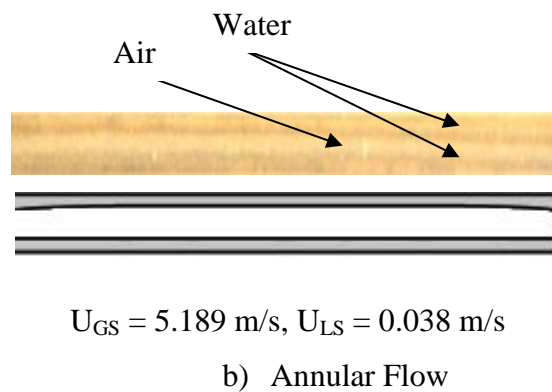
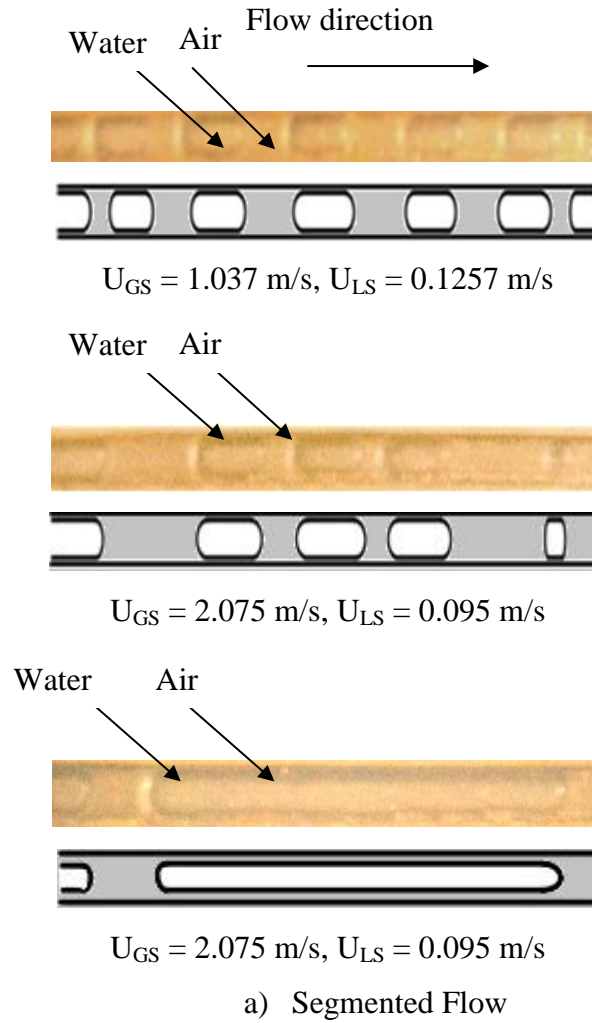
In this study, annular flow was observed at the lowest range liquid superficial velocity  $U_{LS}$  and at the rising of gas superficial velocity  $U_{GS}$  respectively. The volume of liquid is flowing through the channel as thin film around the microchannel wall.

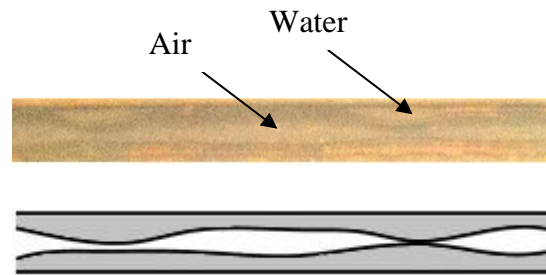
##### c) Throat-annular flow

Throat-annular flow, also known as the Taylor-annular, ring, slug-ring flow, and slug-annular flow is the flow pattern of the two consecutive bubbles coalescence. In this pattern, a gas core is surrounded by a liquid film where large-amplitude waves appear in the liquid film, small bubbles are sometimes presented in the liquid. These are considered to be the transition zone into the next flow pattern between the annular and slug-annular/liquid flow when the liquid phase rises to high velocities.

d) Throat-annular/ Liquid flow

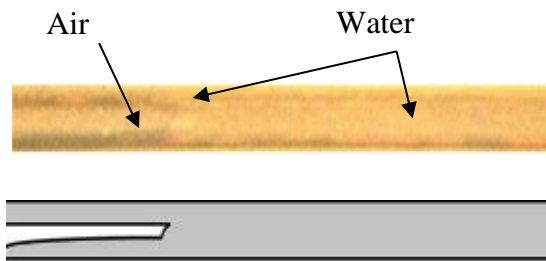
This flow pattern is characterized by periodic oscillation between throat-annular flow and single phase liquid flow. It is observed when the ULS is higher, and the wave of the water throat-annular side wall reaches the wave of water film on the opposite side.



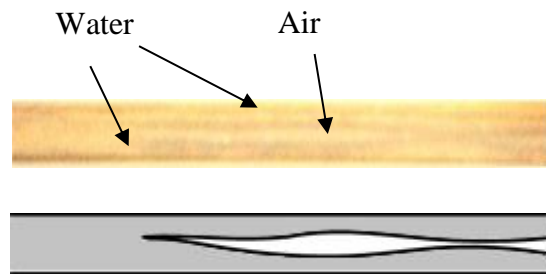


$$U_{GS} = 3.113 \text{ m/s}, U_{LS} = 0.08865 \text{ m/s}$$

c) Throat-annular flow



$$U_{GS} = 1.557 \text{ m/s}, U_{LS} = 0.1118 \text{ m/s}$$



$$U_{GS} = 3.113 \text{ m/s}, U_{LS} = 0.1796 \text{ m/s}$$

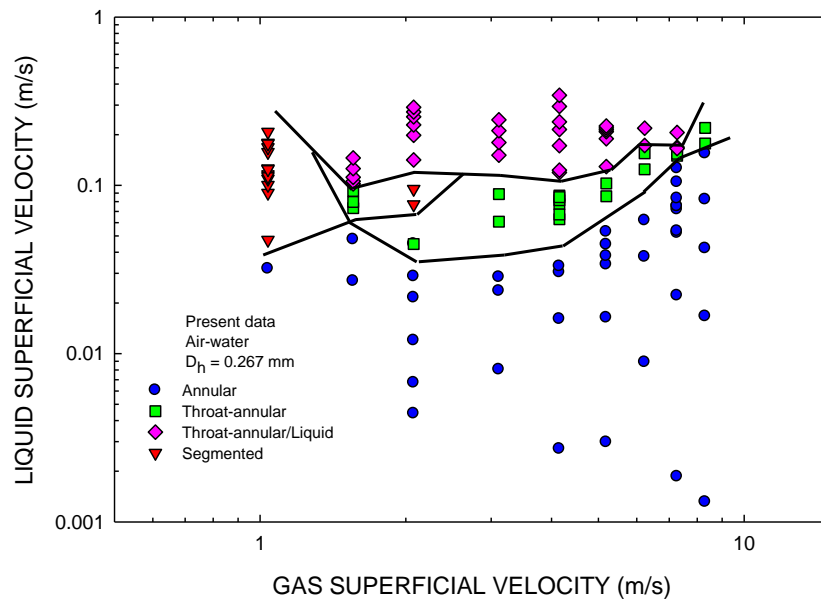
d) Throat-Annular/Liquid Flow

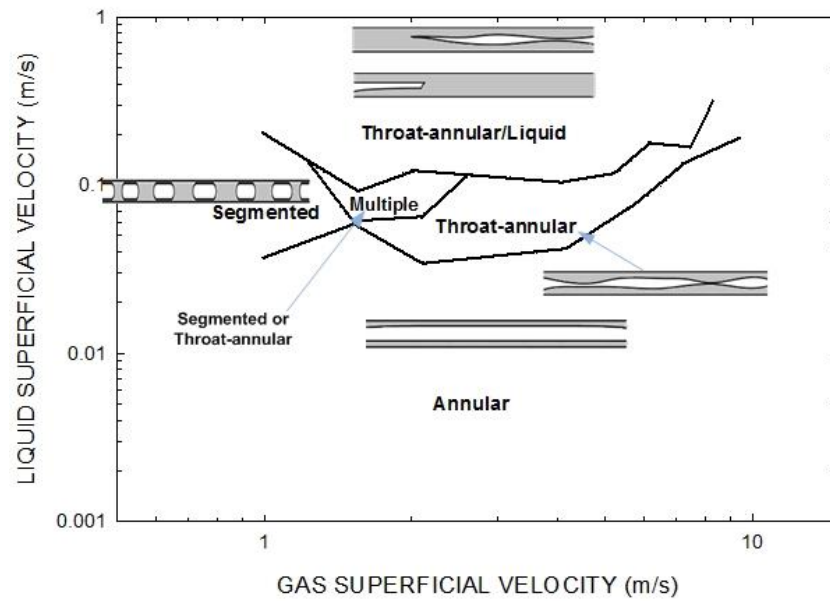
**Figure 5.1** Flow visualizations of two-phase air-water flow patterns in the 267  $\mu\text{m}$  of hydraulic diameter rectangular microchannel test section

### 5.1.2 Flow regime maps

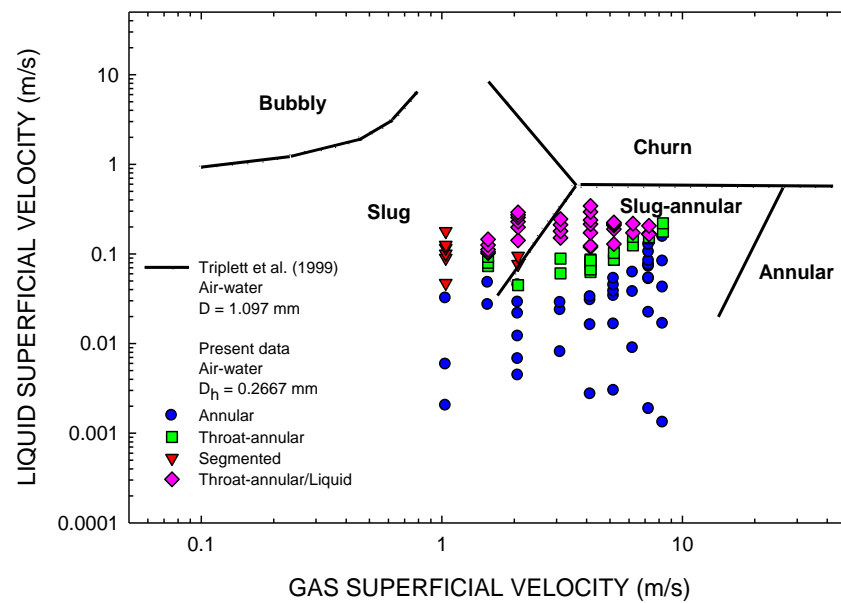
Illustrates the flow regime map of this experiment; using  $U_{GS}$  and  $U_{LS}$  as coordinates, we found that segmented flow occurred at the lowest range of  $U_{GS}$ . When the  $U_{GS}$  rises, the bubble's size grows and expanded along the channel. This effect causes the reduction of the segmented flow pattern and then changes to another flow pattern as throat-annular, throat-annular/liquid, and annular flow up to the rates of  $U_{GS}$  and  $U_{LS}$ .

The flow regime maps in Figure 5.3 – Figure 5.8 were developed by Triplett et al. (1999), Kawahara et al. (2002), Qu et al. (2004), Waelchli and von Rohr (2006), Saisorn and Wongwises (2008), and Wang et al. (2012). The criteria used to select the flow maps are the similar channel dimensions and similar working fluids. In some of these previous studies, the segmented flow was categorized as slug or intermittent flow, the throat-annular is categorized as slug-annular or ring or ring-slug without distinction. For clarity, only the transition boundary lines are shown in the flow map results from the literature, and the individual flow regime is marked in the text accordingly.

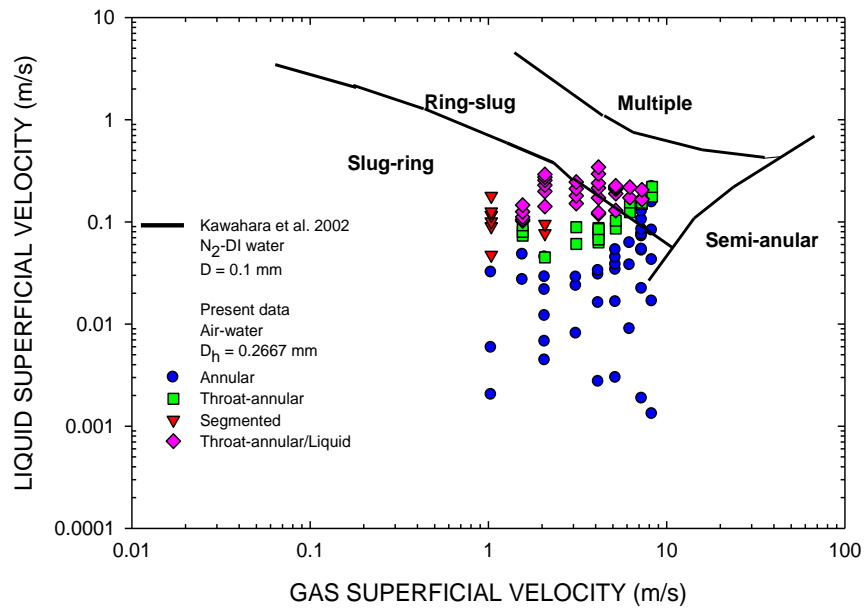




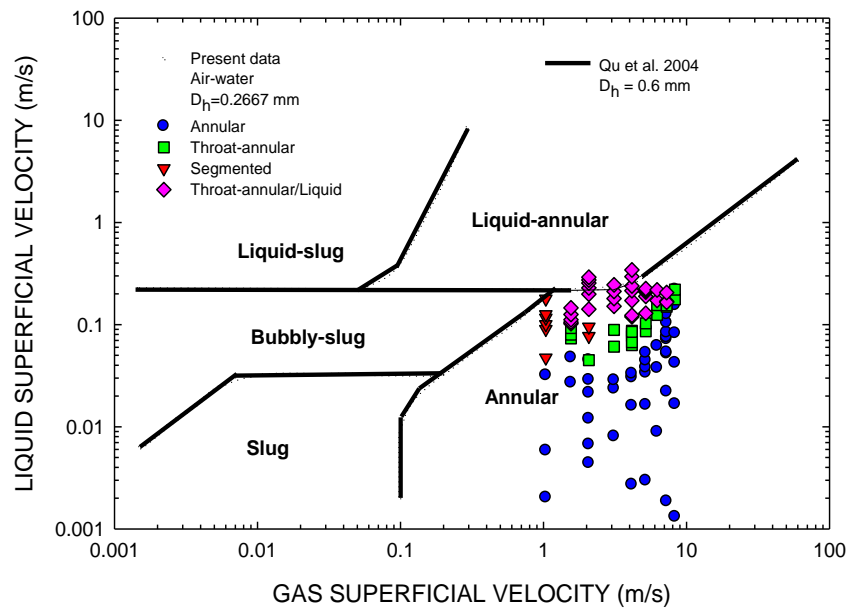
**Figure 5.2** Two-phase flow pattern map for two-phase air-water flow through a 267  $\mu\text{m}$  diameter channel



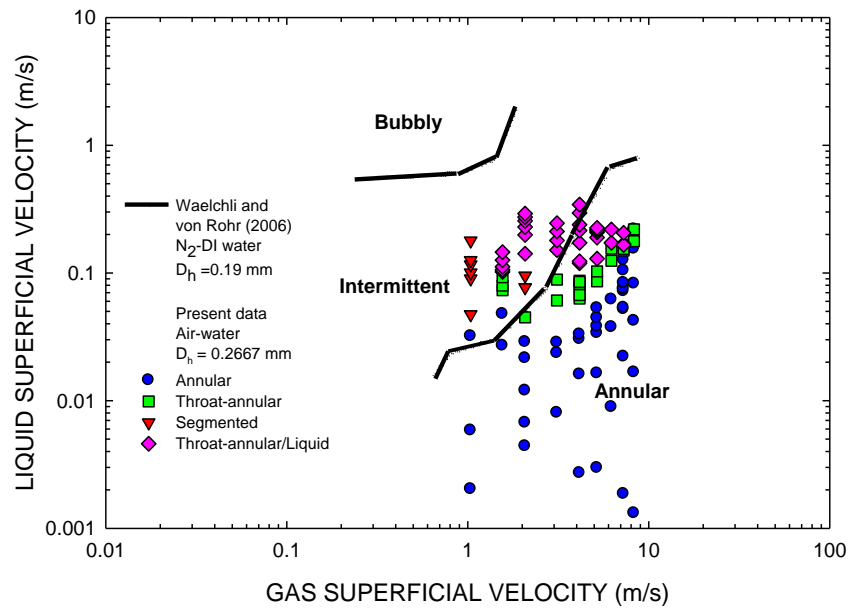
**Figure 5.3** Comparison of the observed flow patterns with the transition lines by Triplett et al. (1999)



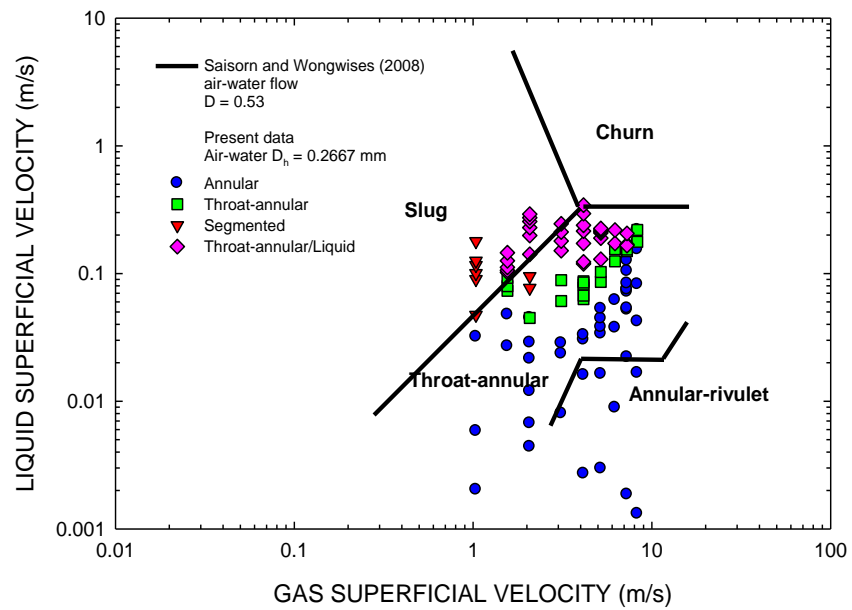
**Figure 5.4** Comparison of the observed flow patterns with the transition lines by Kawahara et al. (2002)



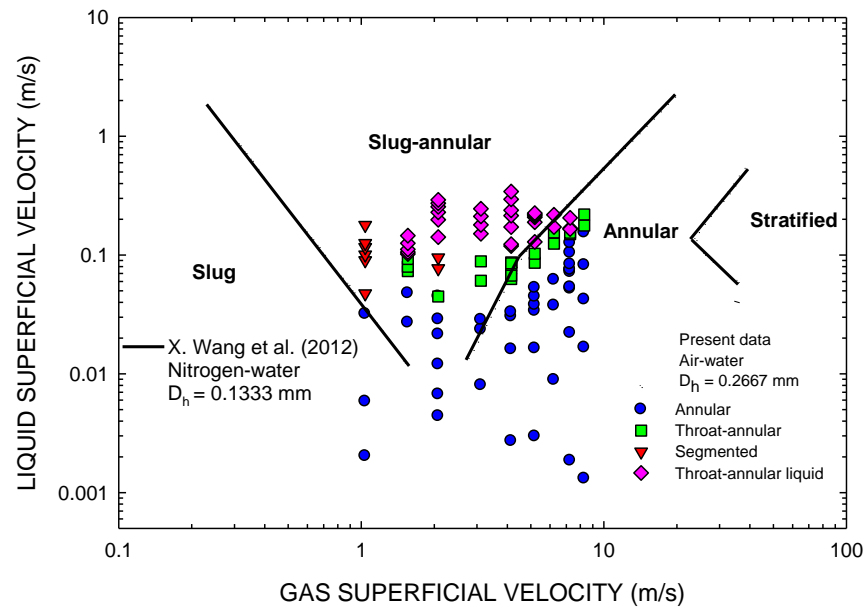
**Figure 5.5** Comparison of the observed flow patterns with the transition lines by Qu et al. (2004)



**Figure 5.6** Comparison of the observed flow patterns with the transition lines by Waelchli and von Rohr (2006)



**Figure 5.7** Comparison of the observed flow patterns with the transition lines by Saisorn and Wongwises (2008)



**Figure 5.8** Comparison of the observed flow patterns with the transition lines by X. Wang et al. (2012)

The predictions of these authors are in reasonable agreement with the experimental observations in the flow pattern as conclusion of the table 5.1.

**Table 5.1** Summary of predictable flow regime maps

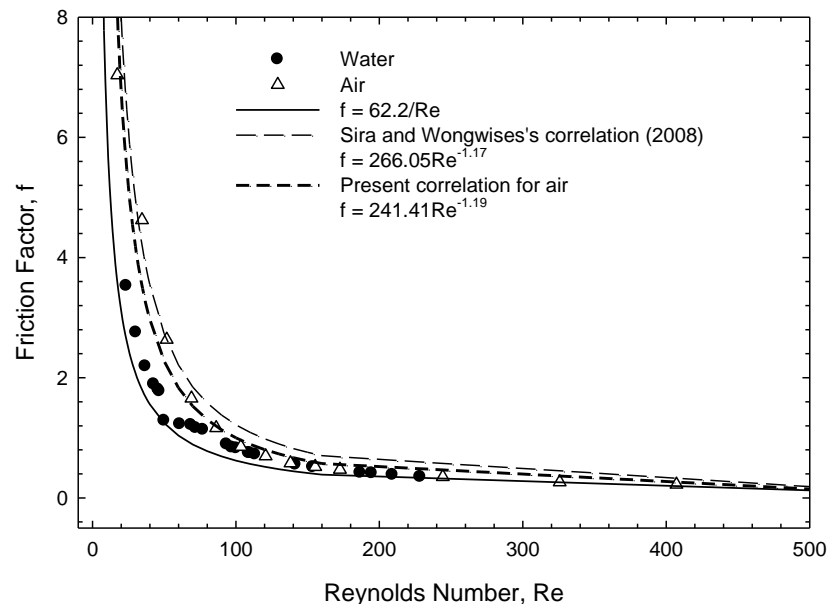
Year	Authors	Working			Well-predicted flow patterns
		fluids	Geometry	Hydraulics diameter (mm)	
1999	Triplett et al.	Air-water	Circular	1.097	Segmented, Throat-annular
2002	Kawahara et al.	N <sub>2</sub> -DI water	Circular	0.1	Segmented
2004	Qu et al.	Air-water	Rectangular	0.6	Annular
2006	Waelchli and von Rohr	N <sub>2</sub> -DI water	Rectangular	0.19	Annular, Segmented
2008	Saisorn and Wongwises	Air-water	Circular	0.53	Annular, Segmented
2012	Wang et al.	N <sub>2</sub> -water	Rectangular	0.1333	Throat-annular, Annular

## 5.2 Pressure drop

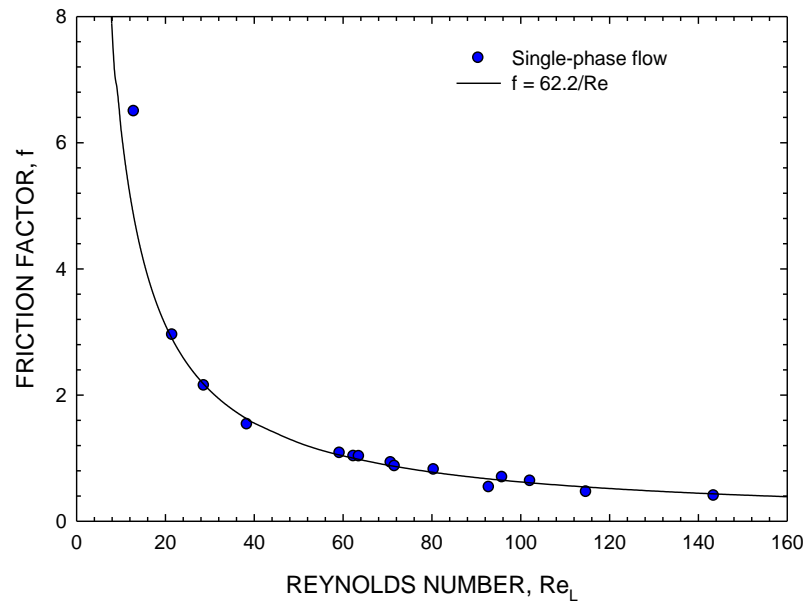
### 5.2.1 Single-phase pressure drop

The single-phase of air and water flow through the channel are the first experiment to investigate the friction factor. In Figures 5.9 and 5.10, the friction factor data calculated from the experiment of single-phase of water both of adiabatic and non-boiling flow are fairly agree well with  $f = 62.2/Re$  that obtained from the conventional sized channel. Nevertheless, the results obtained from air flow are relatively high from  $f = 62.2/Re$  line and rather close to Saisorn and Wongwises's (2008) correlation. For this study, the correlation for laminar air flow is developed and expressed in

$$f = 241.41Re^{-1.19}$$



**Figure 5.9** Experimental friction factor data for adiabatic air and water flow through a 267  $\mu\text{m}$  mm diameter channel

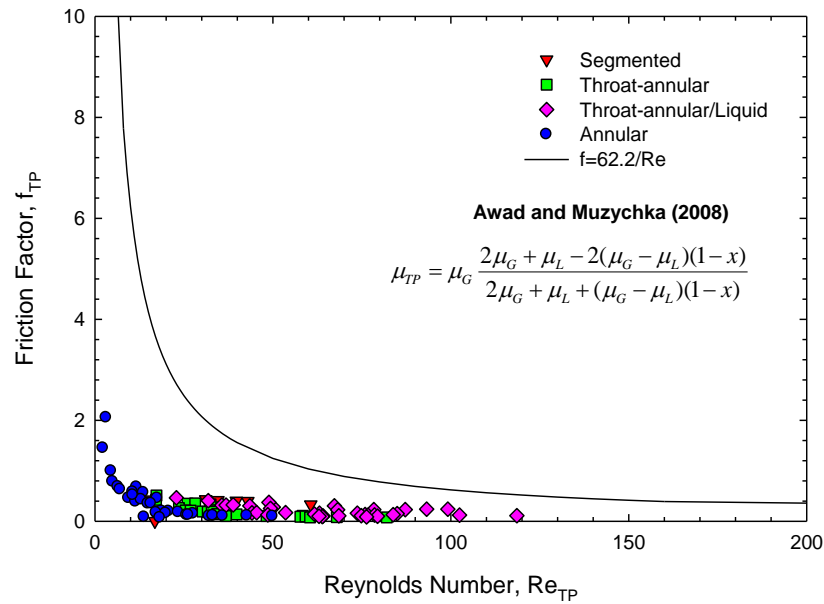


**Figure 5.10** Experimental friction factor data for nonboiling water flow through a 267  $\mu\text{m}$  mm diameter channel

## 5.2.2 Two-phase pressure drop

### 5.2.2.1 Homogeneous flow model

Figure 5. shows the two-phase friction factor and Reynolds number for various flow patterns by using Awad and Muzychka's two-phase viscosity model, which predicts the two-phase pressure drop of adiabatic segmented, throat-annular, and throat-annular/liquid in the agreement of 30% MAE. However, all existing models over-predicted pressure drop data for annular flow.



**Figure 5.11** Two-phase friction factor and Reynolds number for the various adiabatic flow pattern using Awad and Muzychka’s two-phase viscosity model

The predictions with various viscosity models are shown in Table 5.2

**Table 5.2** Effective mean viscosity models

Flow pattern	%MAE of the predictions with various viscosity model					
	McAdams et al. (1942)	Owen (1961)	Dukler et al. (1964)	Beattie and Whalley (1982)	Lin et al. (1991)	Awad and Muzychka (2008)
Segmented	63.3	35.5	94.2	84.4	44.6	36.1
Throat-annular	61.2	31.1	94.5	88.0	27.7	22.3
Throat-annular/liquid	63.7	31.6	94.7	86.1	42.2	32.4
Annular	65.3	176	91.9	87.6	37.9	83.0

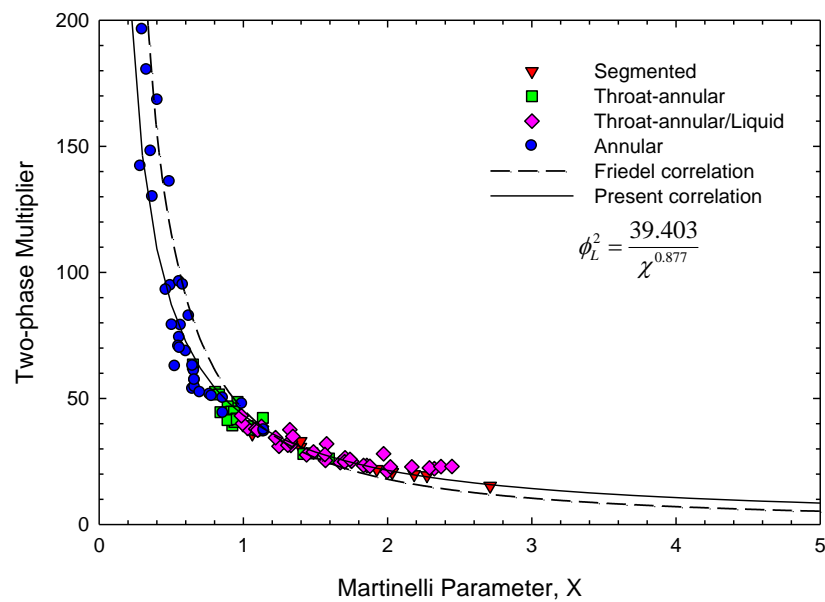
### 5.2.2.2 Separated flow model

#### 5.2.2.2.1 Adiabatic flow

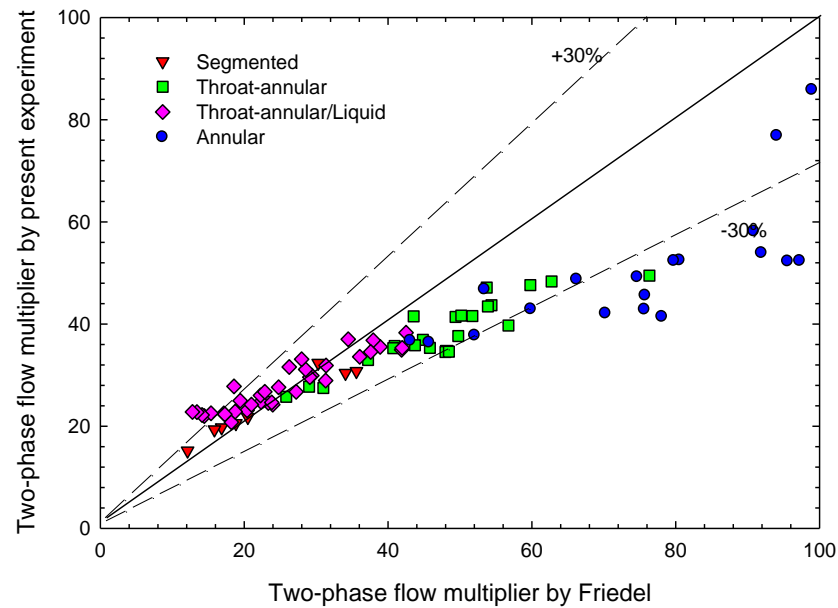
Figure 5.12 shows a comparison of the two-phase friction multiplier data for various adiabatic flow patterns; the predictions by the Lockhart-Martinelli parameter in comparison with the Friedel correlation are also shown in the same figure as the calculated curve. All the flow pattern data are well correlated with the Friedel

correlation. The results from the calculation agree with the measured data within 30% deviation, irrespective of the working fluid, as shown in Fig. 5.13. Further, we proposed the new correlation to predict the two-phase frictional multiplier which developed based on the experimental data as is offered in

$$\phi_L^2 = \frac{39.403}{X^{0.877}}$$



**Figure 5.12** Martinelli parameter versus the two-phase frictional multiplier for various adiabatic flow patterns

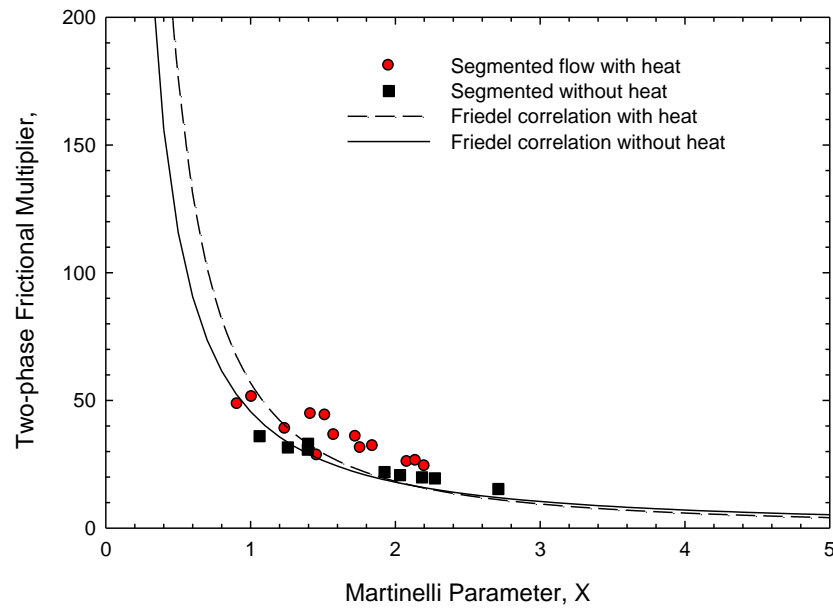


**Figure 5.13** Predicted pressure drop by Friedel correlation versus experimental pressure drop for various adiabatic flow patterns

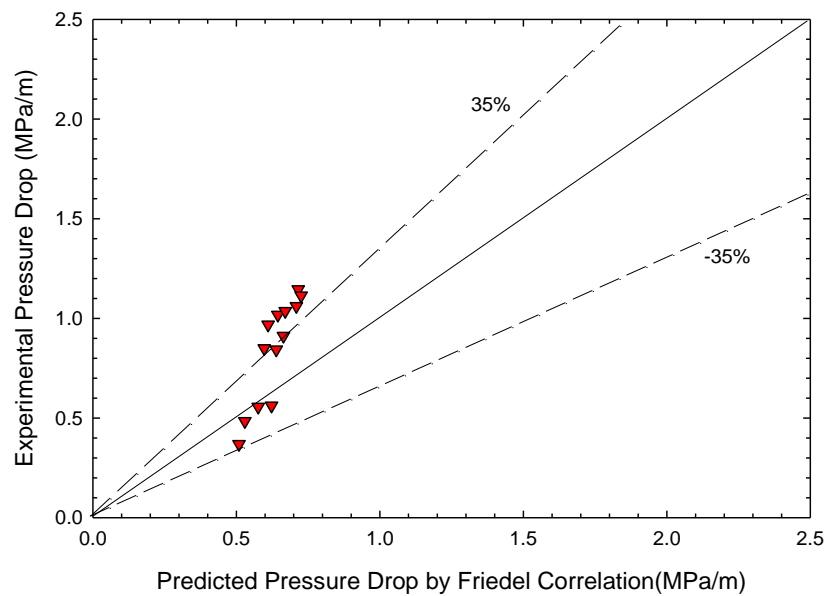
#### 5.2.2.2.2 Nonboiling flow

Figure 5.14 shows the comparison of the Lockhart-Martinelli parameter versus the two-phase frictional multiplier for the nonboiling segmented flow with and without heat transfer and the Friedel correlation.

We found that the two-phase frictional multiplier increased by changing to adiabatic to nonadiabatic flow. Likewise, a comparison between two-phase flow multiplier by Friedel correlation and experimental data is presented in Fig. 5.15, which contains the 35% deviation and provides the predictive accuracy of the corresponding correlations.



**Figure 5.14** Comparison of segmented friction loss with and without heat transfer and the correlation

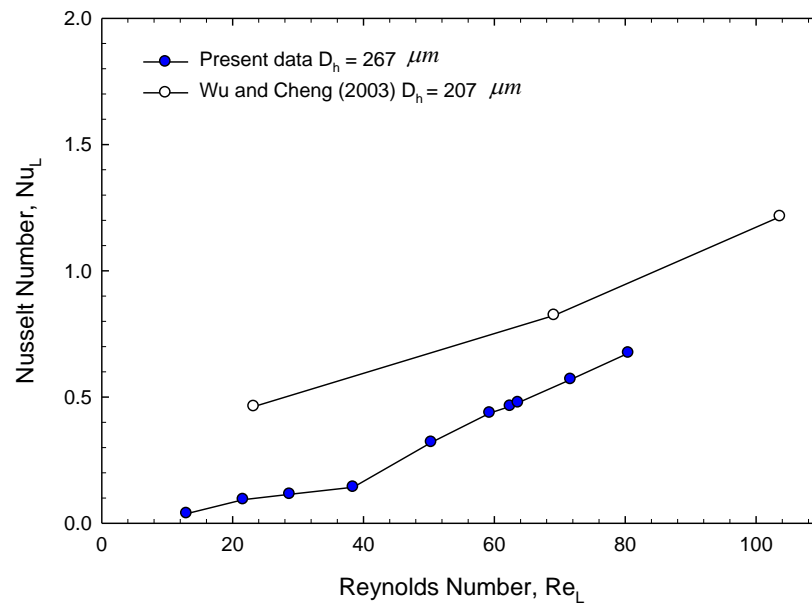


**Figure 5.15** Predicted pressure drop by Friedel correlation versus experimental pressure drop for various nonboiling segmented flow patterns

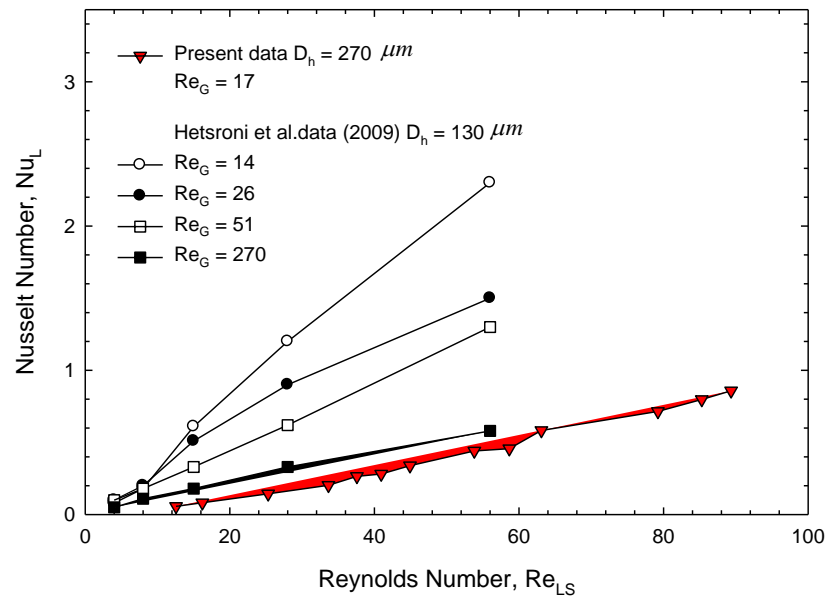
## 5.3 Heat transfer characteristics

### 5.3.1 Single-phase flow

The single-phase and two-phase heat transfer experiment was first conducted to confirm the validity of the experiment setup at as Fig. 5.16 and Fig. 5.17 respectively. The experimental data agree with Wu and Cheng (2003) as Fig. 5.16 and Hetsroni et al. (2009) as Fig. 5.17 which studied heat transfer in the parallel triangular channels of  $130\ \mu\text{m}$  in hydraulic diameter.



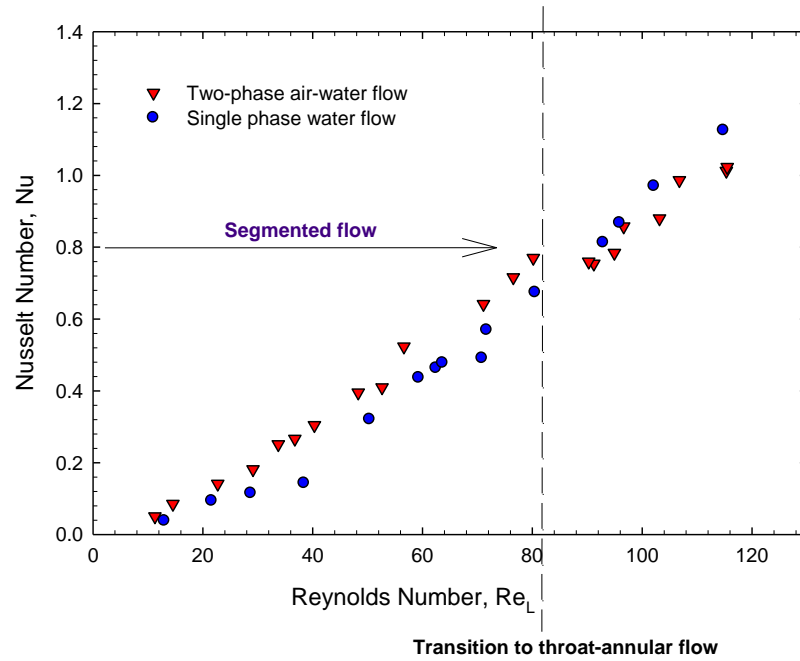
**Figure 5.16** The comparison of Nusselt number versus Reynolds with the existing results of other researcher for single-phase flow



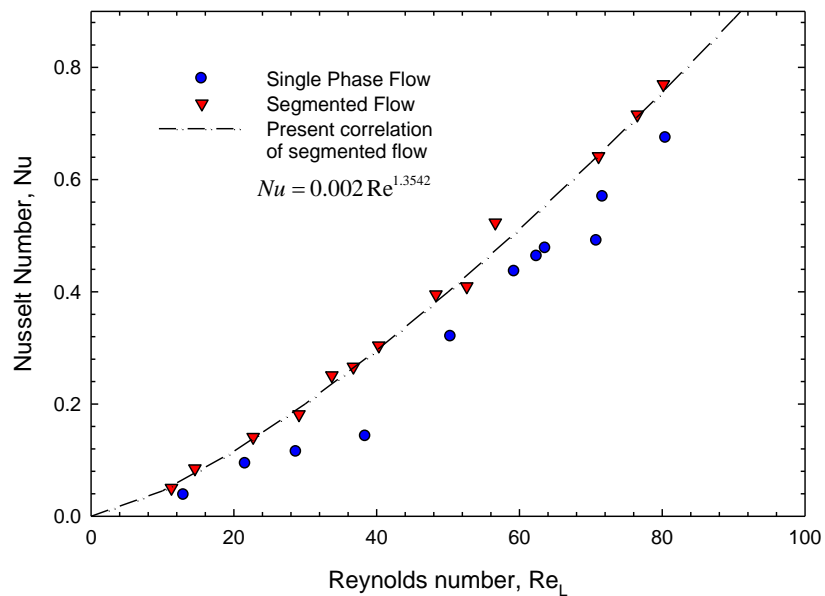
**Figure 5.17** The comparison of Nusselt number versus Reynolds with the existing results of other researcher for two-phase flow

### 5.3.1 Segmented flow

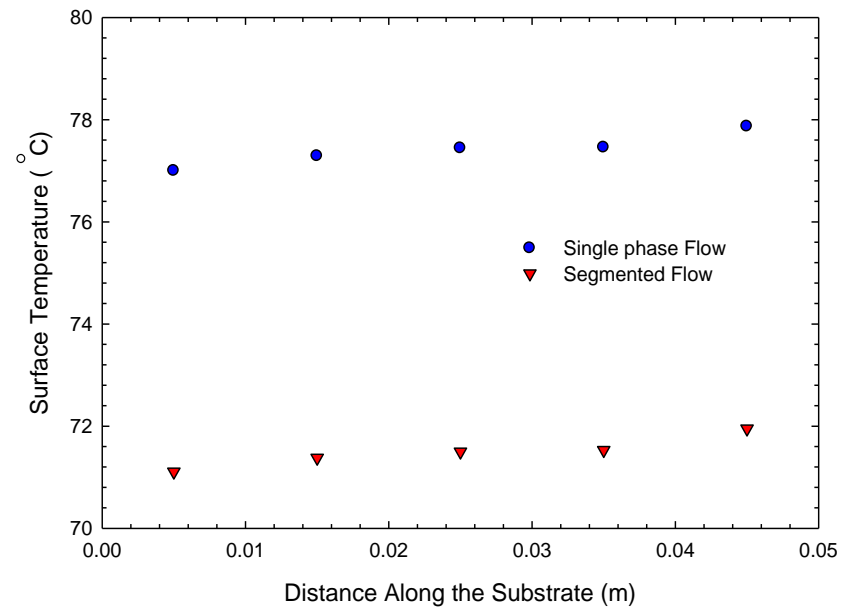
Additionally, Fig. 5.19 shows the segmented flow increases the Nusselt number up to 120% over the single-phase flow in the low Reynolds number range. It should be noted that when the segmented flow changes to another flow pattern, such as what occurs in Fig. 5.18, it is not important to enhance heat transfer with two-phase air-water from single-phase of water anymore. These phenomena are in agreement with the research of Betz and Attinger (2010). Figure 5.20 shows the surface temperature at the channel wall. We found that the wall temperature of single-phase flow is higher than segmented flow. This finding ensures that segmented flow can enhance heat transfer in a rectangular microchannel. The temperature of the surface that increases linearly also indicates that fluid flow through the channel is in the constant heat flux.



**Figure 5.18** Nusselt number of single-phase and two-phase flow versus the Reynolds number with water flow rate at a fixed gas flow rate



**Figure 5.19** The Value of Nusselt number for single-phase and segmented flow versus the Reynolds number with water flow rate at a fixed gas flow rate



**Figure 5.20** Surface temperature,  $T_s$ , along the flow direction, for a water flow rate of  $7.32 \times 10^{-4}$  kg/min, in the single phase and segmented flow case

## **CHAPTER 6 CONCLUSION AND RECOMMENDATIONS FOR FUTURE WORK**

This chapter presents the conclusion and recommendations for future work. In the part of conclusion, the important conclusions of this thesis are categorized into subsections as follows:

### **6.1 Conclusion**

The flow pattern images were analyzed to obtain the new transition lines in the flow regime map. The gas superficial velocity and liquid superficial velocity were varied in a range of  $U_{GS} = 1.038 - 8.302$  m/s and  $U_{LS} = 0.001311 - 0.3429$  m/s, respectively. The flow patterns including annular flow, segmented flow, throat-annular flow and throat-annular/liquid flow were observed through the stereo-zoom microscope. When comparing the flow regime map to other research, we report a new finding associated with the flow pattern and flow regime map, measured in the lower range of superficial velocity.

The pressure drop in the adiabatic and nonboiling flow was measured and compared with the homogeneous flow model as the various viscosity flow correlations and separated flow model of the Friedel correlation. We found that the Awad and Muzychka (2008) viscosity correlation can predict the frictional pressure drop of segmented, throat-annular and throat-annular/liquid in 30% MAE. The Friedel correlation separated flow model can predict the frictional pressure drop of segmented, throat-annular and throat-annular/liquid of adiabatic flow in 30% deviation and nonboiling segmented flow in 35% deviation.

Segmented air-water flow can enhance heat transfer by up to 120% in a rectangular microchannel, in comparison with single-phase flow at the same liquid flow rate. The Nusselt number was used to characterize the improvement in heat transfer (Betz and Attinger 2010).

## **6.2 Recommendations for Future Work**

The experimental apparatus can be applied for investigating the heat transfer characteristics of another working fluids and optimize the the test devices, the feature, size, shape and the material of the test-section.



AN EXPERIMENTAL STUDY OF SEGMENTED TWO-PHASE FLOW AND  
HEAT TRANSFER CHARACTERISTICS IN A MICROCHANNEL

MISS PANSUNEE SUWANKAMNERD

A THESIS SUBMITTED IN PARTIAL FULFILLMENT  
OF THE REQUIREMENTS FOR  
THE DEGREE OF MASTER OF ENGINEERING  
(MECHANICAL ENGINEERING)  
FACULTY OF ENGINEERING  
KING MONGKUT'S UNIVERSITY OF TECHNOLOGY THONBURI  
2013

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